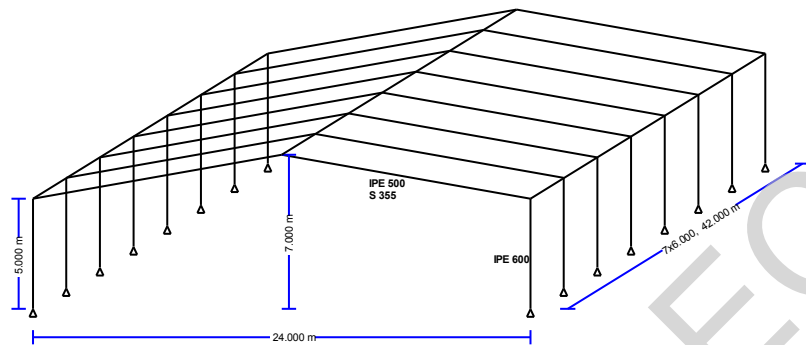


Example Report**1. Design codes**

EN1990:2002, Eurocode 0 Basis of Structural Design
 EN1991-1-1:2002, Eurocode 1-1 Actions on structures
 EN1991-1-3:2003, Eurocode 1-3 Snow loads
 EN1991-1-4:2005, Eurocode 1-4 Wind actions
 EN1993-1-1:2005, Eurocode 3 1-1 Design of Steel structures
 EN1993-1-3:2005, Eurocode 3 1-3 Cold-formed members
 EN1993-1-5:2006, Eurocode 3 1-5 Plated structural elements
 EN1993-1-8:2005, Eurocode 3 1-8 Design of Joints
 CEN/TS 1992-4-1:2009, Design of fastenings in concrete, General
 CEN/TS 1992-4-2:2009, Design of fastenings, Headed Fasteners
 EN1992-1-1:2004, Eurocode 2 Reinforced concrete
 EN1997-1-1:2004, Eurocode 7 Geotechnical design

2. Basic data**2.1. Geometry of frame structure**

Bay width $L = 24.000$ m
 Total height(max) $H = 7.000$ m
 Column height $H1 = 5.000$ m
 Total length $B = 42.000$ m (7x6.000m)
 Spacing of frames $s = 6.000$ m
 Roof slope $\alpha = 9.46^\circ$
 Haunch size $L1 = L/10.0 = 2.400$ m
 Cladding Sheetting thickness $t_w = 0.750$ mm, Profile depth $h_w = 40.0$ mm
 Purlin spacing $= 3.000$ m
 Purlin laterally restrained, Continuous purlin

2.2. Steel sections

Column section IPE 600 - S 355
 Rafter section IPE 500 - S 355
 Purlin section IPE 160 - S 355
 Transverse restraint system L100x100x10 - S 355
 Lateral bracing of columns $L_{m1} = 4.250$ m
 Torsional restrains of rafters $L_{m2} = 3.201$ m
 Compression stiffener at the bottom of haunch

2.3. Steel joints

Type of connection End-plate connection, non-preloaded bolts
 Category of connection Category A: Bearing type
 Category D: Non-preloaded
 End Plate Thickness $t_p=20$ mm, S 235
 Bolts M24, Grade 10.9

2.4. Column base and foundation

Base plate steel grade Thickness $t_p=30$ mm, S 235
 Anchor bolts M24, Grade 5.6
 Concrete of foundation C25/30-B500C
 Concrete cover $C_{nom}=35$ mm
 Soil bearing capacity $q_u=0.200$ kN/mm²
 Unit weight of soil $\gamma=18.00$ kN/m³
 Foundation depth $h_f=2.700$ m

3. Materials and Code parameters

3.1. Materials

Steel: S 355 (EN1993-1-1, §3.2)

$t \leq 40$ mm, Yield strength $f_y=355$ N/mm², Ultimate strength $f_u=510$ N/mm²
 $40\text{mm} < t \leq 80$ mm, Yield strength $f_y=335$ N/mm², Ultimate strength $f_u=470$ N/mm²
 Modulus of elasticity $E=210000$ N/mm², Poisson ratio $\nu=0.30$, Unit mass $\rho=7850$ Kg/m³

Partial factors for materials (EN1993-1-1, §6.1)

$\gamma_{M0}=1.00$, $\gamma_{M1}=1.00$, $\gamma_{M2}=1.25$

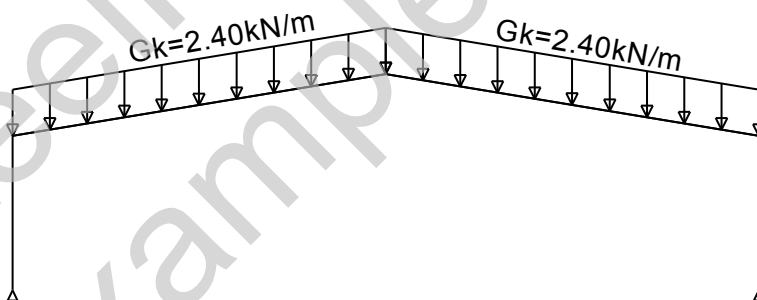
4. Loads

4.1. Permanent loads

(EN1991-1-1)

Self weight of purlins and finishing $g_{k1} = 0.200 + 0.155/3.000 = 0.252$ kN/m²
 Self weight of ceiling under the roof $g_{k2} = 0.000$ kN/m² $g_k = g_{k1} + g_{k2} = 0.252$ kN/m²
 Spacing of frames $s = 6.000$ m
 Roof load on frame $(g_{k1} + g_{k2}) \cdot s = 0.252 \times 6.000 = 1.51$ kN/m
 Self weight of Rafters $G(\text{IPE } 500) = 0.89$ kN/m
 Permanent load on frame $G_k = 1.51 + 0.89 = 2.40$ kN/m
 Self weight of Columns $G(\text{IPE } 600) = 1.20$ kN/m

Load G (Permanent load)

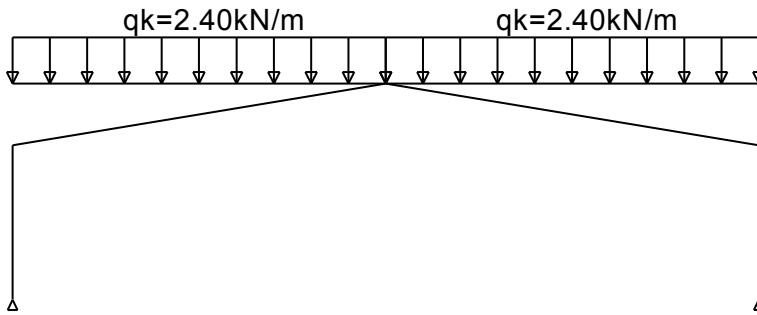


(EC1 EN1991-1-1:2002 Tab.6.10)

4.2. Imposed loads

Roof slope $\alpha = 9.46^\circ$
 Imposed load (category H) $q_k = 0.40$ kN/m²
 Roof load on frame $q_k \cdot s = 0.40 \times 6.000 = 2.40$ kN/m

Load Qk (Imposed load)



4.3. Snow load

(EC1 EN1991-1-3:2003)

Snow load on the ground

(EN1991-1-3 §4, Annex C)

Characteristic value of snow load on the ground: $s_k=0.800 \text{ kN/m}^2$

Snow load on the roof

(EC1 EN1991-1-3:2003, §5,)

pitched roof (EC1-1-3 §5.3.3)

Angle of pitch of roof : $\alpha_1=9.462^\circ$

Angle of pitch of roof : $\alpha_2=9.462^\circ$

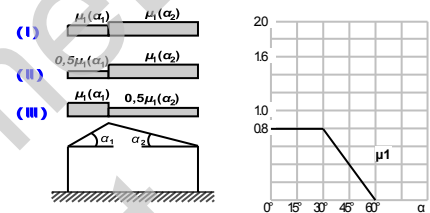
Exposure coefficient : $C_e=1.000$ (EC1-1-3 §5.2 (7))

Thermal coefficient : $C_t=1.000$ (EC1-1-3 §5.2 (8))

Shape coefficients $\mu_1(\alpha_1)=\mu_1(\alpha_2)=0.800$ (EC1-1-3 T.5.2)

$S(\alpha_1)=\mu_1(\alpha_1) \cdot C_e \cdot C_t \cdot S_k=0.800 \times 1.000 \times 1.000 \times 0.800=0.640 \text{ kN/m}^2$

$S(\alpha_2)=\mu_1(\alpha_2) \cdot C_e \cdot C_t \cdot S_k=0.800 \times 1.000 \times 1.000 \times 0.800=0.640 \text{ kN/m}^2$



Snow load

(EC1 EN1991-1-3:2003, §5.2, §5.3.3)

Load case (I) , $S(\text{Left})=S(\alpha_1) = 0.640 \text{ kN/m}^2$, $S(\text{Right})=S(\alpha_2) = 0.640 \text{ kN/m}^2$

Load case (II) , $S(\text{Left})=0.5 \times S(\alpha_1) = 0.320 \text{ kN/m}^2$, $S(\text{Right})=S(\alpha_2) = 0.640 \text{ kN/m}^2$

Load case (III) , $S(\text{Left})=S(\alpha_1) = 0.640 \text{ kN/m}^2$, $S(\text{Right})=0.5 \times S(\alpha_2) = 0.320 \text{ kN/m}^2$

4.4. Snow load on frame

(EC1 EN1991-1-3:2003)

Snow load on the ground $s_k= 0.800 \text{ kN/m}^2$

Snow load on the roof $S_k= 0.8 \times 0.800 \times 1.00 \times 1.00 = 0.640 \text{ kN/m}^2$

Spacing of frames $s= 6.000 \text{ m}$

Snow load on frame $Sk_1= 0.640 \times 6.000 / \cos 9.46^\circ = 3.89 \text{ kN/m}$

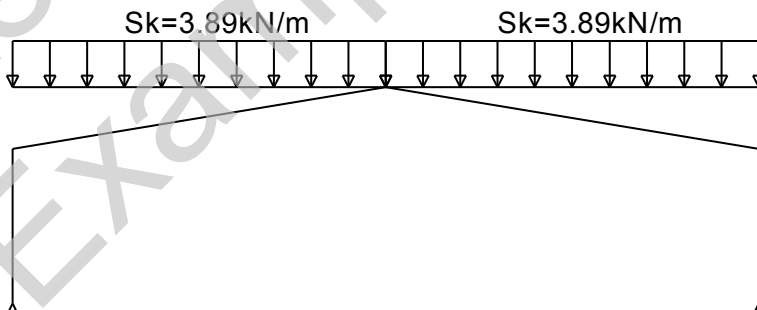
$Sk_2= 0.5 \times 0.640 \times 6.000 / \cos 9.46^\circ = 1.95 \text{ kN/m}$

Load case (I) $Sk_1= 3.89 \text{ kN/m}$, $Sk_2= 3.89 \text{ kN/m}$

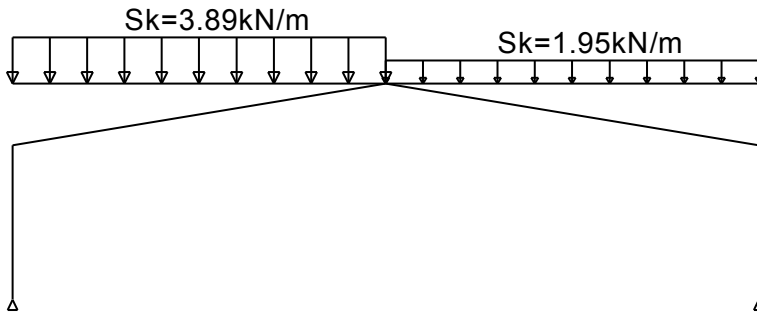
Load case (II) $Sk_1= 3.89 \text{ kN/m}$, $Sk_2= 1.95 \text{ kN/m}$

Load case (III) $Sk_1= 1.95 \text{ kN/m}$, $Sk_2= 3.89 \text{ kN/m}$

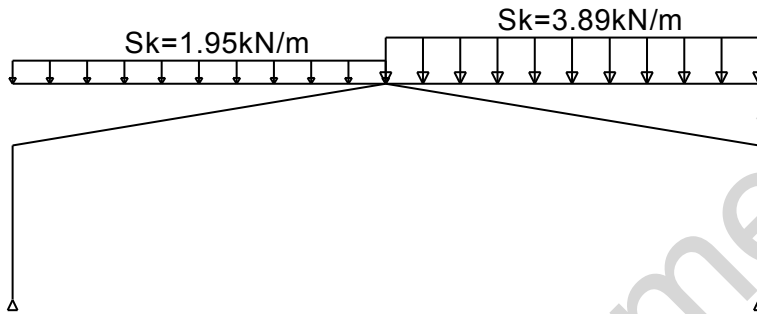
Load Qs1 (Snow load)



Load Qs2 (Snow load)



Load Qs3 (Snow load)



4.5. Wind load

(EC1 EN1991-1-4:2005)

Terrain effects

(EN1991-1-4, §4.3.2, Annex A)

Terrain category : 0 (EN1991-1-4, Tab. 4.1)

Sea, coastal area exposed to the open sea

Roughness factor Cr(z) (EN1991-1-4, §4.3.2)

Terrain category: 0, z=7.000m, zo=0.003m, zmin=1m, zmax:=200m, zoII=0.050m

$kr=0.19 \cdot (0.003/0.05)^{0.07}=0.156$, $Cr(z)=kr \cdot \ln(z/zo)=0.156 \times \ln(7.000/0.003)=1.210$

Orography factor Co(z) (EN1991-1-4, §4.3.3)

Co(z)=0.000 (EN1991-1-4, §4.3.3)

Turbulence factor K1 (EN1991-1-4, §4.4)

Kt=1.000

Exposure factor Ce(z) (EN1991-1-4, §4.5)

Terrain category : 0 (EN1991-1-4, Tab. 4.1)

z= 7.00 m, kr=0.156, lv(z)=0.129, Ce (EN1991-1-4, eq. A.4.8, eq. A.4.7, eq. A.4.4, eq. A.4.3)

Wind peak velocity pressure q(z)=Ce(z) · qb =Ce(z) · (0.625) · Vb²

(EN1991-1-4, §4.5)

Vb=22.73m/sec

z=7.000m

Cr(z)=1.210

Co(z)=0.000

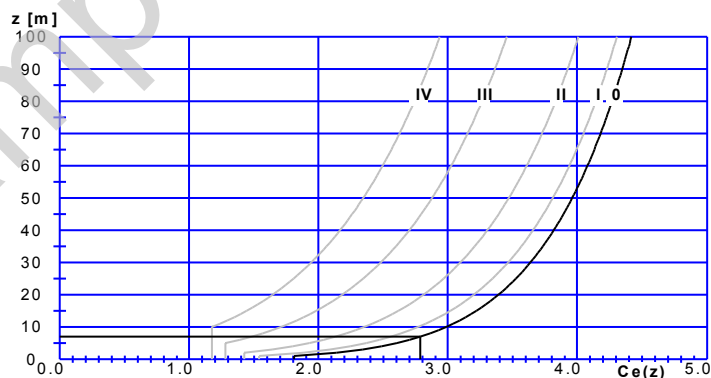
Kt=1.000

Ce(z)=2.786

$$q(z) = Ce(z) \cdot (\frac{1}{2} \rho) \cdot Vb^2$$

$$= Ce(z) \times 0.625 \times 22.73^2$$

$$= 0.900 \text{ N/m}^2$$



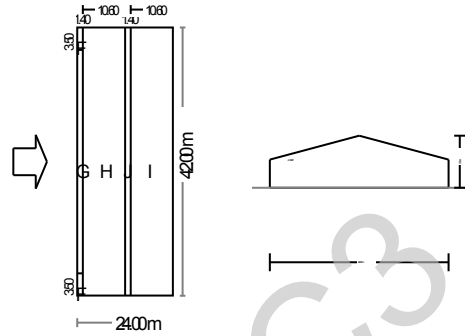
Wind forces on duopitch roof, wind direction: 0.00

(EN1991-1-4, §7.2.5)

Wind pressure coefficients Cpe

(EN1991-1-4, Tab. 7.4a)

wind direction: $\theta=0.00$
 $b=42.00\text{m}$, $d=24.00\text{m}$, $h=7.00\text{m}$, $e=\min(b,2h)=14.00\text{m}$
 $e/4=3.50\text{m}$, $e/10=1.40\text{m}$, $e/2=7.00\text{m}$
 Pitch angle: $\alpha=9.462$



- Zone : F, A= 4.97m², Cpe,10=-1.34, Cpe,1=-2.28
- Zone : F, A= 4.97m², Cpe,10=+0.09, Cpe,1=+0.09
- Zone : G, A= 49.68m², Cpe,10=-1.02, Cpe,1=-1.78
- Zone : G, A= 49.68m², Cpe,10=+0.09, Cpe,1=+0.09
- Zone : H, A= 451.34m², Cpe,10=-0.47, Cpe,1=-0.80
- Zone : H, A= 451.34m², Cpe,10=+0.09, Cpe,1=+0.09
- Zone : I, A= 451.34m², Cpe,10=-0.51, Cpe,1=-0.51
- Zone : I, A= 451.34m², Cpe,10=-0.33, Cpe,1=-0.33
- Zone : J, A= 59.61m², Cpe,10=-0.34, Cpe,1=-0.56
- Zone : J, A= 59.61m², Cpe,10=-0.33, Cpe,1=-0.33

Wind pressure on roof surfaces $w_e=q(z) \cdot Cpe=0.900 \times Cpe$ [kN/m²]

(EN1991-1-4, 5.1)

F		G		H		I		J	
w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}
-1.209	-2.049	-0.919	-1.599	-0.420	-0.719	-0.460	-0.460	-0.302	-0.503
+0.080	+0.080	+0.080	+0.080	+0.080	+0.080	-0.299	-0.299	-0.299	-0.299

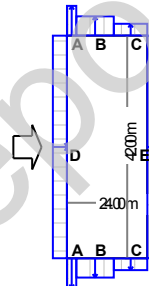
Wind forces on vertical walls

(EN1991-1-4, §7.2.2)

Wind pressure coefficients Cpe

(EN1991-1-4, Tab. 7.1)

- $h/d=5.00/24.00=0.208$, $e=10.00\text{m}$
- Zone : A, (2.00xh), Cpe,10=-1.20, Cpe,1=-1.40
 - Zone : B, (8.00xh), Cpe,10=-0.80, Cpe,1=-1.10
 - Zone : C, (14.00xh), Cpe,10=-0.50, Cpe,1=-0.50
 - Zone : D, (42.00xh), Cpe,10= 0.70, Cpe,1= 1.00
 - Zone : E, (42.00xh), Cpe,10=-0.30, Cpe,1=-0.30



Wind pressure on wall surfaces $w_e=q(z) \cdot Cpe$ [kN/m²]

(EN1991-1-4, 5.1)

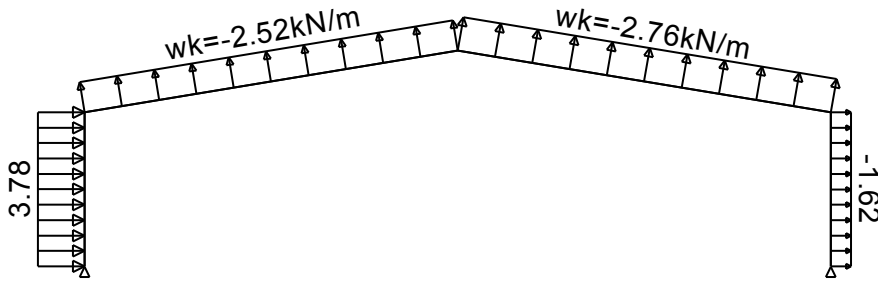
z= 5.00~ 0.00m,	A		B		C		D		E	
	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}	w _{e,10}	w _{e,1}
	-1.080	-1.260	-0.720	-0.990	-0.450	-0.450	0.630	0.900	-0.270	-0.270

4.6. Wind load on frame

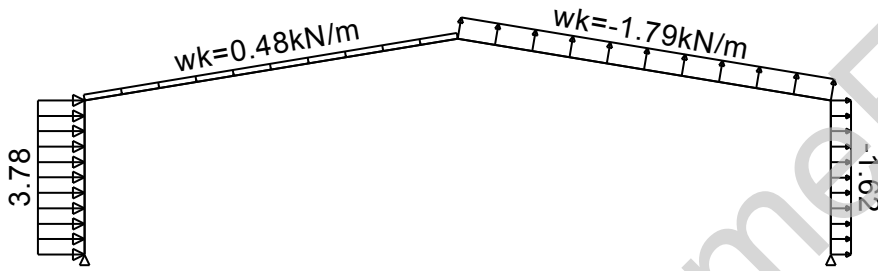
(EC1 EN1991-1-4:2005)

Wind pressure on vertical surface	wk= 0.900 kN/m ²		
Wind internal pressure	wi= 0.000 kN/m ²		
Spacing of frames	s= 6.000 m		
Left column	Wk1= 0.630x6.000= 3.78kN/m,	Wk1= 0.630x6.000= 3.78kN/m	
Left rafter	Wk2=-0.420x6.000= -2.52kN/m,	Wk2= 0.080x6.000= 0.48kN/m	
Right rafter	Wk3=-0.460x6.000= -2.76kN/m,	Wk3=-0.299x6.000= -1.79kN/m	
Right column	Wk4=-0.270x6.000= -1.62kN/m,	Wk4=-0.270x6.000= -1.62kN/m	

Load Qw1 (Wind load)



Load Qw2 (Wind load)



SteelPortalFrameEC3
Example Report

5. Design values of Actions

(EN1990 NA Eurocode EN, §6.4, §6.5)

5.1. Load combination factors

(EN1990 Tab.A1.1)

Category H (roofs)	$Q_k \psi_0=0.00, \psi_1=0.00, \psi_2=0.00$
Snow loads on buildings	$Q_s \psi_0=0.50, \psi_1=0.20, \psi_2=0.00$
Wind loads on buildings	$Q_w \psi_0=0.60, \psi_1=0.20, \psi_2=0.00$

5.2. Ultimate Limit State (ULS) (EQU)

$$E_d = \gamma_G \cdot G_k + \gamma_Q \cdot Q_{k1} + \gamma_Q \cdot \psi_0 \cdot Q_{k2} \quad (\text{Eq. 6.10})$$

$\gamma_{G, \text{sup}}=1.10$ (Unfavourable)

$\gamma_{G, \text{inf}}=0.90$ (Favourable)

$\gamma_Q = 1.50$ (Unfavourable)

$\gamma_Q = 0.00$ (Favourable)

Load combinations (ULS) (EQU),**Permanent load G_k , Imposed load Q_k , Snow load Q_{s1}, Q_{s2}, Q_{s3} , Wind load Q_{w1}, Q_{w2}**

L.C. 101: $1.10G_k+1.50Q_k$	(Eq. 6.10)
L.C. 102: $1.10G_k+1.50Q_{s1}$	(Eq. 6.10)
L.C. 103: $1.10G_k+1.50Q_{s2}$	(Eq. 6.10)
L.C. 104: $1.10G_k+1.50Q_{s3}$	(Eq. 6.10)
L.C. 105: $1.10G_k+1.50Q_{w1}$	(Eq. 6.10)
L.C. 106: $1.10G_k+1.50Q_{w2}$	(Eq. 6.10)
L.C. 111: $0.90G_k+1.50Q_{w1}$	(Eq. 6.10)
L.C. 121: $1.10G_k+1.50Q_{s1}+0.60 \times 1.50Q_{w1} = 1.10xG_k+1.50Q_{s1}+0.90Q_{w1}$	(Eq. 6.10)
L.C. 122: $1.10G_k+1.50Q_{s1}+0.60 \times 1.50Q_{w2} = 1.10xG_k+1.50Q_{s1}+0.90Q_{w2}$	(Eq. 6.10)
L.C. 123: $1.10G_k+1.50Q_{s2}+0.60 \times 1.50Q_{w1} = 1.10xG_k+1.50Q_{s2}+0.90Q_{w1}$	(Eq. 6.10)
L.C. 124: $1.10G_k+1.50Q_{s2}+0.60 \times 1.50Q_{w2} = 1.10xG_k+1.50Q_{s2}+0.90Q_{w2}$	(Eq. 6.10)
L.C. 125: $1.10G_k+1.50Q_{s3}+0.60 \times 1.50Q_{w1} = 1.10xG_k+1.50Q_{s3}+0.90Q_{w1}$	(Eq. 6.10)
L.C. 126: $1.10G_k+1.50Q_{s3}+0.60 \times 1.50Q_{w2} = 1.10xG_k+1.50Q_{s3}+0.90Q_{w2}$	(Eq. 6.10)
L.C. 127: $1.10G_k+1.50Q_{w1}+0.50 \times 1.50Q_{s1} = 1.10xG_k+1.50Q_{w1}+0.75Q_{s1}$	(Eq. 6.10)
L.C. 128: $1.10G_k+1.50Q_{w1}+0.50 \times 1.50Q_{s2} = 1.10xG_k+1.50Q_{w1}+0.75Q_{s2}$	(Eq. 6.10)
L.C. 129: $1.10G_k+1.50Q_{w1}+0.50 \times 1.50Q_{s3} = 1.10xG_k+1.50Q_{w1}+0.75Q_{s3}$	(Eq. 6.10)
L.C. 130: $1.10G_k+1.50Q_{w2}+0.50 \times 1.50Q_{s1} = 1.10xG_k+1.50Q_{w2}+0.75Q_{s1}$	(Eq. 6.10)
L.C. 131: $1.10G_k+1.50Q_{w2}+0.50 \times 1.50Q_{s2} = 1.10xG_k+1.50Q_{w2}+0.75Q_{s2}$	(Eq. 6.10)
L.C. 132: $1.10G_k+1.50Q_{w2}+0.50 \times 1.50Q_{s3} = 1.10xG_k+1.50Q_{w2}+0.75Q_{s3}$	(Eq. 6.10)

5.3. Ultimate Limit State (ULS) (STR)

$$E_d = \gamma_G \cdot G_k + \gamma_Q \cdot Q_{k1} + \gamma_Q \cdot \psi_0 \cdot Q_{k2} \quad (\text{Eq. 6.10})$$

$$E_d = \gamma_G \cdot G_k + \gamma_Q \cdot \psi_0 \cdot Q_{k1} + \gamma_Q \cdot \psi_0 \cdot Q_{k2} \quad (\text{Eq. 6.10a})$$

$$E_d = \xi \cdot \gamma_G \cdot G_k + \gamma_Q \cdot Q_{k1} + \gamma_Q \cdot \psi_0 \cdot Q_{k2} \quad (\text{Eq. 6.10b})$$

$$\gamma_{G, \text{sup}} = 1.35 \quad (\text{Unfavourable})$$

$$\gamma_{G, \text{inf}} = 1.00 \quad (\text{Favourable})$$

$$\gamma_Q = 1.50 \quad (\text{Unfavourable})$$

$$\gamma_Q = 0.00 \quad (\text{Favourable})$$

$$\xi = 0.850, \quad \xi \cdot \gamma_G = 0.850 \times 1.35 = 1.15$$

Load combinations (ULS) (STR),**Permanent load G_k , Imposed load Q_k , Snow load Q_{s1}, Q_{s2}, Q_{s3} , Wind load Q_{w2}**

$$L.C. 201: 1.35G_k + 1.50Q_k \quad (\text{Eq. 6.10})$$

$$L.C. 202: 1.35G_k + 1.50Q_{s1} \quad (\text{Eq. 6.10})$$

$$L.C. 203: 1.35G_k + 1.50Q_{s2} \quad (\text{Eq. 6.10})$$

$$L.C. 204: 1.35G_k + 1.50Q_{s3} \quad (\text{Eq. 6.10})$$

$$L.C. 205: 1.35G_k + 1.50Q_{w1} \quad (\text{Eq. 6.10})$$

$$L.C. 206: 1.35G_k + 1.50Q_{w2} \quad (\text{Eq. 6.10})$$

$$L.C. 210: 1.00G_k + 1.50Q_{w1} \quad (\text{Eq. 6.10})$$

$$L.C. 211: 1.35G_k + 1.50Q_{s1} + 0.60 \times 1.50Q_{w1} = 1.35xG_k + 1.50Q_{s1} + 0.90Q_{w1} \quad (\text{Eq. 6.10})$$

$$L.C. 212: 1.35G_k + 1.50Q_{s1} + 0.60 \times 1.50Q_{w2} = 1.35xG_k + 1.50Q_{s1} + 0.90Q_{w2} \quad (\text{Eq. 6.10})$$

$$L.C. 213: 1.35G_k + 1.50Q_{s2} + 0.60 \times 1.50Q_{w1} = 1.35xG_k + 1.50Q_{s2} + 0.90Q_{w1} \quad (\text{Eq. 6.10})$$

$$L.C. 214: 1.35G_k + 1.50Q_{s2} + 0.60 \times 1.50Q_{w2} = 1.35xG_k + 1.50Q_{s2} + 0.90Q_{w2} \quad (\text{Eq. 6.10})$$

$$L.C. 215: 1.35G_k + 1.50Q_{s3} + 0.60 \times 1.50Q_{w1} = 1.35xG_k + 1.50Q_{s3} + 0.90Q_{w1} \quad (\text{Eq. 6.10})$$

$$L.C. 216: 1.35G_k + 1.50Q_{s3} + 0.60 \times 1.50Q_{w2} = 1.35xG_k + 1.50Q_{s3} + 0.90Q_{w2} \quad (\text{Eq. 6.10})$$

$$L.C. 217: 1.35G_k + 1.50Q_{w1} + 0.50 \times 1.50Q_{s1} = 1.35xG_k + 1.50Q_{w1} + 0.75Q_{s1} \quad (\text{Eq. 6.10})$$

$$L.C. 218: 1.35G_k + 1.50Q_{w1} + 0.50 \times 1.50Q_{s2} = 1.35xG_k + 1.50Q_{w1} + 0.75Q_{s2} \quad (\text{Eq. 6.10})$$

$$L.C. 219: 1.35G_k + 1.50Q_{w1} + 0.50 \times 1.50Q_{s3} = 1.35xG_k + 1.50Q_{w1} + 0.75Q_{s3} \quad (\text{Eq. 6.10})$$

$$L.C. 220: 1.35G_k + 1.50Q_{w2} + 0.50 \times 1.50Q_{s1} = 1.35xG_k + 1.50Q_{w2} + 0.75Q_{s1} \quad (\text{Eq. 6.10})$$

$$L.C. 221: 1.35G_k + 1.50Q_{w2} + 0.50 \times 1.50Q_{s2} = 1.35xG_k + 1.50Q_{w2} + 0.75Q_{s2} \quad (\text{Eq. 6.10})$$

$$L.C. 222: 1.35G_k + 1.50Q_{w2} + 0.50 \times 1.50Q_{s3} = 1.35xG_k + 1.50Q_{w2} + 0.75Q_{s3} \quad (\text{Eq. 6.10})$$

$$L.C. 231: 1.35G_k + 1.50 \times 0.50Q_{s1} + 1.50 \times 0.60Q_{w1} = 1.35xG + 0.75Q_{s1} + 0.90Q_{w1} \quad (\text{Eq. 6.10a})$$

$$L.C. 232: 1.35G_k + 1.50 \times 0.50Q_{s1} + 1.50 \times 0.60Q_{w2} = 1.35xG + 0.75Q_{s1} + 0.90Q_{w2} \quad (\text{Eq. 6.10a})$$

$$L.C. 233: 1.35G_k + 1.50 \times 0.50Q_{s2} + 1.50 \times 0.60Q_{w1} = 1.35xG + 0.75Q_{s2} + 0.90Q_{w1} \quad (\text{Eq. 6.10a})$$

$$L.C. 234: 1.35G_k + 1.50 \times 0.50Q_{s2} + 1.50 \times 0.60Q_{w2} = 1.35xG + 0.75Q_{s2} + 0.90Q_{w2} \quad (\text{Eq. 6.10a})$$

$$L.C. 235: 1.35G_k + 1.50 \times 0.50Q_{s3} + 1.50 \times 0.60Q_{w1} = 1.35xG + 0.75Q_{s3} + 0.90Q_{w1} \quad (\text{Eq. 6.10a})$$

$$L.C. 236: 1.35G_k + 1.50 \times 0.50Q_{s3} + 1.50 \times 0.60Q_{w2} = 1.35xG + 0.75Q_{s3} + 0.90Q_{w2} \quad (\text{Eq. 6.10a})$$

$$L.C. 251: 0.850 \times 1.35G_k + 1.50Q_{s1} + 1.50 \times 0.60Q_{w1} = 1.15xG + 1.50Q_{s1} + 0.90Q_{w1} \quad (\text{Eq. 6.10b})$$

$$L.C. 252: 0.850 \times 1.35G_k + 1.50Q_{s1} + 1.50 \times 0.60Q_{w2} = 1.15xG + 1.50Q_{s1} + 0.90Q_{w2} \quad (\text{Eq. 6.10b})$$

$$L.C. 253: 0.850 \times 1.35G_k + 1.50Q_{s2} + 1.50 \times 0.60Q_{w1} = 1.15xG + 1.50Q_{s2} + 0.90Q_{w1} \quad (\text{Eq. 6.10b})$$

$$L.C. 254: 0.850 \times 1.35G_k + 1.50Q_{s2} + 1.50 \times 0.60Q_{w2} = 1.15xG + 1.50Q_{s2} + 0.90Q_{w2} \quad (\text{Eq. 6.10b})$$

$$L.C. 255: 0.850 \times 1.35G_k + 1.50Q_{s3} + 1.50 \times 0.60Q_{w1} = 1.15xG + 1.50Q_{s3} + 0.90Q_{w1} \quad (\text{Eq. 6.10b})$$

$$L.C. 256: 0.850 \times 1.35G_k + 1.50Q_{s3} + 1.50 \times 0.60Q_{w2} = 1.15xG + 1.50Q_{s3} + 0.90Q_{w2} \quad (\text{Eq. 6.10b})$$

$$L.C. 257: 0.850 \times 1.35G_k + 1.50Q_{w1} + 1.50 \times 0.50Q_{s1} = 1.15xG + 1.50Q_{w1} + 0.75Q_{s1} \quad (\text{Eq. 6.10b})$$

$$L.C. 258: 0.850 \times 1.35G_k + 1.50Q_{w1} + 1.50 \times 0.50Q_{s2} = 1.15xG + 1.50Q_{w1} + 0.75Q_{s2} \quad (\text{Eq. 6.10b})$$

$$L.C. 259: 0.850 \times 1.35G_k + 1.50Q_{w1} + 1.50 \times 0.50Q_{s3} = 1.15xG + 1.50Q_{w1} + 0.75Q_{s3} \quad (\text{Eq. 6.10b})$$

$$L.C. 260: 0.850 \times 1.35G_k + 1.50Q_{w2} + 1.50 \times 0.50Q_{s1} = 1.15xG + 1.50Q_{w2} + 0.75Q_{s1} \quad (\text{Eq. 6.10b})$$

$$L.C. 261: 0.850 \times 1.35G_k + 1.50Q_{w2} + 1.50 \times 0.50Q_{s2} = 1.15xG + 1.50Q_{w2} + 0.75Q_{s2} \quad (\text{Eq. 6.10b})$$

$$L.C. 262: 0.850 \times 1.35G_k + 1.50Q_{w2} + 1.50 \times 0.50Q_{s3} = 1.15xG + 1.50Q_{w2} + 0.75Q_{s3} \quad (\text{Eq. 6.10b})$$

5.4. Serviceability Limit State (SLS)

$$E_d = G_k + Q_{k1} + \psi_0 \cdot Q_{k2} + \psi_0 \cdot Q_{k3} \quad (\text{Characteristic combination}) \quad (\text{Eq. 6.14b})$$

$$E_d = G_k + \psi_1 \cdot Q_{k1} + \psi_2 \cdot Q_{k2} + \psi_2 \cdot Q_{k3} \quad (\text{Frequent combination}) \quad (\text{Eq. 6.15b})$$

$$E_d = G_k + \psi_2 \cdot Q_{k1} + \psi_2 \cdot Q_{k2} + \psi_2 \cdot Q_{k3} \quad (\text{Quasi-permanent combination}) \quad (\text{Eq. 6.16b})$$

Load combinations (SLS)

Permanent load G_k , Imposed load Q_k , Snow load Q_{s1}, Q_{s2}, Q_{s3} , Wind load Q_{w1}, Q_{w2}

$$L.C. 301: G_k + Q_k \quad (\text{Eq. 6.14a})$$

$$L.C. 302: G_k + Q_{s1} \quad (\text{Eq. 6.14a})$$

$$L.C. 303: G_k + Q_{s2} \quad (\text{Eq. 6.14a})$$

$$L.C. 304: G_k + Q_{s3} \quad (\text{Eq. 6.14a})$$

$$L.C. 305: G_k + Q_{w1} \quad (\text{Eq. 6.14a})$$

$$L.C. 306: G_k + Q_{w2} \quad (\text{Eq. 6.14a})$$

$$L.C. 311: G + Q_{s1} + 0.60Q_{w1} \quad (\text{Eq. 6.14a})$$

$$L.C. 312: G + Q_{s1} + 0.60Q_{w2} \quad (\text{Eq. 6.14a})$$

$$L.C. 313: G + Q_{s2} + 0.60Q_{w1} \quad (\text{Eq. 6.14a})$$

$$L.C. 314: G + Q_{s2} + 0.60Q_{w2} \quad (\text{Eq. 6.14a})$$

$$L.C. 315: G + Q_{s3} + 0.60Q_{w1} \quad (\text{Eq. 6.14a})$$

$$L.C. 316: G + Q_{s3} + 0.60Q_{w2} \quad (\text{Eq. 6.14a})$$

$$L.C. 317: G + Q_{w1} + 0.50Q_{s1} \quad (\text{Eq. 6.14a})$$

$$L.C. 318: G + Q_{w1} + 0.50Q_{s2} \quad (\text{Eq. 6.14a})$$

$$L.C. 319: G + Q_{w1} + 0.50Q_{s3} \quad (\text{Eq. 6.14a})$$

$$L.C. 320: G + Q_{w2} + 0.50Q_{s1} \quad (\text{Eq. 6.14a})$$

$$L.C. 321: G + Q_{w2} + 0.50Q_{s2} \quad (\text{Eq. 6.14a})$$

$$L.C. 322: G + Q_{w2} + 0.50Q_{s3} \quad (\text{Eq. 6.14a})$$

$$L.C. 331: G + 0.50Q_{s1} + 0.30Q_{w1} \quad (\text{Eq. 6.15a})$$

$$L.C. 332: G + 0.50Q_{s1} + 0.30Q_{w2} \quad (\text{Eq. 6.15a})$$

$$L.C. 333: G + 0.50Q_{s2} + 0.30Q_{w1} \quad (\text{Eq. 6.15a})$$

$$L.C. 334: G + 0.50Q_{s2} + 0.30Q_{w2} \quad (\text{Eq. 6.15a})$$

$$L.C. 335: G + 0.50Q_{s3} + 0.30Q_{w1} \quad (\text{Eq. 6.15a})$$

$$L.C. 336: G + 0.50Q_{s3} + 0.30Q_{w2} \quad (\text{Eq. 6.15a})$$

$$L.C. 337: G + 0.20Q_{w1} + 0.00Q_{s1} \quad (\text{Eq. 6.15a})$$

$$L.C. 338: G + 0.20Q_{w1} + 0.00Q_{s2} \quad (\text{Eq. 6.15a})$$

$$L.C. 339: G + 0.20Q_{w1} + 0.00Q_{s3} \quad (\text{Eq. 6.15a})$$

$$L.C. 340: G + 0.20Q_{w2} + 0.00Q_{s1} \quad (\text{Eq. 6.15a})$$

$$L.C. 341: G + 0.20Q_{w2} + 0.00Q_{s2} \quad (\text{Eq. 6.15a})$$

$$L.C. 342: G + 0.20Q_{w2} + 0.00Q_{s3} \quad (\text{Eq. 6.15a})$$

$$L.C. 351: G + 0.00Q_{s1} + 0.30Q_{w1} \quad (\text{Eq. 6.16a})$$

$$L.C. 352: G + 0.00Q_{s1} + 0.30Q_{w2} \quad (\text{Eq. 6.16a})$$

$$L.C. 353: G + 0.00Q_{s2} + 0.30Q_{w1} \quad (\text{Eq. 6.16a})$$

$$L.C. 354: G + 0.00Q_{s2} + 0.30Q_{w2} \quad (\text{Eq. 6.16a})$$

$$L.C. 355: G + 0.00Q_{s3} + 0.30Q_{w1} \quad (\text{Eq. 6.16a})$$

$$L.C. 356: G + 0.00Q_{s3} + 0.30Q_{w2} \quad (\text{Eq. 6.16a})$$

5.5. Ultimate Limit State (ULS) Seismic situation

$$E_d = G_k + A_{ed} + \psi_2 \cdot Q_{k1} + \psi_2 \cdot Q_{k2} + \psi_2 \cdot Q_{k3} \quad (\text{Eq. 6.12b})$$

Snow load Q_s , Wind load Q_w , Seismic load A_{ed}

$$L.C. 601: G_k + 0.20Q_{s1} + A_{ed} \quad (\text{Eq. 6.14a})$$

5.6. Summary of load combination

Permanent load Q_k, Imposed load Q_k, Snow load Q_{s1}, Q_{s2}, Q_{s3}, Wind load ,Q_{w2}

1	L.C. 101	(ULS) (EQU)	1.10Gk+1.50Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
2	L.C. 102	(ULS) (EQU)	1.10Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
3	L.C. 103	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.00Qw1+0.00Qw2
4	L.C. 104	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.00Qw1+0.00Qw2
5	L.C. 105	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
6	L.C. 106	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.50Qw2
7	L.C. 111	(ULS) (EQU)	0.90Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
8	L.C. 121	(ULS) (EQU)	1.10Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.90Qw1+0.00Qw2
9	L.C. 122	(ULS) (EQU)	1.10Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.90Qw2
10	L.C. 123	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.90Qw1+0.00Qw2
11	L.C. 124	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.00Qw1+0.90Qw2
12	L.C. 125	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.90Qw1+0.00Qw2
13	L.C. 126	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.00Qw1+0.90Qw2
14	L.C. 127	(ULS) (EQU)	1.10Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
15	L.C. 128	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+1.50Qw1+0.00Qw2
16	L.C. 129	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+1.50Qw1+0.00Qw2
17	L.C. 130	(ULS) (EQU)	1.10Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.50Qw2
18	L.C. 131	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+0.00Qw1+1.50Qw2
19	L.C. 132	(ULS) (EQU)	1.10Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+0.00Qw1+1.50Qw2
20	L.C. 201	(ULS) (STR)	1.35Gk+1.50Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
21	L.C. 202	(ULS) (STR)	1.35Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
22	L.C. 203	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.00Qw1+0.00Qw2
23	L.C. 204	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.00Qw1+0.00Qw2
24	L.C. 205	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
25	L.C. 206	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.50Qw2
26	L.C. 210	(ULS) (STR)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
27	L.C. 211	(ULS) (STR)	1.35Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.90Qw1+0.00Qw2
28	L.C. 212	(ULS) (STR)	1.35Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.90Qw2
29	L.C. 213	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.90Qw1+0.00Qw2
30	L.C. 214	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.00Qw1+0.90Qw2
31	L.C. 215	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.90Qw1+0.00Qw2
32	L.C. 216	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.00Qw1+0.90Qw2
33	L.C. 217	(ULS) (STR)	1.35Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
34	L.C. 218	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+1.50Qw1+0.00Qw2
35	L.C. 219	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+1.50Qw1+0.00Qw2
36	L.C. 220	(ULS) (STR)	1.35Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.50Qw2
37	L.C. 221	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+0.00Qw1+1.50Qw2
38	L.C. 222	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+0.00Qw1+1.50Qw2
39	L.C. 231	(ULS) (STR)	1.35Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+0.90Qw1+0.00Qw2
40	L.C. 232	(ULS) (STR)	1.35Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.90Qw2
41	L.C. 233	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+0.90Qw1+0.00Qw2
42	L.C. 234	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+0.00Qw1+0.90Qw2
43	L.C. 235	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+0.90Qw1+0.00Qw2
44	L.C. 236	(ULS) (STR)	1.35Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+0.00Qw1+0.90Qw2
45	L.C. 251	(ULS) (STR)	1.15Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.90Qw1+0.00Qw2
46	L.C. 252	(ULS) (STR)	1.15Gk+0.00Qk+1.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.90Qw2
47	L.C. 253	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.90Qw1+0.00Qw2
48	L.C. 254	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+1.50Qs2+0.00Qs3+0.00Qw1+0.90Qw2
49	L.C. 255	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.90Qw1+0.00Qw2
50	L.C. 256	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.00Qs2+1.50Qs3+0.00Qw1+0.90Qw2
51	L.C. 257	(ULS) (STR)	1.15Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+1.50Qw1+0.00Qw2
52	L.C. 258	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+1.50Qw1+0.00Qw2
53	L.C. 259	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+1.50Qw1+0.00Qw2
54	L.C. 260	(ULS) (STR)	1.15Gk+0.00Qk+0.75Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.50Qw2
55	L.C. 261	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.75Qs2+0.00Qs3+0.00Qw1+1.50Qw2
56	L.C. 262	(ULS) (STR)	1.15Gk+0.00Qk+0.00Qs1+0.00Qs2+0.75Qs3+0.00Qw1+1.50Qw2
57	L.C. 301	(SLS)	1.00Gk+1.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
58	L.C. 302	(SLS)	1.00Gk+0.00Qk+1.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
59	L.C. 303	(SLS)	1.00Gk+0.00Qk+0.00Qs1+1.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
60	L.C. 304	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+1.00Qs3+0.00Qw1+0.00Qw2
61	L.C. 305	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+1.00Qw1+0.00Qw2
62	L.C. 306	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.00Qw2
63	L.C. 311	(SLS)	1.00Gk+0.00Qk+1.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2
64	L.C. 312	(SLS)	1.00Gk+0.00Qk+1.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.60Qw2
65	L.C. 313	(SLS)	1.00Gk+0.00Qk+0.00Qs1+1.00Qs2+0.00Qs3+0.60Qw1+0.00Qw2
66	L.C. 314	(SLS)	1.00Gk+0.00Qk+0.00Qs1+1.00Qs2+0.00Qs3+0.00Qw1+0.60Qw2
67	L.C. 315	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+1.00Qs3+0.60Qw1+0.00Qw2
68	L.C. 316	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+1.00Qs3+0.00Qw1+0.60Qw2
69	L.C. 317	(SLS)	1.00Gk+0.00Qk+0.50Qs1+0.00Qs2+0.00Qs3+1.00Qw1+0.00Qw2
70	L.C. 318	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.50Qs2+0.00Qs3+1.00Qw1+0.00Qw2
71	L.C. 319	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.50Qs3+1.00Qw1+0.00Qw2
72	L.C. 320	(SLS)	1.00Gk+0.00Qk+0.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+1.00Qw2
73	L.C. 321	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.50Qs2+0.00Qs3+0.00Qw1+1.00Qw2
74	L.C. 322	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.50Qs3+0.00Qw1+1.00Qw2
75	L.C. 331	(SLS)	1.00Gk+0.00Qk+0.50Qs1+0.00Qs2+0.00Qs3+0.30Qw1+0.00Qw2
76	L.C. 332	(SLS)	1.00Gk+0.00Qk+0.50Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.30Qw2
77	L.C. 333	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.50Qs2+0.00Qs3+0.30Qw1+0.00Qw2
78	L.C. 334	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.50Qs2+0.00Qs3+0.00Qw1+0.30Qw2
79	L.C. 335	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.50Qs3+0.30Qw1+0.00Qw2
80	L.C. 336	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.50Qs3+0.00Qw1+0.30Qw2
81	L.C. 337	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.20Qw1+0.00Qw2
82	L.C. 338	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.20Qw1+0.00Qw2
83	L.C. 339	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.20Qw1+0.00Qw2
84	L.C. 340	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.20Qw2
85	L.C. 341	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.20Qw2
86	L.C. 342	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.20Qw2
87	L.C. 351	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.30Qw1+0.00Qw2
88	L.C. 352	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.30Qw2
89	L.C. 353	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.30Qw1+0.00Qw2
90	L.C. 354	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.30Qw2
91	L.C. 355	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.30Qw1+0.00Qw2
92	L.C. 356	(SLS)	1.00Gk+0.00Qk+0.00Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.30Qw2
93	L.C. 601	(SESM)	1.00Gk+0.00Qk+0.20Qs1+0.00Qs2+0.00Qs3+0.00Qw1+0.00Qw2 + Aed

6. Steel sections

6.1. Column section

Cross-section properties

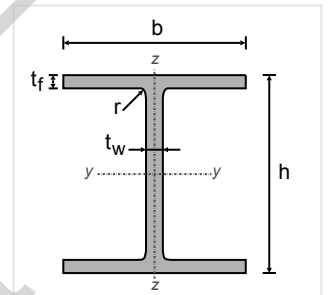
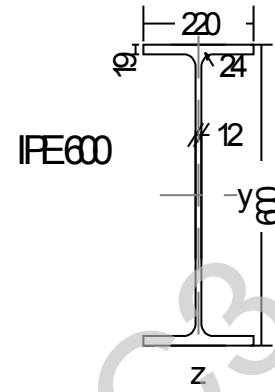
Cross-section IPE 600-S 355

Dimensions of cross section

Depth of cross section	h=	600.00 mm
Width of cross section	b=	220.00 mm
Web depth	hw=	581.00 mm
Depth of straight portion of web	dw=	514.00 mm
Web thickness	tw=	12.00 mm
Flange thickness	tf=	19.00 mm
Radius of root fillet	r=	24.00 mm
Mass	=	122.00 Kg/m

Properties of cross section

Area	A=	15600 mm ²	
Second moment of area	I _y =	920.80x10 ⁶ mm ⁴	I _z =33.870x10 ⁶ mm ⁴
Section modulus	W _y =	3069.0x10 ³ mm ³	W _z =307.90x10 ³ mm ³
Plastic section modulus	W _{py} =	3512.0x10 ³ mm ³	W _{pz} =485.60x10 ³ mm ³
Radius of gyration	i _y =	243.0 mm	i _z = 46.6 mm
Shear area	Av _z =	8380 mm ²	Av _y = 8360 mm ²
Torsional constant	I _t =	1.654x10 ⁶ mm ⁴	i _p = 247 mm
Warping constant	I _w =	2845.5x10 ⁹ mm ⁶	



6.2. Rafter section

Cross-section properties

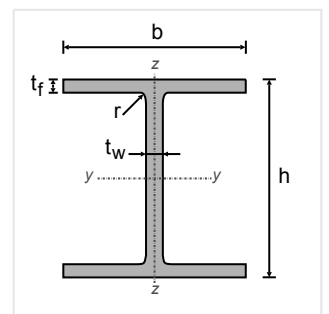
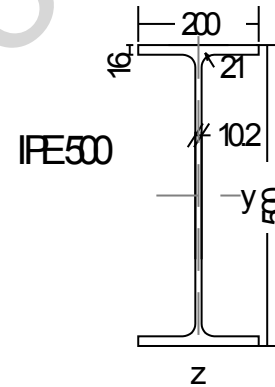
Cross-section IPE 500-S 355

Dimensions of cross section

Depth of cross section	h=	500.00 mm
Width of cross section	b=	200.00 mm
Web depth	hw=	484.00 mm
Depth of straight portion of web	dw=	426.00 mm
Web thickness	tw=	10.20 mm
Flange thickness	tf=	16.00 mm
Radius of root fillet	r=	21.00 mm
Mass	=	90.70 Kg/m

Properties of cross section

Area	A=	11550 mm ²	
Second moment of area	I _y =	482.00x10 ⁶ mm ⁴	I _z =21.420x10 ⁶ mm ⁴
Section modulus	W _y =	1928.0x10 ³ mm ³	W _z =214.20x10 ³ mm ³
Plastic section modulus	W _{py} =	2194.0x10 ³ mm ³	W _{pz} =335.90x10 ³ mm ³
Radius of gyration	i _y =	204.3 mm	i _z = 43.1 mm
Shear area	Av _z =	5985 mm ²	Av _y = 6400 mm ²
Torsional constant	I _t =	0.893x10 ⁶ mm ⁴	i _p = 209 mm
Warping constant	I _w =	1249.4x10 ⁹ mm ⁶	



6.3. Haunch section at haunch end

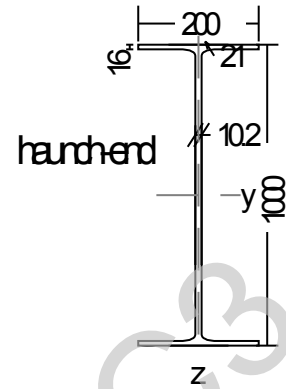
Cross-section properties

Welded section

Cross-section haunch-end-S 355

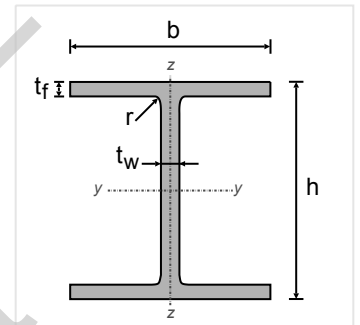
Dimensions of cross section

Depth of cross section	h=	1000.00 mm
Width of cross section	b=	200.00 mm
Web depth	hw=	984.00 mm
Depth of straight portion of web	dw=	908.60 mm
Web thickness	tw=	10.20 mm
Flange thickness	tf=	16.00 mm
Radius of root fillet	r=	21.00 mm
Mass	=	127.83 Kg/m



Properties of cross section

Area	A=	16274 mm ²	
Second moment of area	Iy=	2320.3x10 ⁶ mm ⁴	Iz=21.419x10 ⁶ mm ⁴
Section modulus	Wy=	4640.7x10 ³ mm ³	Wz=214.19x10 ³ mm ³
Plastic section modulus	Wpy=	5538.2x10 ³ mm ³	Wpz=345.18x10 ³ mm ³
Radius of gyration	iy=	377.6 mm	iz= 36.3 mm
Shear area	Avz=	10037 mm ²	Avy= 6400 mm ²
Torsional constant	It=	0.879x10 ⁶ mm ⁴	ip= 379 mm
Warping constant	Iw=	5164.0x10 ⁹ mm ⁶	
Weld	a=	21.0x10 ⁹ mm	



6.4. Haunch section at haunch-middle

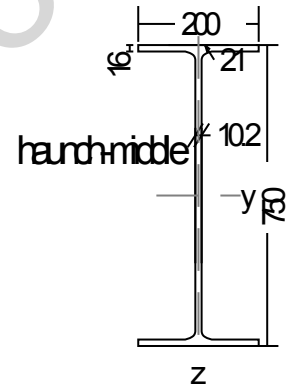
Cross-section properties

Welded section

Cross-section haunch-middle-S 355

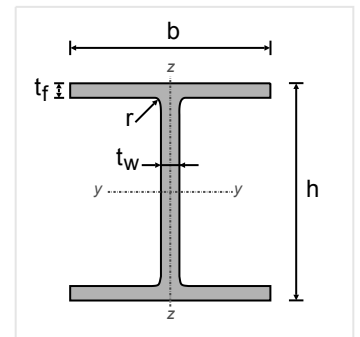
Dimensions of cross section

Depth of cross section	h=	750.00 mm
Width of cross section	b=	200.00 mm
Web depth	hw=	734.00 mm
Depth of straight portion of web	dw=	658.60 mm
Web thickness	tw=	10.20 mm
Flange thickness	tf=	16.00 mm
Radius of root fillet	r=	21.00 mm
Mass	=	107.80 Kg/m



Properties of cross section

Area	A=	13724 mm ²	
Second moment of area	Iy=	1176.8x10 ⁶ mm ⁴	Iz=21.397x10 ⁶ mm ⁴
Section modulus	Wy=	3138.1x10 ³ mm ³	Wz=213.97x10 ³ mm ³
Plastic section modulus	Wpy=	3663.4x10 ³ mm ³	Wpz=338.68x10 ³ mm ³
Radius of gyration	iy=	292.8 mm	iz= 39.5 mm
Shear area	Avz=	7487 mm ²	Avy= 6400 mm ²
Torsional constant	It=	0.790x10 ⁶ mm ⁴	ip= 295 mm
Warping constant	Iw=	2873.4x10 ⁹ mm ⁶	
Weld	a=	21.0x10 ⁹ mm	



7. Finite Element Analysis

(EN1993-1-1, §5.1)

The 2-dimensional finite element program FRAME2Dexpres© RUNET is used for the analysis.
 The column bases are assumed to be pinned.
 The connection of rafter to column are assumed to be fully rigid.
 The increased stiffness of the haunches is taken into account.
 The global or local imperfections are taken into account by equivalent loads.

Linear-elastic analysis is used for the design of static loads.

7.1. Data used for elastic analysis

Nodal points

Node	x [mm]	y [mm]
1	0	0
2	0	5000
3	12000	7000
4	24000	5000
5	24000	0

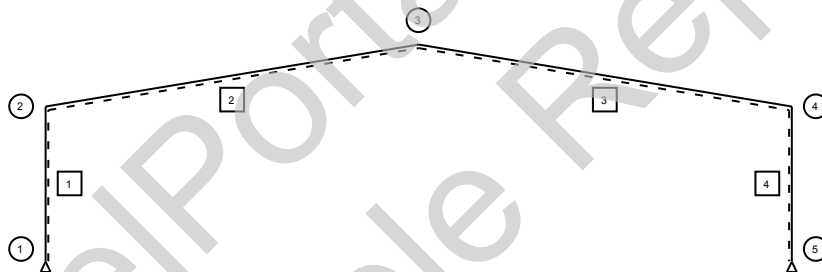
Supports

Node	kind	ux [mm]	uy [mm]	ur [rad]
1	pin	ux=uy=0		
5	pin	ux=uy=0		

Elements

Element	node 1	node 2	length (mm)	angle (°)	E (GPa)	A (mm ²)	I (mm ⁴)
1	1	2	5000	90.00	210	15600	920800x10 ³
2	2	3	12166	9.46	210	11550	482000x10 ³
3	3	4	12166	350.54	210	11550	482000x10 ³
4	4	5	5000	270.00	210	15600	920800x10 ³

Finite element model (FEM) Linear elastic analysis



8. Results of static-linear-elastic analysis

8.1. Displacements [mm]

L.C.	Horiz. defl. Column Dx mm	Vert. defl. Apex Dy mm	Bending Defl. of Rafter w mm
101 ULS-EQU	6.896	43.241	3.469
102 ULS-EQU	9.370	58.758	4.714
103 ULS-EQU	11.321	48.643	4.714
104 ULS-EQU	11.321	48.643	4.714
105 ULS-EQU	6.204	11.521	0.864
106 ULS-EQU	6.765	9.337	1.875
111 ULS-EQU	6.734	14.848	1.131
121 ULS-EQU	9.043	40.867	3.437
122 ULS-EQU	11.679	53.382	4.958
123 ULS-EQU	10.995	30.752	3.437
124 ULS-EQU	13.630	43.267	4.958
125 ULS-EQU	5.849	30.752	3.315
126 ULS-EQU	7.224	43.267	3.804
127 ULS-EQU	5.599	8.709	0.963
128 ULS-EQU	6.575	3.652	0.963
129 ULS-EQU	3.010	3.652	0.759
130 ULS-EQU	9.991	29.568	3.498
131 ULS-EQU	10.967	24.510	3.498
132 ULS-EQU	7.402	24.510	2.686
201 ULS-STR	7.559	47.400	3.802
202 ULS-STR	10.033	62.917	5.047
203 ULS-STR	11.984	52.802	5.047
204 ULS-STR	11.984	52.802	5.047
205 ULS-STR	5.541	7.363	0.530
206 ULS-STR	7.428	13.496	2.208
210 ULS-STR	6.469	13.185	0.997
211 ULS-STR	9.707	45.026	3.770
212 ULS-STR	12.342	57.541	5.291
213 ULS-STR	11.658	34.911	3.770
214 ULS-STR	14.293	47.425	5.291
215 ULS-STR	6.512	34.911	3.648
216 ULS-STR	7.887	47.425	4.137
217 ULS-STR	6.262	12.868	1.296
218 ULS-STR	7.238	7.810	1.296
219 ULS-STR	3.673	7.810	1.093
220 ULS-STR	10.654	33.726	3.831
221 ULS-STR	11.630	28.668	3.831
222 ULS-STR	8.066	28.668	3.020
231 ULS-STR	6.480	24.795	2.147
232 ULS-STR	9.115	37.310	3.668
233 ULS-STR	7.456	19.738	2.147
234 ULS-STR	10.091	32.253	3.668
235 ULS-STR	3.891	19.738	2.025
236 ULS-STR	6.527	32.253	2.857
251 ULS-STR	9.176	41.699	3.504
252 ULS-STR	11.811	54.214	5.025
253 ULS-STR	11.127	31.584	3.504
254 ULS-STR	13.762	44.099	5.025
255 ULS-STR	5.981	31.584	3.381
256 ULS-STR	7.356	44.099	3.870
257 ULS-STR	5.732	9.541	1.029
258 ULS-STR	6.707	4.483	1.029
259 ULS-STR	3.143	4.483	0.826
260 ULS-STR	10.124	30.399	3.565
261 ULS-STR	11.099	25.342	3.565
262 ULS-STR	7.535	25.342	2.753
301 SLS	5.304	33.263	2.668
302 SLS	6.954	43.608	3.498
303 SLS	8.255	36.865	3.498
304 SLS	8.255	36.864	3.498
305 SLS	3.429	3.245	0.220
306 SLS	5.217	10.660	1.606
311 SLS	6.736	31.681	2.647
312 SLS	8.493	40.024	3.661
313 SLS	8.037	24.937	2.647
314 SLS	9.794	33.280	3.661
315 SLS	4.606	24.937	2.566
316 SLS	5.523	33.280	2.891
317 SLS	4.440	10.242	0.998
318 SLS	5.090	6.870	0.998
319 SLS	2.714	6.870	0.862
320 SLS	7.368	24.147	2.688
321 SLS	8.018	20.776	2.688
322 SLS	5.642	20.776	2.147
331 SLS	4.694	24.157	1.991
332 SLS	5.573	28.329	2.498
333 SLS	5.345	20.786	1.991
334 SLS	6.223	24.957	2.498
335 SLS	3.629	20.786	1.950
336 SLS	4.088	24.957	2.113
337 SLS	2.580	12.658	1.050
338 SLS	2.580	12.658	1.050
339 SLS	2.580	12.658	1.050
340 SLS	3.165	15.439	1.388
341 SLS	3.165	15.439	1.388
342 SLS	3.165	15.439	1.388
351 SLS	2.543	10.670	0.909
352 SLS	3.422	14.842	1.416
353 SLS	2.543	10.670	0.909
354 SLS	3.422	14.842	1.416
355 SLS	2.543	10.670	0.909
356 SLS	3.422	14.842	1.416

8.2. Reactions at the supports

		Horizontal Force Hed [kN],			Vertical Force Ved [kN],			Moment Med [kNm]
L.C.		Left support 1			Right support 2			
		Hed,1 kN	Ved,1 kN	Med,1 kNm	Hed,2 kN	Ved,2 kN	Med,2 kNm	
101	ULS-EQU	51.7	82.5	0.0	-51.7	82.5	0.0	
102	ULS-EQU	70.3	109.8	0.0	-70.3	109.8	0.0	
103	ULS-EQU	58.2	100.9	0.0	-58.2	83.1	0.0	
104	ULS-EQU	58.2	83.1	0.0	-58.2	100.9	0.0	
105	ULS-EQU	-31.0	-9.2	0.0	3.3	-8.3	0.0	
106	ULS-EQU	-2.9	37.2	0.0	-18.6	16.6	0.0	
111	ULS-EQU	-35.0	-16.2	0.0	7.3	-15.4	0.0	
121	ULS-EQU	38.6	81.0	0.0	-55.2	81.5	0.0	
122	ULS-EQU	55.4	108.8	0.0	-68.3	96.5	0.0	
123	ULS-EQU	26.5	72.1	0.0	-43.1	54.9	0.0	
124	ULS-EQU	43.3	99.9	0.0	-56.2	69.9	0.0	
125	ULS-EQU	26.5	54.4	0.0	-43.1	72.6	0.0	
126	ULS-EQU	43.3	82.2	0.0	-56.2	87.6	0.0	
127	ULS-EQU	-6.8	26.3	0.0	-20.9	27.2	0.0	
128	ULS-EQU	-12.8	21.9	0.0	-14.8	13.9	0.0	
129	ULS-EQU	-12.8	13.0	0.0	-14.8	22.7	0.0	
130	ULS-EQU	21.3	72.7	0.0	-42.8	52.2	0.0	
131	ULS-EQU	15.2	68.2	0.0	-36.7	38.8	0.0	
132	ULS-EQU	15.2	59.4	0.0	-36.7	47.7	0.0	
201	ULS-STR	56.7	91.3	0.0	-56.7	91.3	0.0	
202	ULS-STR	75.3	118.6	0.0	-75.3	118.6	0.0	
203	ULS-STR	63.2	109.7	0.0	-63.2	91.9	0.0	
204	ULS-STR	63.2	91.9	0.0	-63.2	109.7	0.0	
205	ULS-STR	-26.0	-0.4	0.0	-1.6	0.5	0.0	
206	ULS-STR	2.0	46.0	0.0	-23.6	25.4	0.0	
210	ULS-STR	-33.0	-12.7	0.0	5.3	-11.9	0.0	
211	ULS-STR	43.6	89.8	0.0	-60.1	90.3	0.0	
212	ULS-STR	60.4	117.6	0.0	-73.3	105.3	0.0	
213	ULS-STR	31.5	80.9	0.0	-48.0	63.7	0.0	
214	ULS-STR	48.3	108.7	0.0	-61.2	78.7	0.0	
215	ULS-STR	31.5	63.2	0.0	-48.0	81.4	0.0	
216	ULS-STR	48.3	91.0	0.0	-61.2	96.4	0.0	
217	ULS-STR	-1.8	35.1	0.0	-25.8	36.0	0.0	
218	ULS-STR	-7.8	30.7	0.0	-19.8	22.7	0.0	
219	ULS-STR	-7.8	21.8	0.0	-19.8	31.5	0.0	
220	ULS-STR	26.2	81.5	0.0	-47.8	61.0	0.0	
221	ULS-STR	20.2	77.0	0.0	-41.7	47.6	0.0	
222	ULS-STR	20.2	68.2	0.0	-41.7	56.5	0.0	
231	ULS-STR	19.4	54.3	0.0	-35.9	54.8	0.0	
232	ULS-STR	36.2	82.1	0.0	-49.1	69.8	0.0	
233	ULS-STR	13.3	49.9	0.0	-29.9	41.5	0.0	
234	ULS-STR	30.1	77.7	0.0	-43.0	56.5	0.0	
235	ULS-STR	13.3	41.0	0.0	-29.9	50.4	0.0	
236	ULS-STR	30.1	68.8	0.0	-43.0	65.4	0.0	
251	ULS-STR	39.6	82.8	0.0	-56.2	83.3	0.0	
252	ULS-STR	56.4	110.6	0.0	-69.3	98.3	0.0	
253	ULS-STR	27.5	73.9	0.0	-44.1	56.6	0.0	
254	ULS-STR	44.3	101.7	0.0	-57.2	71.6	0.0	
255	ULS-STR	27.5	56.1	0.0	-44.1	74.4	0.0	
256	ULS-STR	44.3	83.9	0.0	-57.2	89.4	0.0	
257	ULS-STR	-5.8	28.1	0.0	-21.9	28.9	0.0	
258	ULS-STR	-11.8	23.7	0.0	-15.8	15.6	0.0	
259	ULS-STR	-11.8	14.8	0.0	-15.8	24.5	0.0	
260	ULS-STR	22.3	74.4	0.0	-43.8	53.9	0.0	
261	ULS-STR	16.2	70.0	0.0	-37.7	40.6	0.0	
262	ULS-STR	16.2	61.1	0.0	-37.7	49.5	0.0	
301	SLS	39.8	64.4	0.0	-39.8	64.4	0.0	
302	SLS	52.2	82.6	0.0	-52.2	82.6	0.0	
303	SLS	44.1	76.6	0.0	-44.1	64.8	0.0	
304	SLS	44.1	64.8	0.0	-44.1	76.6	0.0	
305	SLS	-15.3	3.3	0.0	-3.1	3.8	0.0	
306	SLS	3.4	34.2	0.0	-17.7	20.5	0.0	
311	SLS	31.0	63.4	0.0	-42.1	63.7	0.0	
312	SLS	42.2	81.9	0.0	-50.9	73.7	0.0	
313	SLS	23.0	57.5	0.0	-34.0	46.0	0.0	
314	SLS	34.2	76.0	0.0	-42.8	56.0	0.0	
315	SLS	23.0	45.6	0.0	-34.0	57.8	0.0	
316	SLS	34.2	64.2	0.0	-42.8	67.8	0.0	
317	SLS	0.8	26.9	0.0	-19.2	27.5	0.0	
318	SLS	-3.2	24.0	0.0	-15.2	18.6	0.0	
319	SLS	-3.2	18.1	0.0	-15.2	24.5	0.0	
320	SLS	19.5	57.8	0.0	-33.8	44.2	0.0	
321	SLS	15.5	54.9	0.0	-29.8	35.3	0.0	
322	SLS	15.5	49.0	0.0	-29.8	41.2	0.0	
331	SLS	25.5	49.3	0.0	-31.0	49.5	0.0	
332	SLS	31.1	58.6	0.0	-35.4	54.5	0.0	
333	SLS	21.4	46.3	0.0	-27.0	40.6	0.0	
334	SLS	27.0	55.6	0.0	-31.3	45.6	0.0	
335	SLS	21.4	40.4	0.0	-27.0	46.5	0.0	
336	SLS	27.0	49.7	0.0	-31.3	51.5	0.0	
337	SLS	12.9	28.8	0.0	-16.5	28.9	0.0	
338	SLS	12.9	28.8	0.0	-16.5	28.9	0.0	
339	SLS	12.9	28.8	0.0	-16.5	28.9	0.0	
340	SLS	16.6	35.0	0.0	-19.5	32.3	0.0	
341	SLS	16.6	35.0	0.0	-19.5	32.3	0.0	
342	SLS	16.6	35.0	0.0	-19.5	32.3	0.0	
351	SLS	9.3	25.6	0.0	-14.9	25.8	0.0	
352	SLS	14.9	34.9	0.0	-19.2	30.8	0.0	
353	SLS	9.3	25.6	0.0	-14.9	25.8	0.0	
354	SLS	14.9	34.9	0.0	-19.2	30.8	0.0	
355	SLS	9.3	25.6	0.0	-14.9	25.8	0.0	
356	SLS	14.9	34.9	0.0	-19.2	30.8	0.0	

8.3. Axial forces Ned [kN]

L.C.	Left column 1 Ned,1	Left rafter 2 Ned,2	Right rafter 3 Ned,3	Right column 4 Ned,4	
101	ULS-EQU	-79.2	-57.3	-57.3	-79.2
102	ULS-EQU	-106.5	-77.8	-77.8	-106.5
103	ULS-EQU	-97.6	-64.4	-64.4	-79.8
104	ULS-EQU	-79.8	-64.4	-64.4	-97.6
105	ULS-EQU	12.5	0.4	0.2	11.6
106	ULS-EQU	-33.9	-26.0	-22.7	-13.3
111	ULS-EQU	18.9	4.8	4.6	18.1
121	ULS-EQU	-77.7	-63.1	-63.1	-78.2
122	ULS-EQU	-105.5	-78.9	-76.9	-93.2
123	ULS-EQU	-68.8	-49.7	-49.7	-51.6
124	ULS-EQU	-96.6	-65.5	-63.5	-66.6
125	ULS-EQU	-51.1	-49.7	-49.7	-69.3
126	ULS-EQU	-78.9	-65.5	-63.5	-84.3
127	ULS-EQU	-23.0	-26.4	-26.6	-23.9
128	ULS-EQU	-18.6	-19.7	-19.9	-10.6
129	ULS-EQU	-9.7	-19.7	-19.9	-19.4
130	ULS-EQU	-69.4	-52.8	-49.5	-48.9
131	ULS-EQU	-64.9	-46.1	-42.8	-35.5
132	ULS-EQU	-56.1	-46.1	-42.8	-44.4
201	ULS-STR	-87.3	-62.8	-62.8	-87.3
202	ULS-STR	-114.5	-83.3	-83.3	-114.5
203	ULS-STR	-105.6	-69.9	-69.9	-87.9
204	ULS-STR	-87.9	-69.9	-69.9	-105.6
205	ULS-STR	4.4	-5.1	-5.3	3.6
206	ULS-STR	-41.9	-31.5	-28.2	-21.4
210	ULS-STR	15.7	2.6	2.4	14.9
211	ULS-STR	-85.8	-68.6	-68.7	-86.3
212	ULS-STR	-113.6	-84.4	-82.4	-101.3
213	ULS-STR	-76.9	-55.2	-55.3	-59.6
214	ULS-STR	-104.7	-71.0	-69.0	-74.6
215	ULS-STR	-59.1	-55.2	-55.3	-77.4
216	ULS-STR	-86.9	-71.0	-69.0	-92.4
217	ULS-STR	-31.1	-31.9	-32.1	-31.9
218	ULS-STR	-26.6	-25.2	-25.4	-18.6
219	ULS-STR	-17.8	-25.2	-25.4	-27.5
220	ULS-STR	-77.4	-58.3	-55.0	-56.9
221	ULS-STR	-73.0	-51.6	-48.3	-43.6
222	ULS-STR	-64.1	-51.6	-48.3	-52.5
231	ULS-STR	-50.2	-41.8	-41.9	-50.8
232	ULS-STR	-78.1	-57.6	-55.6	-65.7
233	ULS-STR	-45.8	-35.1	-35.2	-37.4
234	ULS-STR	-73.6	-50.9	-48.9	-52.4
235	ULS-STR	-36.9	-35.1	-35.2	-46.3
236	ULS-STR	-64.7	-50.9	-48.9	-61.3
251	ULS-STR	-79.3	-64.2	-64.3	-79.8
252	ULS-STR	-107.1	-80.0	-78.0	-94.8
253	ULS-STR	-70.4	-50.8	-50.9	-53.2
254	ULS-STR	-98.3	-66.6	-64.6	-68.2
255	ULS-STR	-52.7	-50.8	-50.9	-71.0
256	ULS-STR	-80.5	-66.6	-64.6	-85.9
257	ULS-STR	-24.6	-27.5	-27.7	-25.5
258	ULS-STR	-20.2	-20.8	-21.0	-12.2
259	ULS-STR	-11.3	-20.8	-21.0	-21.1
260	ULS-STR	-71.0	-53.9	-50.6	-50.5
261	ULS-STR	-66.6	-47.2	-43.9	-37.2
262	ULS-STR	-57.7	-47.2	-43.9	-46.0
301	SLS	-61.4	-44.1	-44.1	-61.4
302	SLS	-79.6	-57.8	-57.8	-79.6
303	SLS	-73.6	-48.8	-48.8	-61.8
304	SLS	-61.8	-48.8	-48.8	-73.6
305	SLS	-0.3	-5.6	-5.7	-0.8
306	SLS	-31.2	-23.2	-21.0	-17.5
311	SLS	-60.4	-47.9	-48.0	-60.7
312	SLS	-78.9	-58.5	-57.1	-70.7
313	SLS	-54.5	-39.0	-39.0	-43.0
314	SLS	-73.0	-49.5	-48.2	-53.0
315	SLS	-42.6	-39.0	-39.0	-54.8
316	SLS	-61.2	-49.5	-48.2	-64.8
317	SLS	-23.9	-23.5	-23.6	-24.5
318	SLS	-21.0	-19.0	-19.1	-15.6
319	SLS	-15.1	-19.0	-19.1	-21.5
320	SLS	-54.8	-41.1	-38.8	-41.2
321	SLS	-51.9	-36.6	-34.4	-32.3
322	SLS	-46.0	-36.6	-34.4	-38.2
331	SLS	-46.3	-35.0	-35.0	-46.5
332	SLS	-55.6	-40.3	-39.6	-51.5
333	SLS	-43.3	-30.5	-30.5	-37.6
334	SLS	-52.6	-35.8	-35.1	-42.6
335	SLS	-37.4	-30.5	-30.5	-43.5
336	SLS	-46.7	-35.8	-35.1	-48.5
337	SLS	-25.8	-18.7	-18.8	-25.9
338	SLS	-25.8	-18.7	-18.8	-25.9
339	SLS	-25.8	-18.7	-18.8	-25.9
340	SLS	-32.0	-22.3	-21.8	-29.3
341	SLS	-32.0	-22.3	-21.8	-29.3
342	SLS	-32.0	-22.3	-21.8	-29.3
351	SLS	-22.6	-17.1	-17.1	-22.8
352	SLS	-31.9	-22.4	-21.7	-27.8
353	SLS	-22.6	-17.1	-17.1	-22.8
354	SLS	-31.9	-22.4	-21.7	-27.8
355	SLS	-22.6	-17.1	-17.1	-22.8
356	SLS	-31.9	-22.4	-21.7	-27.8

8.4. Shearing forces Ved [kN]

L.C.	Left column 1		Left rafter 2			Right rafter 3			Right column 4		
	VedA,1	VedB,1	VedA,2	VedC,2	VedB,2	VedA,3	VedC,3	VedB,3	VedA,4	VedB,4	
101	ULS-EQU	-51.7	-51.7	66.4	51.6	-8.5	8.5	-51.6	-66.4	51.7	51.7
102	ULS-EQU	-70.3	-70.3	90.2	70.1	-11.6	11.6	-70.1	-90.2	70.3	70.3
103	ULS-EQU	-58.2	-58.2	83.4	63.4	-18.3	0.8	-52.7	-65.9	58.2	58.2
104	ULS-EQU	-58.2	-58.2	65.9	52.7	-0.8	18.3	-63.4	-83.4	58.2	58.2
105	ULS-EQU	31.0	2.6	-16.4	-13.6	-2.1	-3.1	11.9	15.5	-15.5	-3.3
106	ULS-EQU	2.9	-25.4	26.2	18.2	-14.3	-7.0	-3.4	-6.0	6.4	18.6
111	ULS-EQU	35.0	6.6	-21.5	-17.5	-1.5	-3.8	15.8	20.6	-19.5	-7.3
121	ULS-EQU	-38.6	-55.6	63.5	48.9	-10.7	7.5	-49.9	-64.0	47.9	55.2
122	ULS-EQU	-55.4	-72.4	89.1	68.0	-18.0	5.2	-60.7	-76.9	61.0	68.3
123	ULS-EQU	-26.5	-43.5	56.8	42.1	-17.4	-3.2	-32.5	-39.7	35.8	43.1
124	ULS-EQU	-43.3	-60.3	82.3	61.2	-24.7	-5.6	-43.4	-52.6	48.9	56.2
125	ULS-EQU	-26.5	-43.5	39.2	31.5	0.1	14.3	-43.1	-57.3	35.8	43.1
126	ULS-EQU	-43.3	-60.3	64.8	50.6	-7.2	12.0	-54.0	-70.2	48.9	56.2
127	ULS-EQU	6.8	-21.6	14.7	10.6	-6.1	0.9	-12.3	-15.5	8.7	20.9
128	ULS-EQU	12.8	-15.5	11.3	7.2	-9.5	-4.5	-1.8	-3.4	2.7	14.8
129	ULS-EQU	12.8	-15.5	2.5	1.9	-0.7	4.3	-8.9	-12.1	2.7	14.8
130	ULS-EQU	-21.3	-49.6	57.3	42.4	-18.2	-3.0	-30.3	-37.0	30.6	42.8
131	ULS-EQU	-15.2	-43.6	53.9	39.0	-21.6	-8.4	-21.6	-24.9	24.6	36.7
132	ULS-EQU	-15.2	-43.6	45.1	33.7	-12.9	0.3	-26.9	-33.6	24.6	36.7
201	ULS-STR	-56.7	-56.7	72.8	56.6	-9.3	9.3	-56.6	-72.8	56.7	56.7
202	ULS-STR	-75.3	-75.3	96.6	75.1	-12.4	12.4	-75.1	-96.6	75.3	75.3
203	ULS-STR	-63.2	-63.2	89.8	68.3	-19.1	1.6	-57.7	-72.3	63.2	63.2
204	ULS-STR	-63.2	-63.2	72.3	57.7	-1.6	19.1	-68.3	-89.8	63.2	63.2
205	ULS-STR	26.0	-2.3	-10.0	-8.6	-2.9	-2.3	6.9	9.2	-10.5	1.6
206	ULS-STR	-2.0	-30.4	32.6	23.2	-15.1	-6.2	-11.1	-12.3	11.4	23.6
210	ULS-STR	33.0	4.6	-18.9	-15.5	-1.8	-3.4	13.8	18.1	-17.5	-5.3
211	ULS-STR	-43.6	-60.6	69.9	53.8	-11.5	8.4	-54.9	-70.4	52.8	60.1
212	ULS-STR	-60.4	-77.4	95.5	72.9	-18.8	6.0	-65.7	-83.3	66.0	73.3
213	ULS-STR	-31.5	-48.5	63.1	47.1	-18.3	-2.4	-37.5	-46.1	40.7	48.0
214	ULS-STR	-48.3	-65.3	88.7	66.2	-25.5	-4.7	-48.3	-59.0	53.9	61.2
215	ULS-STR	-31.5	-48.5	45.6	36.5	-0.7	15.1	-48.1	-63.6	40.7	48.0
216	ULS-STR	-48.3	-65.3	71.2	55.5	-8.0	12.8	-58.9	-76.5	53.9	61.2
217	ULS-STR	1.8	-26.6	21.1	15.5	-6.9	1.7	-17.2	-21.9	13.7	25.8
218	ULS-STR	7.8	-20.5	17.7	12.2	-10.3	-3.7	-8.6	-9.8	7.6	19.8
219	ULS-STR	7.8	-20.5	8.9	6.9	-1.5	5.1	-13.9	-18.5	7.6	19.8
220	ULS-STR	-26.2	-54.6	63.7	47.3	-19.1	-2.2	-35.3	-43.4	35.6	47.8
221	ULS-STR	-20.2	-48.5	60.3	43.9	-22.4	-7.6	-26.6	-31.3	29.6	41.7
222	ULS-STR	-20.2	-48.5	51.5	38.6	-13.7	1.2	-31.9	-40.0	29.6	41.7
231	ULS-STR	-19.4	-36.4	38.8	29.7	-7.5	4.4	-30.7	-39.3	28.6	35.9
232	ULS-STR	-36.2	-53.2	64.4	48.8	-14.8	2.0	-41.5	-52.3	41.8	49.1
233	ULS-STR	-13.3	-30.3	35.5	26.3	-10.9	-1.0	-22.0	-27.2	22.6	29.9
234	ULS-STR	-30.1	-47.1	61.0	45.4	-18.2	-3.4	-32.9	-40.1	35.7	43.0
235	ULS-STR	-13.3	-30.3	26.7	21.0	-2.1	7.8	-27.3	-36.0	22.6	29.9
236	ULS-STR	-30.1	-47.1	52.3	40.1	-9.4	5.4	-38.2	-48.9	35.7	43.0
251	ULS-STR	-39.6	-56.6	64.8	49.9	-10.8	7.7	-50.9	-65.3	48.9	56.2
252	ULS-STR	-56.4	-73.4	90.3	69.0	-18.1	5.3	-61.7	-78.2	62.0	69.3
253	ULS-STR	-27.5	-44.5	58.0	43.1	-17.6	-3.1	-33.5	-41.0	36.8	44.1
254	ULS-STR	-44.3	-61.3	83.6	62.2	-24.9	-5.4	-44.3	-53.9	49.9	57.2
255	ULS-STR	-27.5	-44.5	40.5	32.5	-0.1	14.5	-44.1	-58.5	36.8	44.1
256	ULS-STR	-44.3	-61.3	66.1	51.6	-7.4	12.1	-55.0	-71.4	49.9	57.2
257	ULS-STR	5.8	-22.6	16.0	11.6	-6.3	1.0	-13.3	-16.8	9.7	21.9
258	ULS-STR	11.8	-16.5	12.6	8.2	-9.7	-4.3	-2.9	-4.6	3.7	15.8
259	ULS-STR	11.8	-16.5	3.8	2.9	-0.9	4.4	-9.9	-13.4	3.7	15.8
260	ULS-STR	-22.3	-50.6	58.5	43.4	-18.4	-2.9	-31.3	-38.3	31.6	43.8
261	ULS-STR	-16.2	-44.6	55.2	40.0	-21.8	-8.3	-22.6	-26.2	25.6	37.7
262	ULS-STR	-16.2	-44.6	46.4	34.7	-13.0	0.5	-27.9	-34.9	25.6	37.7
301	SLS	-39.8	-39.8	51.1	39.7	-6.5	6.5	-39.7	-51.1	39.8	39.8
302	SLS	-52.2	-52.2	66.9	52.0	-8.6	8.6	-52.0	-66.9	52.2	52.2
303	SLS	-44.1	-44.1	62.4	47.5	-13.1	1.4	-40.5	-50.7	44.1	44.1
304	SLS	-44.1	-44.1	50.7	40.5	-1.4	13.1	-47.5	-62.4	44.1	44.1
305	SLS	15.3	-3.6	-4.1	-3.8	-2.3	-1.2	2.6	3.6	-5.0	3.1
306	SLS	-3.4	-22.3	24.3	17.4	-10.4	-3.8	-9.4	-10.8	9.6	17.7
311	SLS	-31.0	-42.4	49.2	37.9	-8.0	5.9	-38.6	-49.5	37.2	42.1
312	SLS	-42.2	-53.6	66.2	50.6	-12.8	4.3	-45.8	-58.1	46.0	50.9
313	SLS	-23.0	-34.3	44.6	33.4	-12.5	-1.3	-27.0	-33.3	29.2	34.0
314	SLS	-34.2	-45.5	61.7	46.1	-17.4	-2.8	-34.2	-41.9	37.9	42.8
315	SLS	-23.0	-34.3	33.0	26.3	-0.8	10.4	-34.0	-45.0	29.2	34.0
316	SLS	-34.2	-45.5	50.0	39.0	-5.7	8.8	-41.3	-53.6	37.9	42.8
317	SLS	-0.8	-19.7	16.6	12.3	-4.9	1.5	-13.5	-17.1	11.1	19.2
318	SLS	3.2	-15.7	14.3	10.1	-7.2	-2.1	-7.7	-9.1	7.1	15.2
319	SLS	3.2	-15.7	8.5	6.6	-1.4	3.7	-11.2	-14.9	7.1	15.2
320	SLS	-19.5	-38.4	45.0	33.5	-13.0	-1.2	-25.5	-31.5	25.7	33.8
321	SLS	-15.5	-34.4	42.7	31.3	-15.3	-4.7	-19.7	-23.4	21.7	29.8
322	SLS	-15.5	-34.4	36.9	27.7	-9.5	1.1	-23.3	-29.2	21.7	29.8
331	SLS	-25.5	-31.1	37.3	28.9	-5.6	4.6	-29.2	-37.5	28.6	31.0
332	SLS	-31.1	-36.7	45.9	35.2	-8.1	3.8	-32.8	-41.8	32.9	35.4
333	SLS	-21.4	-27.1	35.1	26.6	-7.9	1.0	-23.4	-29.4	24.5	27.0
334	SLS	-27.0	-32.7	43.6	33.0	-10.3	0.2	-27.0	-33.7	28.9	31.3
335	SLS	-21.4	-27.1	29.2	23.1	-2.0	6.8	-26.9	-35.3	24.5	27.0
336	SLS	-27.0	-32.7	37.8	29.4	-4.5	6.1	-30.6	-39.6	28.9	31.3
337	SLS	-12.9	-16.6	19.6	15.1	-3.1	2.4	-15.4	-19.7	14.9	16.5
338	SLS	-12.9	-16.6	19.6	15.1	-3.1	2.4	-15.4	-19.7	14.9	16.5
339	SLS	-12.9	-16.6	19.6	15.1	-3.1	2.4	-15.4	-19.7	14.9	16.5
340	SLS	-16.6	-20.4	25.3	19.4	-4.7	1.9	-17.8	-22.6	17.8	19.5
341	SLS	-16.6	-20.4	25.3	19.4	-4.7	1.9	-17.8	-22.6	17.8	19.5
342	SLS	-16.6	-20.4	25.3	19.4	-4.7	1.9	-17.8	-22.6	17.8	19.5
351	SLS	-9.3	-15.0	16.6	12.8	-3.0	1.9	-13.1	-16.8	12.4	14.9
352	SLS	-14.9	-20.6	25.2	19.1	-5.4	1.1	-16.7	-21.1	16.8	19.2
353	SLS	-9.3	-15.0	16.6	12.8	-3.0	1.9	-13.1	-16.8	12.4	14.9
354	SLS	-14.9	-20.6	25.2	19.1	-5.4	1.1	-16.7	-21.1	16.8	19.2
355	SLS	-9.3	-15.0	16.6	12.8	-3.0	1.9	-13.1	-16.8	12.4	14.9
356	SLS	-14.9	-20.6	25.2	19.1	-5.4	1.1	-16.7	-21.1	16.8	19.2

A:left end, C:haunch end, B: right end

8.5. Bending moments Med [kNm]

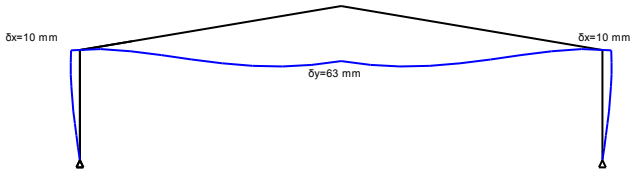
L.C.	Left column 1			Right column 4		
	MedA,1	MedM,1	MedB,1	MedA,4	MedM,4	MedB,4
101 ULS-EQU	0.0	-129.3	-258.7	-258.7	-129.3	0.0
102 ULS-EQU	0.0	-175.8	-351.5	-351.5	-175.8	0.0
103 ULS-EQU	0.0	-145.5	-291.0	-291.0	-145.5	0.0
104 ULS-EQU	0.0	-145.5	-291.0	-291.0	-145.5	0.0
105 ULS-EQU	0.0	42.0	84.0	47.1	23.6	0.0
106 ULS-EQU	0.0	0.8	-56.2	-62.6	-31.3	0.0
111 ULS-EQU	0.0	52.0	103.9	67.0	33.5	0.0
121 ULS-EQU	0.0	-117.7	-235.5	-257.6	-128.8	0.0
122 ULS-EQU	0.0	-159.8	-319.6	-323.4	-161.7	0.0
123 ULS-EQU	0.0	-87.5	-174.9	-197.1	-98.5	0.0
124 ULS-EQU	0.0	-129.5	-259.1	-262.9	-131.4	0.0
125 ULS-EQU	0.0	-87.5	-174.9	-197.1	-98.5	0.0
126 ULS-EQU	0.0	-129.5	-259.1	-262.9	-131.4	0.0
127 ULS-EQU	0.0	4.0	-37.0	-73.9	-37.0	0.0
128 ULS-EQU	0.0	14.5	-6.8	-43.7	-21.8	0.0
129 ULS-EQU	0.0	14.5	-6.8	-43.7	-21.8	0.0
130 ULS-EQU	0.0	-88.6	-177.2	-183.6	-91.8	0.0
131 ULS-EQU	0.0	-73.5	-147.0	-153.3	-76.7	0.0
132 ULS-EQU	0.0	-73.5	-147.0	-153.3	-76.7	0.0
201 ULS-STR	0.0	-141.8	-283.6	-283.6	-141.8	0.0
202 ULS-STR	0.0	-188.2	-376.4	-376.4	-188.2	0.0
203 ULS-STR	0.0	-157.9	-315.9	-315.9	-157.9	0.0
204 ULS-STR	0.0	-157.9	-315.9	-315.9	-157.9	0.0
205 ULS-STR	0.0	59.6	59.1	22.2	-0.5	0.0
206 ULS-STR	0.0	-40.5	-81.1	-87.4	-43.7	0.0
210 ULS-STR	0.0	47.0	94.0	57.1	28.5	0.0
211 ULS-STR	0.0	-130.2	-260.3	-282.5	-141.2	0.0
212 ULS-STR	0.0	-172.2	-344.5	-348.3	-174.1	0.0
213 ULS-STR	0.0	-99.9	-199.8	-222.0	-111.0	0.0
214 ULS-STR	0.0	-142.0	-283.9	-287.8	-143.9	0.0
215 ULS-STR	0.0	-99.9	-199.8	-222.0	-111.0	0.0
216 ULS-STR	0.0	-142.0	-283.9	-287.8	-143.9	0.0
217 ULS-STR	0.0	0.3	-61.9	-98.8	-49.4	0.0
218 ULS-STR	0.0	5.4	-31.7	-68.5	-34.3	0.0
219 ULS-STR	0.0	5.4	-31.7	-68.5	-34.3	0.0
220 ULS-STR	0.0	-101.1	-202.1	-208.5	-104.2	0.0
221 ULS-STR	0.0	-85.9	-171.9	-178.2	-89.1	0.0
222 ULS-STR	0.0	-85.9	-171.9	-178.2	-89.1	0.0
231 ULS-STR	0.0	-69.6	-139.3	-161.4	-80.7	0.0
232 ULS-STR	0.0	-111.7	-223.4	-227.2	-113.6	0.0
233 ULS-STR	0.0	-54.5	-109.0	-131.2	-65.6	0.0
234 ULS-STR	0.0	-96.6	-193.2	-197.0	-98.5	0.0
235 ULS-STR	0.0	-54.5	-109.0	-131.2	-65.6	0.0
236 ULS-STR	0.0	-96.6	-193.2	-197.0	-98.5	0.0
251 ULS-STR	0.0	-120.2	-240.4	-262.6	-131.3	0.0
252 ULS-STR	0.0	-162.3	-324.6	-328.4	-164.2	0.0
253 ULS-STR	0.0	-90.0	-179.9	-202.1	-101.0	0.0
254 ULS-STR	0.0	-132.0	-264.0	-267.9	-133.9	0.0
255 ULS-STR	0.0	-90.0	-179.9	-202.1	-101.0	0.0
256 ULS-STR	0.0	-132.0	-264.0	-267.9	-133.9	0.0
257 ULS-STR	0.0	2.9	-42.0	-78.9	-39.5	0.0
258 ULS-STR	0.0	12.3	-11.8	-48.6	-24.3	0.0
259 ULS-STR	0.0	12.3	-11.8	-48.6	-24.3	0.0
260 ULS-STR	0.0	-91.1	-182.2	-188.6	-94.3	0.0
261 ULS-STR	0.0	-76.0	-152.0	-158.3	-79.2	0.0
262 ULS-STR	0.0	-76.0	-152.0	-158.3	-79.2	0.0
301 SLS	0.0	-99.5	-199.0	-199.0	-99.5	0.0
302 SLS	0.0	-130.4	-260.9	-260.9	-130.4	0.0
303 SLS	0.0	-110.3	-220.5	-220.5	-110.3	0.0
304 SLS	0.0	-110.3	-220.5	-220.5	-110.3	0.0
305 SLS	0.0	31.1	29.5	4.9	-2.9	0.0
306 SLS	0.0	-32.0	-64.0	-68.2	-34.1	0.0
311 SLS	0.0	-91.8	-183.5	-198.3	-99.1	0.0
312 SLS	0.0	-119.8	-239.6	-242.1	-121.1	0.0
313 SLS	0.0	-71.6	-143.2	-157.9	-79.0	0.0
314 SLS	0.0	-99.6	-199.2	-201.8	-100.9	0.0
315 SLS	0.0	-71.6	-143.2	-157.9	-79.0	0.0
316 SLS	0.0	-99.6	-199.2	-201.8	-100.9	0.0
317 SLS	0.0	-25.6	-51.2	-75.8	-37.9	0.0
318 SLS	0.0	1.4	-31.1	-55.6	-27.8	0.0
319 SLS	0.0	1.4	-31.1	-55.6	-27.8	0.0
320 SLS	0.0	-72.3	-144.7	-148.9	-74.5	0.0
321 SLS	0.0	-62.3	-124.5	-128.8	-64.4	0.0
322 SLS	0.0	-62.3	-124.5	-128.8	-64.4	0.0
331 SLS	0.0	-70.8	-141.5	-148.9	-74.4	0.0
332 SLS	0.0	-84.8	-169.5	-170.8	-85.4	0.0
333 SLS	0.0	-60.7	-121.3	-128.7	-64.4	0.0
334 SLS	0.0	-74.7	-149.4	-150.6	-75.3	0.0
335 SLS	0.0	-60.7	-121.3	-128.7	-64.4	0.0
336 SLS	0.0	-74.7	-149.4	-150.6	-75.3	0.0
337 SLS	0.0	-36.9	-73.7	-78.6	-39.3	0.0
338 SLS	0.0	-36.9	-73.7	-78.6	-39.3	0.0
339 SLS	0.0	-36.9	-73.7	-78.6	-39.3	0.0
340 SLS	0.0	-46.2	-92.4	-93.2	-46.6	0.0
341 SLS	0.0	-46.2	-92.4	-93.2	-46.6	0.0
342 SLS	0.0	-46.2	-92.4	-93.2	-46.6	0.0
351 SLS	0.0	-30.4	-60.8	-68.2	-34.1	0.0
352 SLS	0.0	-44.4	-88.8	-90.1	-45.1	0.0
353 SLS	0.0	-30.4	-60.8	-68.2	-34.1	0.0
354 SLS	0.0	-44.4	-88.8	-90.1	-45.1	0.0
355 SLS	0.0	-30.4	-60.8	-68.2	-34.1	0.0
356 SLS	0.0	-44.4	-88.8	-90.1	-45.1	0.0

A:left end, B: right end

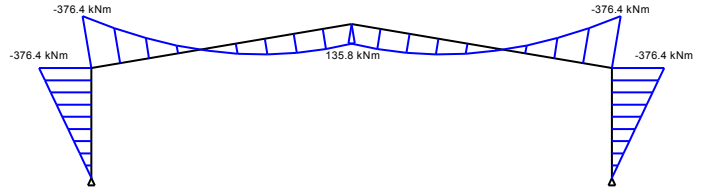
L.C.	Left rafter 2				Right rafter 3				
	MedA,2	MedC2	MedM,2	MedB,2	MedA,3	MedM,3	MedC3	MedB,3	
101	ULS-EQU	-258.7	-117.1	99.2	93.3	93.3	99.2	-117.1	-258.7
102	ULS-EQU	-351.5	-159.2	134.8	126.8	126.8	134.8	-159.2	-351.5
103	ULS-EQU	-291.0	-114.9	125.0	105.0	105.0	105.0	-114.9	-291.0
104	ULS-EQU	-291.0	-148.6	105.0	105.0	105.0	125.0	-114.9	-291.0
105	ULS-EQU	84.0	48.1	27.7	-28.5	-28.5	-31.7	14.2	47.1
106	ULS-EQU	-56.2	-2.9	47.1	16.5	16.5	-23.0	-47.0	-62.6
111	ULS-EQU	103.9	57.1	34.1	-35.7	-35.7	-39.2	23.2	67.0
121	ULS-EQU	-235.5	-100.6	95.3	86.0	86.0	90.8	-120.9	-257.6
122	ULS-EQU	-319.6	-131.2	131.3	113.0	113.0	115.0	-158.2	-323.4
123	ULS-EQU	-174.9	-56.3	89.1	64.2	64.2	-66.5	-110.4	-197.1
124	ULS-EQU	-259.1	-86.9	125.9	91.2	91.2	-85.9	-147.7	-262.9
125	ULS-EQU	-174.9	-90.1	-55.4	64.2	64.2	81.5	-76.6	-197.1
126	ULS-EQU	-259.1	-120.6	95.6	91.2	91.2	101.8	-113.9	-262.9
127	ULS-EQU	-37.0	-6.7	26.0	15.1	15.1	15.4	-40.6	-73.9
128	ULS-EQU	-6.8	15.4	30.6	4.2	4.2	-19.7	-34.2	-43.7
129	ULS-EQU	-6.8	-1.5	5.2	4.2	4.2	10.9	-18.4	-43.7
130	ULS-EQU	-177.2	-57.7	87.0	60.1	60.1	-61.7	-102.8	-183.6
131	ULS-EQU	-147.0	-35.5	86.9	49.2	49.2	-52.1	-97.5	-153.3
132	ULS-EQU	-147.0	-52.4	66.6	49.2	49.2	49.3	-80.7	-153.3
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201	ULS-STR	-283.6	-128.4	108.7	102.3	102.3	108.7	-128.4	-283.6
202	ULS-STR	-376.4	-170.4	144.3	135.8	135.8	144.3	-170.4	-376.4
203	ULS-STR	-315.9	-126.1	134.4	113.9	113.9	114.1	-159.9	-315.9
204	ULS-STR	-315.9	-159.9	114.1	113.9	113.9	134.4	-126.1	-315.9
205	ULS-STR	59.1	36.8	19.8	-19.6	-19.6	-22.3	3.0	22.2
206	ULS-STR	-81.1	-14.1	54.5	25.5	25.5	-31.0	-59.2	-87.4
210	ULS-STR	94.0	52.6	30.9	-32.1	-32.1	-35.5	18.7	57.1
211	ULS-STR	-260.3	-111.8	104.8	95.0	95.0	100.3	-132.2	-282.5
212	ULS-STR	-344.5	-142.4	140.7	122.0	122.0	124.4	-169.5	-348.3
213	ULS-STR	-199.8	-67.6	98.0	73.1	73.1	-74.4	-121.6	-222.0
214	ULS-STR	-283.9	-98.1	134.9	100.1	100.1	-93.8	-159.0	-287.8
215	ULS-STR	-199.8	-101.3	73.2	73.1	73.1	90.8	-87.9	-222.0
216	ULS-STR	-283.9	-131.9	105.1	100.1	100.1	111.2	-125.2	-287.8
217	ULS-STR	-61.9	-18.0	34.5	24.1	24.1	24.8	-51.8	-98.8
218	ULS-STR	-31.7	4.1	36.3	13.2	13.2	-27.7	-46.6	-68.5
219	ULS-STR	-31.7	-12.7	14.6	13.2	13.2	19.8	-29.7	-68.5
220	ULS-STR	-202.1	-68.9	95.8	69.1	69.1	-69.7	-114.1	-208.5
221	ULS-STR	-171.9	-46.8	95.3	58.2	58.2	-60.0	-108.8	-178.2
222	ULS-STR	-171.9	-63.7	75.7	58.2	58.2	58.4	-91.9	-178.2
231	ULS-STR	-139.3	-57.0	58.7	51.3	51.3	54.0	-77.3	-161.4
232	ULS-STR	-223.4	-87.6	95.1	78.3	78.3	78.8	-114.7	-227.2
233	ULS-STR	-109.0	-34.9	56.0	40.4	40.4	-45.4	-72.1	-131.2
234	ULS-STR	-193.2	-65.5	92.8	67.4	67.4	-64.8	-109.4	-197.0
235	ULS-STR	-109.0	-51.8	41.3	40.4	40.4	48.8	-55.2	-131.2
236	ULS-STR	-193.2	-82.3	76.1	67.4	67.4	70.7	-92.5	-197.0
251	ULS-STR	-240.4	-102.8	97.2	87.8	87.8	92.7	-123.1	-262.6
252	ULS-STR	-324.6	-133.4	133.2	114.8	114.8	116.9	-160.5	-328.4
253	ULS-STR	-179.9	-58.6	90.9	65.9	65.9	-68.1	-112.6	-202.1
254	ULS-STR	-264.0	-89.1	127.7	93.0	93.0	-87.4	-149.9	-267.9
255	ULS-STR	-179.9	-92.3	65.9	65.9	65.9	83.4	-78.9	-202.1
256	ULS-STR	-264.0	-122.9	97.5	93.0	93.0	103.6	-116.2	-267.9
257	ULS-STR	-42.0	-9.0	27.7	16.9	16.9	17.3	-42.8	-78.9
258	ULS-STR	-11.8	13.2	31.5	6.0	6.0	-21.3	-37.9	-48.6
259	ULS-STR	-11.8	-3.7	7.0	6.0	6.0	12.7	-20.7	-48.6
260	ULS-STR	-182.2	-59.9	88.7	61.9	61.9	-63.3	-105.0	-188.6
261	ULS-STR	-152.0	-37.8	88.6	51.0	51.0	-53.6	-99.8	-158.3
262	ULS-STR	-152.0	-54.7	68.4	51.0	51.0	51.1	-82.9	-158.3
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301	SLS	-199.0	-90.1	76.3	71.8	71.8	76.3	-90.1	-199.0
302	SLS	-260.9	-118.1	100.0	94.1	94.1	100.0	-118.1	-260.9
303	SLS	-220.5	-88.6	93.3	79.5	79.5	79.8	-111.1	-220.5
304	SLS	-220.5	-111.1	79.8	79.5	79.5	93.3	-88.6	-220.5
305	SLS	29.5	20.0	10.0	-9.5	-9.5	-11.3	-2.5	4.9
306	SLS	-64.0	-13.9	39.5	20.6	20.6	-23.8	-44.0	-68.2
311	SLS	-183.5	-79.1	73.7	66.9	66.9	70.7	-92.6	-198.3
312	SLS	-239.6	-99.4	97.6	84.9	84.9	86.7	-117.5	-242.1
313	SLS	-143.2	-49.6	69.0	52.3	52.3	-52.8	-85.6	-157.9
314	SLS	-199.2	-69.9	93.5	70.3	70.3	-65.7	-110.5	-201.8
315	SLS	-143.2	-72.1	52.5	52.3	52.3	64.2	-63.1	-157.9
316	SLS	-199.2	-92.4	73.9	70.3	70.3	78.0	-88.0	-201.8
317	SLS	-51.2	-16.5	26.5	19.7	19.7	20.3	-39.1	-75.8
318	SLS	-31.1	-1.7	27.0	12.4	12.4	-21.6	-35.6	-55.6
319	SLS	-31.1	-13.0	13.5	12.4	12.4	16.9	-24.3	-55.6
320	SLS	-144.7	-50.5	67.5	49.7	49.7	-49.6	-80.5	-148.9
321	SLS	-124.5	-35.7	66.9	42.4	42.4	-43.2	-77.0	-128.8
322	SLS	-124.5	-47.0	54.1	42.4	42.4	42.6	-65.8	-128.8
331	SLS	-141.5	-62.1	55.9	51.4	51.4	54.4	-68.8	-148.9
332	SLS	-169.5	-72.2	67.7	60.4	60.4	62.3	-81.3	-170.8
333	SLS	-121.3	-47.3	52.9	44.1	44.1	44.3	-65.3	-128.7
334	SLS	-149.4	-57.5	65.1	53.1	53.1	53.1	-77.8	-150.6
335	SLS	-121.3	-58.5	44.9	44.1	44.1	50.9	-54.1	-128.7
336	SLS	-149.4	-68.7	56.0	53.1	53.1	58.0	-66.5	-150.6
337	SLS	-73.7	-32.0	29.4	26.8	26.8	28.4	-36.5	-78.6
338	SLS	-73.7	-32.0	29.4	26.8	26.8	28.4	-36.5	-78.6
339	SLS	-73.7	-32.0	29.4	26.8	26.8	28.4	-36.5	-78.6
340	SLS	-92.4	-38.8	37.3	32.8	32.8	33.7	-44.8	-93.2
341	SLS	-92.4	-38.8	37.3	32.8	32.8	33.7	-44.8	-93.2
342	SLS	-92.4	-38.8	37.3	32.8	32.8	33.7	-44.8	-93.2
351	SLS	-60.8	-25.5	25.0	22.3	22.3	23.5	-32.3	-68.2
352	SLS	-88.8	-35.7	37.1	31.3	31.3	31.6	-44.7	-90.1
353	SLS	-60.8	-25.5	25.0	22.3	22.3	23.5	-32.3	-68.2
354	SLS	-88.8	-35.7	37.1	31.3	31.3	31.6	-44.7	-90.1
355	SLS	-60.8	-25.5	25.0	22.3	22.3	23.5	-32.3	-68.2
356	SLS	-88.8	-35.7	37.1	31.3	31.3	31.6	-44.7	-90.1

-A:left end, C:haunch end, M: span, B: right end

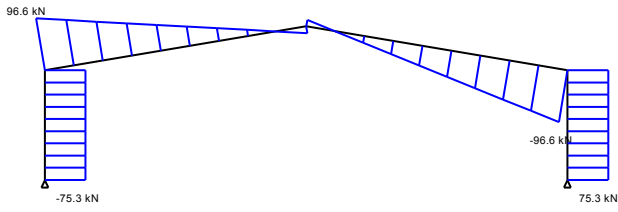
L.C. 202 Displacements mm



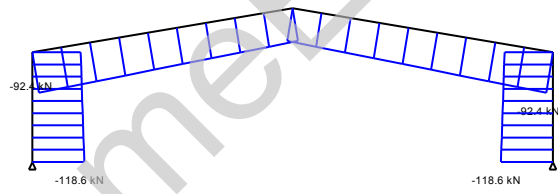
L.C. 202 Bend. moments kNm



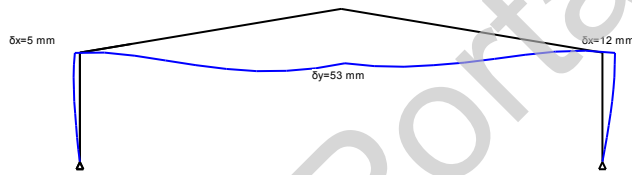
L.C. 202 Shear forces kN



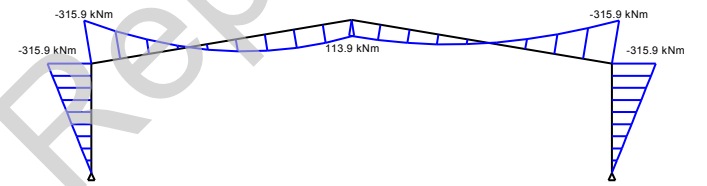
L.C. 202 Axial forces kN



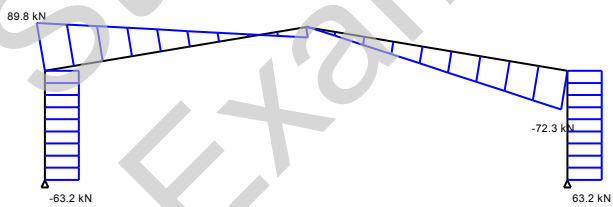
L.C. 203 Displacements mm



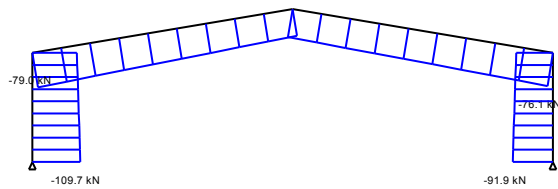
L.C. 203 Bend. moments kNm



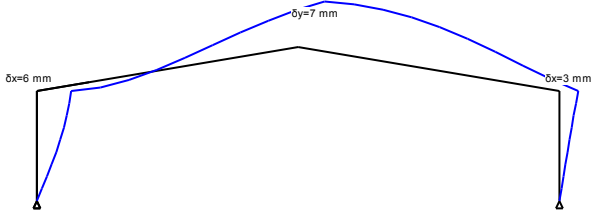
L.C. 203 Shear forces kN



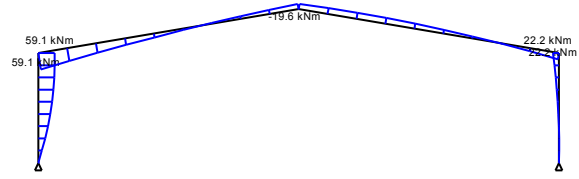
L.C. 203 Axial forces kN



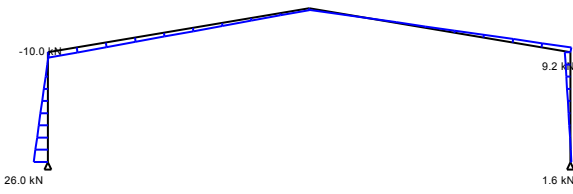
L.C. 205 Displacements mm



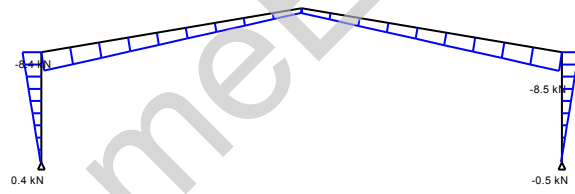
L.C. 205 Bend. moments kNm



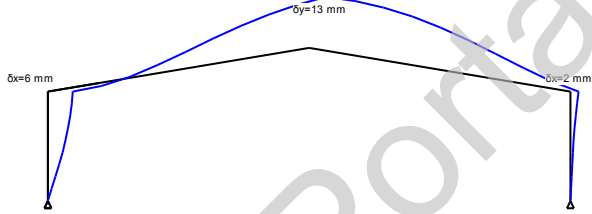
L.C. 205 Shear forces kN



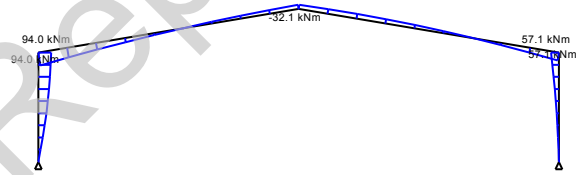
L.C. 205 Axial forces kN



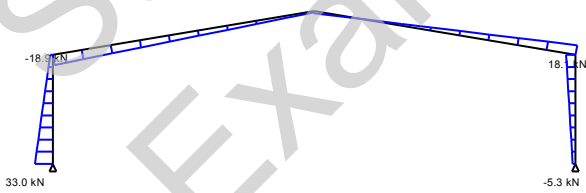
L.C. 210 Displacements mm



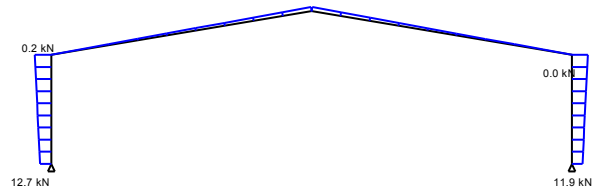
L.C. 210 Bend. moments kNm



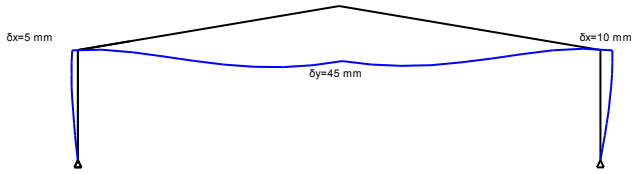
L.C. 210 Shear forces kN



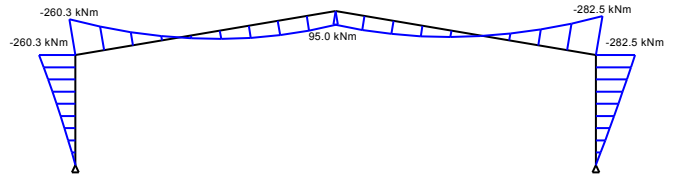
L.C. 210 Axial forces kN



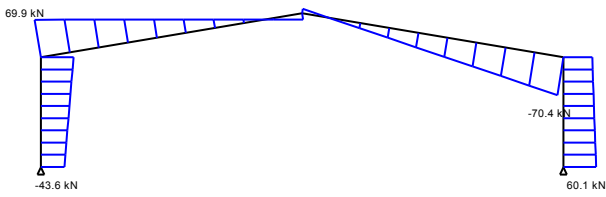
L.C. 211 Displacements mm



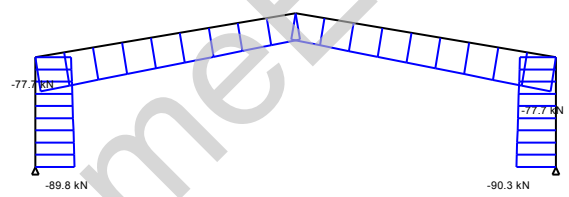
L.C. 211 Bend. moments kNm



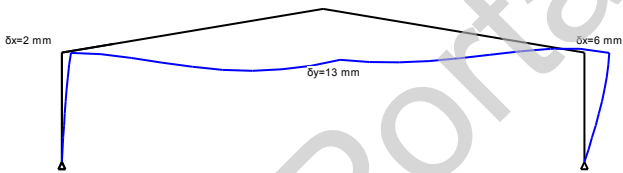
L.C. 211 Shear forces kN



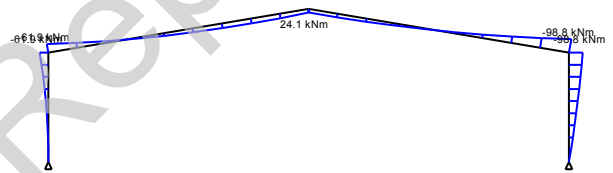
L.C. 211 Axial forces kN



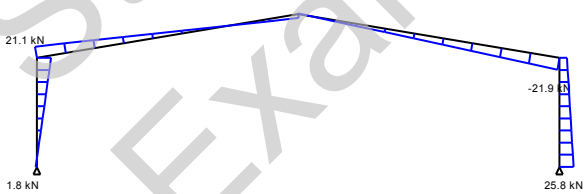
L.C. 217 Displacements mm



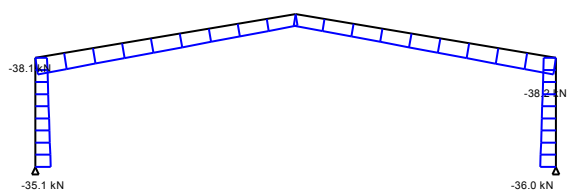
L.C. 217 Bend. moments kNm



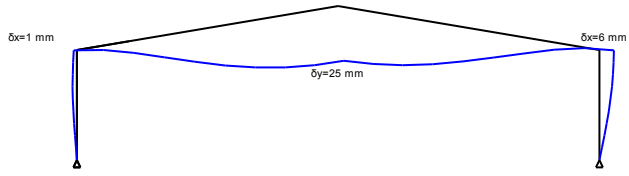
L.C. 217 Shear forces kN



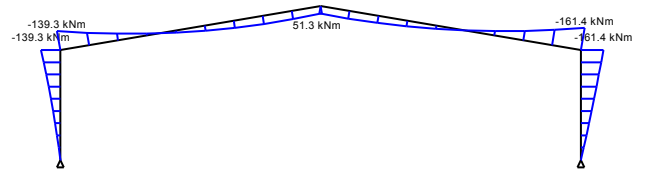
L.C. 217 Axial forces kN



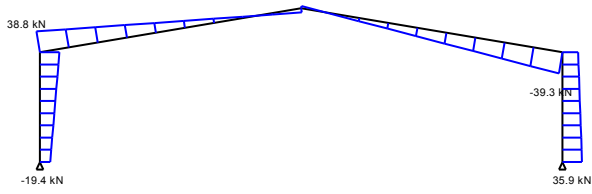
L.C. 231 Displacements mm



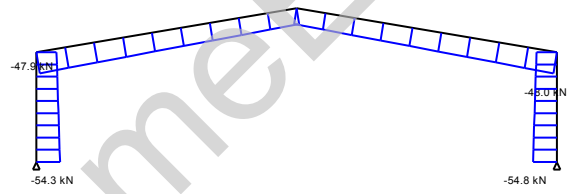
L.C. 231 Bend. moments kNm



L.C. 231 Shear forces kN



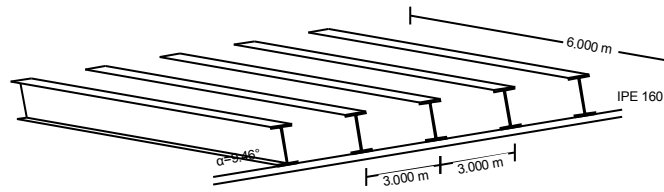
L.C. 231 Axial forces kN



SteelPortalFrameFC3
Example Report

9. Design of Purlins

Purlin laterally restrained, IPE 160 S 355
 Continuous purlin, L= 6.000 m, s= 3.000 m



9.1. Materials

Steel: S 355 (EN1993-1-1, §3.2)
 t ≤ 40 mm, Yield strength $f_y = 355 \text{ N/mm}^2$, Ultimate strength $f_u = 510 \text{ N/mm}^2$
 40mm < t ≤ 80 mm, Yield strength $f_y = 335 \text{ N/mm}^2$, Ultimate strength $f_u = 470 \text{ N/mm}^2$
 Modulus of elasticity $E = 210000 \text{ N/mm}^2$, Poisson ratio $\nu = 0.30$, Unit mass $\rho = 7850 \text{ Kg/m}^3$

Partial safety factors for actions (EN1990, Annex A1)
 $\gamma_{G,sup} = 1.35$, $\gamma_Q = 1.50$, $\gamma_{G,inf} = 1.00$, $\psi_0 = 0.70$

Partial factors for materials (EN1993-1-1, §6.1)
 $\gamma_{M0} = 1.00$, $\gamma_{M1} = 1.00$, $\gamma_{M2} = 1.25$

9.2. Loading

(EN1991-1-1)

Roof loads

Roof slope	$\alpha = 9.46^\circ$	
Load of roof covering	$g_{k1} = 0.200 \text{ kN/m}^2$	(EN1991-1-1 §5)
Imposed load (category H)	$q_k = 0.400 \text{ kN/m}^2$	(EN1991-1-1 §6.3.4.2)
Snow load	$s_k = 0.640 \text{ kN/m}^2$	(EN1991-1-3 §5.3)
Wind pressure	$w_k = 0.000 \text{ kN/m}^2$	(EN1991-1-4 §7.2)
Wind uplift	$w_k = -0.460 \text{ kN/m}^2$	

Load on purlin

Purlin spacing	$s = 3.000 \text{ m}$
Load of roof covering	$G_{k1} = 3.000 \times 0.200 = 0.60 \text{ kN/m}$
Purlin weight	$G_{k2} = 0.15 \text{ kN/m}$
Permanent load	$G_k = G_{k1} + G_{k2} = 0.60 + 0.15 = 0.75 \text{ kN/m}$
Imposed load (category H)	$Q_{kk} = 3.000 \times 0.400 = 1.20 \text{ kN/m}$
Snow load	$Q_{sk} = 3.000 \times 0.640 = 1.92 \text{ kN/m}$
Wind uplift	$Q_{wk} = -3.000 \times 0.460 = -1.38 \text{ kN/m}$

Load on purlin main axis(z) and transverse direction(y)

Permanent load	$G_{k,z} = 0.75 \times \cos(9.46) = 0.74 \text{ kN/m}$, $G_{k,y} = 0.75 \times \sin(9.46) = 0.12 \text{ kN/m}$
Imposed load (category H)	$Q_{kk,z} = 1.20 \times \cos(9.46) = 1.18 \text{ kN/m}$, $Q_{kk,y} = 1.20 \times \sin(9.46) = 0.20 \text{ kN/m}$
Snow load	$Q_{sk,z} = 1.92 \times \cos(9.46) = 1.89 \text{ kN/m}$, $Q_{sk,y} = 1.92 \times \sin(9.46) = 0.32 \text{ kN/m}$
Wind pressure	$Q_{wk,z} = 0.00 \text{ kN/m}$, $Q_{wk,y} = 0.00 \text{ kN/m}$
Wind uplift	$Q_{wk,z} = -1.38 \text{ kN/m}$, $Q_{wk,y} = 0.00 \text{ kN/m}$

9.3. Design values of Actions, Load combinations

<u>Ultimate Limit State, Load combinations</u>		(EN1990 §6.4.3.2, T.A1.2A, T.A1.2B)
Sagging	$\gamma_{G, sup} \cdot G_{k, z} + \gamma_Q \cdot Q_{k, z} + \gamma_Q \cdot \psi_o \cdot Q_{wk, z} = 1.35 \times 0.74 + 1.50 \times 1.89 + 1.50 \times 0.60 \times 0.00 = 3.84 \text{ kN/m}$	
Hogging	$\gamma_{G, inf} \cdot G_{k, z} - \gamma_Q \cdot Q_{wk, z} = 1.00 \times 0.74 - 1.50 \times 1.38 = -1.33 \text{ kN/m}$	
Transverse	$\gamma_{G, sup} \cdot G_{k, y} + \gamma_Q \cdot Q_{k, y} = 1.35 \times 0.12 + 1.50 \times 0.32 = 0.64 \text{ kN/m}$	

<u>Serviceability Limit State (SLS), Load combinations</u>		(EN1990 §6.5.3, T.A1.4)
Sagging	$G_{k, z} + Q_{k, z} + \psi_o \cdot Q_{wk, z} = 0.74 + 1.89 + 0.60 \times 0.00 = 2.63 \text{ kN/m}$	
Hogging	$G_{k, z} + Q_{wk, z} = 0.74 - 1.38 = -0.64 \text{ kN/m}$	

9.4. Design actions

Design actions, Ultimate Limit State

Sagging	$M_{yed, o} = 0.078 \times 3.84 \times 6.000^2 = 10.78 \text{ kNm}$, $M_{yed, s} = -0.105 \times 3.84 \times 6.000^2 = -14.51 \text{ kNm}$ $V_{zed} = 0.605 \times 3.84 \times 6.000 = 13.94 \text{ kN}$
Hogging	$M_{yed, o} = -0.078 \times 1.33 \times 6.000^2 = -3.74 \text{ kNm}$, $M_{yed, s} = 0.105 \times 1.33 \times 6.000^2 = 5.03 \text{ kNm}$ $V_{zed} = 0.605 \times 1.33 \times 6.000 = 4.83 \text{ kN}$
Transverse	Laterally restrained

Design actions, Serviceability Limit State (SLS)

Sagging	$M_{yed, o} = 0.078 \times 2.63 \times 6.000^2 = 7.40 \text{ kNm}$, $M_{yed, s} = -0.105 \times 2.63 \times 6.000^2 = -9.96 \text{ kNm}$
Hogging	$M_{yed, o} = -0.078 \times 0.64 \times 6.000^2 = -1.80 \text{ kNm}$, $M_{yed, s} = 0.105 \times 0.64 \times 6.000^2 = 2.42 \text{ kNm}$

9.5. Cross-section properties, Purlins

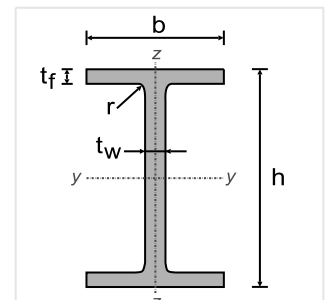
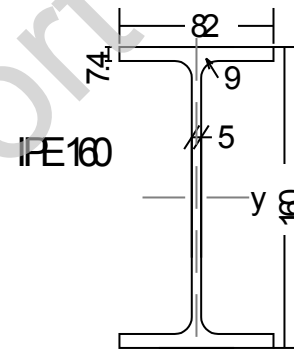
Cross-section IPE 160-S 355

Dimensions of cross section

Depth of cross section	h = 160.00 mm
Width of cross section	b = 82.00 mm
Web depth	hw = 152.60 mm
Depth of straight portion of web	dw = 127.20 mm
Web thickness	tw = 5.00 mm
Flange thickness	tf = 7.40 mm
Radius of root fillet	r = 9.00 mm
Mass	= 15.80 Kg/m

Properties of cross section

Area	A = 2009 mm ²	
Second moment of area	Iy = 8.693 × 10 ⁶ mm ⁴	Iz = 0.683 × 10 ⁶ mm ⁴
Section modulus	Wy = 108.70 × 10 ³ mm ³	Wz = 16.660 × 10 ³ mm ³
Plastic section modulus	Wpy = 123.90 × 10 ³ mm ³	Wpz = 26.100 × 10 ³ mm ³
Radius of gyration	iy = 65.8 mm	iz = 18.4 mm
Shear area	Avz = 966 mm ²	Avy = 1214 mm ²
Torsional constant	It = 0.036 × 10 ⁶ mm ⁴	ip = 68 mm
Warping constant	Iw = 3.959 × 10 ⁹ mm ⁶	



(EN1993-1-1, §7)

9.6. Serviceability Limit State (SLS), Purlins

Purlin deflections, Sagging

Loading G+Q:	$w = 2.63 \times 6000^4 / (153.6 \times 2.1 \times 10^5 \times 8.693 \times 10^6) = 12.17 \text{ mm} = L/493 < L/200$
Loading Q:	$w = 1.89 \times 6000^4 / (153.6 \times 2.1 \times 10^5 \times 8.693 \times 10^6) = 8.75 \text{ mm} = L/686 < L/250$

Purlin deflections, Hogging

Loading G+Q:	$w = -0.64 \times 6000^4 / (153.6 \times 2.1 \times 10^5 \times 8.693 \times 10^6) = -2.96 \text{ mm} = L/2026 < L/200$
Loading Q:	$w = -1.38 \times 6000^4 / (153.6 \times 2.1 \times 10^5 \times 8.693 \times 10^6) = -6.38 \text{ mm} = L/939 < L/250$

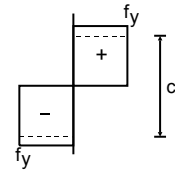
Purlin deflections, Serviceability Limit State (SLS), Is verified

9.7. Classification of cross-sections, Bending My (Purlin section)

(EN1993-1-1, §5.5)

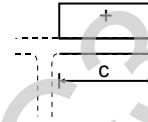
Web

$c=160.0-2 \times 7.4-2 \times 9.0=127.2$ mm, $t=5.0$ mm, $c/t=127.2/5.0=25.44$
 S 355 , $t=5.0 \leq 40$ mm, $f_y=355$ N/mm², $\epsilon=(235/355)^{0.5}=0.81$
 $c/t=25.44 \leq 72\epsilon=72 \times 0.81=58.32$
 The web is class 1 (EN1993-1-1, Tab.5.2)



Flange

$c=82.0/2-5.0/2-9.0=29.5$ mm, $t=7.4$ mm, $c/t=29.5/7.4=3.99$
 S 355 , $t=7.4 \leq 40$ mm, $f_y=355$ N/mm², $\epsilon=(235/355)^{0.5}=0.81$
 $c/t=3.99 \leq 9\epsilon=9 \times 0.81=7.29$
 The flange is class 1 (EN1993-1-1, Tab.5.2)



Overall classification of cross-section is Class 1, Bending My,ed

9.8. Resistance of cross-section, Purlin section

(EN1993-1-1, §6.2)

Ultimate Limit State, Verification for bending moment y-y

(EN1993-1-1, §6.2.5)

My.ed= 14.51 kNm

Bending Resistance $M_{ply,rd}=W_{ply} \cdot f_y / \gamma_{M0} = [10^{-6}] \times 123.90 \times 10^3 \times 355 / 1.00 = 43.98$ kNm
 $M_{y,ed} = 14.51$ kNm < 43.98 kNm = $M_{y,rd} = M_{ply,rd}$, Is verified

Ultimate Limit State, Verification for shear z

(EN1993-1-1, §6.2.6)

Vz.ed= 13.94 kNm

$A_v = A - 2b \cdot t_f + (t_w + 2r) t_f = 2009 - 2 \times 82.0 \times 7.4 + (5.0 + 2 \times 9.0) \times 7.4 = 966$ mm² (EC3 §6.2.6.3)
 $A_v = 966$ mm² > $\eta \cdot h_w \cdot t_w = 1.00 \times (160.0 - 2 \times 7.4) \times 5.0 = 1.00 \times 152.6 \times 5.0 = 763$ mm²
 Plastic Shear Resistance $V_{pl,z,rd} = A_v (f_y / \sqrt{3}) / \gamma_{M0} = [10^{-3}] \times 966 \times (355 / 1.73) / 1.00 = 197.91$ kN
 $V_{z,ed} = 13.94$ kN < 197.91 kN = $V_{z,rd} = V_{pl,z,rd}$, Is verified

$h_w / t_w = (160.0 - 2 \times 7.4) / 5.0 = 152.6 / 5.0 = 30.52 \leq 72\epsilon / \eta = 72 \times 0.81 / 1.00 = 58.32$ ($\eta = 1.00$)

S 355 , $t=5.0 \leq 40$ mm, $f_y=355$ N/mm², $\epsilon=(235/355)^{0.5}=0.81$
 Shear buckling resistance is not necessary to be verified (EC3 §6.2.6.6)

Ultimate Limit State, Verification for axial force, shear and bending

(EN1993-1-1, §6.2.9)

N.ed= 0.00kN, Vz.ed= 13.94kNm, My.ed= 14.51kN

$M_{pl,y,rd} = 43.98$ kNm, $V_{pl,z,rd} = 197.91$ kN
 $N_{ed} = 0$ kN, Effect of axial force is neglected (EC3 §6.2.9.1 Eq.6.33, Eq.6.34, Eq.6.35)
 $V_{ed} = 13.94$ kN < $0.50 \times 197.91 = 0.50 \times V_{pl,z,rd} = 98.96$ kN
 Effect of shear force is neglected (EC3 §6.2.8.2)

9.9. Lateral restraining of sheeting

(EC3 EN1993-1-3:2005, §10.1)

Sheeting thickness $t_w = 0.750$ mm, Profile depth $h_w = 40.0$ mm

Shear stiffness of sheeting

(EN1993-1-3, §10.1.1Eq.10.1b)

$s = t^{1.5} (50 + 10b^{0.33}) s / h_w = 0.750^{1.5} \times (50 + 10 \times 6000^{0.33}) \times 3000 / 40.0 = 11288$ kNm/m

Minimum required shear stiffness, for laterally restrained purlin

(§10.1.1Eq.10.1a)

$s_{min} = [\pi^2 E \cdot I_w / L^2 + G \cdot I_t + \pi^2 E \cdot I_z (h/2)^2 / L^2] \cdot 70 / h = [\pi^2 \times 2.1 \times 10^5 \times 3.959 \times 10^9 / 6000^2 + 8.1 \times 10^4 \times 0.036 \times 10^6 + \pi^2 \times 2.1 \times 10^5 \times 0.683 \times 10^6 \times 80^2 / 6000^2] \times 70 / 160^2 \times [10^{-3}] = 9272$ kNm/m
 $s = 11288$ kNm/m > 9272 kNm/m

The sheeting can be considered as sufficiently stiff to restrain the purlins

Rotational restraint given by the sheeting $C_d = 1 / (1 / C_{d,a} + 1 / C_{d,c})$ (EN1993-1-3, §10.1.5.2)

$C_{d,c} = k \cdot E \cdot I_{eff} / s$, $k = 2$, $I_{eff} = 0.3 \times 0.75 \times 39.25^2 = 347$ mm⁴/m, $s = 3000$ mm (Eq.10.16)

$C_{d,c} = [10^{-3}] \times 2 \times 2.1 \times 10^5 \times 346.6 / 3000 = 48.5$ kNm/m

$C_{d,a} = C_{100} \cdot k_{ba} \cdot k_t \cdot k_{br} \cdot k_a \cdot k_{bt}$ (EN1993-1-3, Eq.10.17)

$C_{100} = 2.0$, $k_{ba} = 1.25 \times 160 / 100 = 2.00$, $k_t = (0.75 / 0.75)^{1.5} = 1.00$, $k_{br} = 1.0$, $k_a = 1.0$, $k_{bt} = 1.0$

$C_{d,a} = 2.0 \times 2.00 \times 1.00 \times 1.0 \times 1.0 \times 1.0 = 4.0$ kNm/m

$C_d = C_{d,a} = 3.7$ kNm/m

9.10. Lateral torsional buckling (Purlin laterally restrained)

(EN1993-1-1, §6.3.2)

Elastic critical moment for lateral-torsional buckling (EC3 §6.3.2.2.2, EN1993:2002 AnnexC)
Timoshenko, S.P, Gere, J.M, Theory of elastic stability, McGraw-Hill, 1961
 $M_{cr} = C_1 \cdot [\pi^2 EI_z / (kL)^2] \{ \sqrt{[(kz/kw)^2 (I_w/I_z) + (kL)^2 G I_{t,eq} / (\pi^2 EI_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2]} - (C_2 \cdot z_g - C_3 \cdot z_j) \}$
 $G = E / (2(1+\nu)) = 210000 / (2(1+0.30)) = 80769 = 8.1 \times 10^4 \text{ N/mm}^2$, $I_{t,eq} = I_t + C_d \cdot (kL)^2 / (\pi^2 G)$

Hogging

$k \cdot L = 6000 \text{ mm}$, $z_g = -80 \text{ mm}$, $z_j = 0 \text{ mm}$ (EN1993:2002 T.C.1)

$kz = 1.0$, $k_w = 1.0$, $C_1 = 1.680$, $C_2 = 0.809$, $C_3 = 0.000$ (EN1993:2002 T.C.1)

$M_{cr} = [10^{-6}] 1.680 \times [\pi^2 \times 2.1 \times 10^5 \times 0.683 \times 10^6 / 6000^2]$

$\times \{ [1.0 \times (3.959 \times 10^9 / 0.683 \times 10^6)$

$+ 6000^2 \times 8.1 \times 10^4 \times 0.203 \times 10^6 / (\pi^2 \times 2.1 \times 10^5 \times 0.683 \times 10^6)$

$+ (-0.809 \times 80)^2]^{0.5} - (-0.809 \times 80) \} = 47.4 \text{ kNm}$

$I_{t,eq} = (0.036 \times 10^6 + 10^3 \times 3.7 \times 6000^2 / (\pi^2 \times 8.1 \times 10^4)) = 0.203 \times 10^6 \text{ mm}^4$

$\bar{\lambda}_{,lt} = \sqrt{(W_{pl,y} \cdot f_y / M_{cr})} = \sqrt{\{ [10^{-6}] \times 123.90 \times 10^3 \times 355 / 47.4 \}} = 0.963$ (EC3 Eq.6.56)

$h/b = 160/82 = 1.95 < 2.00$ buckling curve: b

imperfection factor: $\alpha_{,lt} = 0.34$, $\beta = 0.75$, $\chi_{,lt} = 0.722$ (T.6.3, T.6.5, Fig.6.4)

$\Phi_{,lt} = 0.5 [1 + \alpha_{,lt} (\bar{\lambda}_{,lt} - \bar{\lambda}_{,lt0}) + \beta \bar{\lambda}_{,lt}^2] = 0.5 \times [1 + 0.34 \times (0.963 - 0.40) + 0.75 \times 0.963^2] = 0.944$

$\chi_{,lt} = 1 / [\Phi_{,lt} + \sqrt{(\Phi_{,lt}^2 - \beta \bar{\lambda}_{,lt}^2)}] = 1 / [0.944 + \sqrt{(0.944^2 - 0.75 \times 0.944^2)}] = 0.722$

Reduction factor $\chi_{,lt} = 1 / [\Phi_{,lt} + \sqrt{(\Phi_{,lt}^2 - \beta \bar{\lambda}_{,lt}^2)}]$, $\chi_{,lt} \leq 1.0$, $1 / \bar{\lambda}_{,lt}^2$, $\chi_{,lt} = 0.722$ (Eq.6.57)

$M_{b,rd} = \chi_{,lt} \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 0.722 \times [10^{-6}] \times 123.90 \times 10^3 \times 355 / 1.00 = 31.76 \text{ kNm}$ (EC3 Eq.6.55)

$M_{y,ed} = 5.03 \text{ kNm} < 31.76 \text{ kNm} = M_{b,rd}$, Is verified

10. Global analysis

(EN1993-1-1, §5.2)

10.1. Effects of deformed geometry of the structure

(EN1993-1-1, §5.2.1)

$$\alpha_{cr} = (H_{nhf}/V_{ed}) (h/\delta_{h,ed}) \quad (\text{Eq. 5.2})$$

From elastic analysis we obtain, L.C. 202: 1.35Gk+1.50Qs1

Vertical reaction at the base of column

V_{ed} = 118.6 kN

Horizontal reaction at the base of column

H_{ed} = 75.3 kN

Axial force at rafters

N_{red} = 92.4 kN

Notional horizontal force applied at the top of the columns

H_{nhf} = 1.0 kN

Horizontal deflection at column top for notional force

δ_{h,ed} = 0.93 mm

$$\alpha_{cr} = (1.0/118.6) (5000/0.93) = 45.47 \quad (\text{Eq. 5.2})$$

Check axial compression of rafters. Axial compression is significant if

(§5.2.1, (4)B)

$$\lambda = \sqrt{(A \cdot f_y / N_{cr})} > 0.3 \sqrt{(A \cdot f_y / N_{ed})}, \quad N_{ed} > 0.09 N_{cr}$$

(§5.2.1 Eq. 5.3)

Development length of the rafter pair from column to column $L = 24000 / \cos 9.46^\circ = 24331 \text{ mm}$

$$N_{cr} = \pi^2 EI / L^2 = \pi^2 \times 210 \times 482.00 \times 10^6 / (24331)^2 = 1687.5 \text{ kN}$$

Maximum axial force in the rafters $N_{ed} = 92.4 \text{ kN}$, L.C. 202: 1.35Gk+1.50Qs1

$$\lambda = \sqrt{(11550 \times 355 / 1687502)} = 1.56 < 0.3 \sqrt{(11550 \times 355 / 92417)} = 2.00$$

Axial compression of rafters is not significant, we can use Eq. 5.2

$$\alpha_{cr} = 45.47 > 10 \quad (\text{Eq. 5.1})$$

First-order elastic analysis may be used

(§5.2.2.1)

$$\text{Amplification factor for design moments } \delta = 1 / (1 - 1/\alpha_{cr}) = 1 / (1 - 1/45.47) = 1.02 \quad (\text{Eq. 5.4})$$

10.2. Imperfections for global analysis

(EN1993-1-1, §5.3.2)

$$\varphi = \varphi_0 \cdot \alpha_h \cdot \alpha_m \cdot \delta = (1/200) \times 0.894 \times 0.866 \times 1.022 = 3.960 \times 10^{-3} = 1/253 \quad (\text{Eq. 5.5})$$

$$\varphi_0 = 1/200, \quad \alpha_h = 2/\sqrt{h} = 2/\sqrt{5.000} = 0.894 \quad 2/3 \leq \alpha_h \leq 1.0, \quad \alpha_m = \sqrt{(0.5(1+1/2))} = 0.866$$

Sway imperfection may be disregarded where $H_{ed} > 0.15 V_{ed}$

(§5.3.2 (4) Eq. 5.7)

$$\text{Effect of initial sway imperfection } H_{eq} = 3.960 \times 10^{-3} \times V_{ed} \quad (\text{§5.3.2 (5)})$$

10.3. Sway imperfections for columns

(EN1993-1-1, §5.3.2)

Reactions at the supports, Horizontal Force Hed [kN], Vertical Force Ved [kN]

		Left column 1		Right column 2		Hed1+Hed2		Ved1+Ved2		φ·Ved Heq kN
		Hed,1	Ved,1	Hed,2	Ved,2	Hed	Ved	Hed/Vhe		
201	ULS-STR	56.7	91.3	-56.7	91.3	0.0	182.6	0.00	0.362	
202	ULS-STR	75.3	118.6	-75.3	118.6	0.0	237.1	0.00	0.469	
203	ULS-STR	63.2	109.7	-63.2	91.9	0.0	201.6	0.00	0.434	
204	ULS-STR	63.2	91.9	-63.2	109.7	0.0	201.6	0.00	0.434	
205	ULS-STR	-26.0	-0.4	-1.6	0.5	-27.6	0.1	347.55	0.000	
206	ULS-STR	2.0	46.0	-23.6	25.4	-21.5	71.4	0.30	0.000	
210	ULS-STR	-33.0	-12.7	5.3	-11.9	-27.6	-24.6	1.12	0.000	
211	ULS-STR	43.6	89.8	-60.1	90.3	-16.6	180.1	0.09	0.358	
212	ULS-STR	60.4	117.6	-73.3	105.3	-12.9	222.9	0.06	0.466	
213	ULS-STR	31.5	80.9	-48.0	63.7	-16.6	144.6	0.11	0.321	
214	ULS-STR	48.3	108.7	-61.2	78.7	-12.9	187.4	0.07	0.431	
215	ULS-STR	31.5	63.2	-48.0	81.4	-16.6	144.6	0.11	0.323	
216	ULS-STR	48.3	91.0	-61.2	96.4	-12.9	187.4	0.07	0.382	
217	ULS-STR	-1.8	35.1	-25.8	36.0	-27.6	71.1	0.39	0.000	
218	ULS-STR	-7.8	30.7	-19.8	22.7	-27.6	53.4	0.52	0.000	
219	ULS-STR	-7.8	21.8	-19.8	31.5	-27.6	53.4	0.52	0.000	
220	ULS-STR	26.2	81.5	-47.8	61.0	-21.5	142.5	0.15	0.000	
221	ULS-STR	20.2	77.0	-41.7	47.6	-21.5	124.7	0.17	0.000	
222	ULS-STR	20.2	68.2	-41.7	56.5	-21.5	124.7	0.17	0.000	
231	ULS-STR	19.4	54.3	-35.9	54.8	-16.6	109.1	0.15	0.000	
232	ULS-STR	36.2	82.1	-49.1	69.8	-12.9	151.9	0.09	0.325	
233	ULS-STR	13.3	49.9	-29.9	41.5	-16.6	91.3	0.18	0.000	
234	ULS-STR	30.1	77.7	-43.0	56.5	-12.9	134.1	0.10	0.308	
235	ULS-STR	13.3	41.0	-29.9	50.4	-16.6	91.3	0.18	0.000	
236	ULS-STR	30.1	68.8	-43.0	65.4	-12.9	134.1	0.10	0.272	
251	ULS-STR	39.6	82.8	-56.2	83.3	-16.6	166.1	0.10	0.330	
252	ULS-STR	56.4	110.6	-69.3	98.3	-12.9	208.9	0.06	0.438	
253	ULS-STR	27.5	73.9	-44.1	56.6	-16.6	130.5	0.13	0.293	
254	ULS-STR	44.3	101.7	-57.2	71.6	-12.9	173.3	0.07	0.403	
255	ULS-STR	27.5	56.1	-44.1	74.4	-16.6	130.5	0.13	0.295	
256	ULS-STR	44.3	83.9	-57.2	89.4	-12.9	173.3	0.07	0.354	
257	ULS-STR	-5.8	28.1	-21.9	28.9	-27.6	57.0	0.48	0.000	
258	ULS-STR	-11.8	23.7	-15.8	15.6	-27.6	39.3	0.70	0.000	
259	ULS-STR	-11.8	14.8	-15.8	24.5	-27.6	39.3	0.70	0.000	
260	ULS-STR	22.3	74.4	-43.8	53.9	-21.5	128.4	0.17	0.000	
261	ULS-STR	16.2	70.0	-37.7	40.6	-21.5	110.6	0.19	0.000	
262	ULS-STR	16.2	61.1	-37.7	49.5	-21.5	110.6	0.19	0.000	

10.4. Internal forces and bending moments with imperfection effect

10.5. Axial forces Ned [kN]

L.C.	Axial forces Ned [kN]				
	Left column 1 Ned,1	Left rafter 2 Ned,2	Right rafter 3 Ned,3	Right column 4 Ned,4	
201	ULS-STR	-87.2	-62.9	-62.9	-87.3
202	ULS-STR	-114.4	-83.5	-83.5	-114.6
203	ULS-STR	-105.5	-70.1	-70.1	-88.0
204	ULS-STR	-87.8	-70.1	-70.1	-105.7
205	ULS-STR	4.4	-5.1	-5.3	3.6
206	ULS-STR	-41.9	-31.5	-28.2	-21.4
210	ULS-STR	15.7	2.6	2.4	14.9
211	ULS-STR	-85.7	-68.7	-68.8	-86.3
212	ULS-STR	-113.5	-84.6	-82.6	-101.4
213	ULS-STR	-76.8	-55.3	-55.4	-59.7
214	ULS-STR	-104.6	-71.2	-69.2	-74.7
215	ULS-STR	-59.1	-55.3	-55.4	-77.5
216	ULS-STR	-86.9	-71.2	-69.2	-92.5
217	ULS-STR	-31.1	-31.9	-32.1	-31.9
218	ULS-STR	-26.6	-25.2	-25.4	-18.6
219	ULS-STR	-17.8	-25.2	-25.4	-27.5
220	ULS-STR	-77.4	-58.3	-55.0	-56.9
221	ULS-STR	-73.0	-51.6	-48.3	-43.6
222	ULS-STR	-64.1	-51.6	-48.3	-52.5
231	ULS-STR	-50.2	-41.8	-41.9	-50.8
232	ULS-STR	-78.0	-57.7	-55.7	-65.8
233	ULS-STR	-45.8	-35.1	-35.2	-37.4
234	ULS-STR	-73.6	-51.0	-49.0	-52.5
235	ULS-STR	-36.9	-35.1	-35.2	-46.3
236	ULS-STR	-64.7	-51.0	-49.0	-61.4
251	ULS-STR	-79.3	-64.3	-64.4	-79.9
252	ULS-STR	-107.0	-80.2	-78.2	-94.9
253	ULS-STR	-70.4	-50.9	-51.0	-53.3
254	ULS-STR	-98.2	-66.8	-64.8	-68.3
255	ULS-STR	-52.6	-50.9	-51.0	-71.0
256	ULS-STR	-80.4	-66.7	-64.7	-86.0
257	ULS-STR	-24.6	-27.5	-27.7	-25.5
258	ULS-STR	-20.2	-20.8	-21.0	-12.2
259	ULS-STR	-11.3	-20.8	-21.0	-21.1
260	ULS-STR	-71.0	-53.9	-50.6	-50.5
261	ULS-STR	-66.6	-47.2	-43.9	-37.2
262	ULS-STR	-57.7	-47.2	-43.9	-46.0

10.6. Shearing forces Ved [kN]

L.C.		Left column 1		Left rafter 2			Right rafter 3			Right column 4	
		VedA,1	VedB,1	VedA,2	VedC,2	VedB,2	VedA,3	VedC,3	VedB,3	VedA,4	VedB,4
201	ULS-STR	-56.5	-56.5	72.7	56.5	-9.4	9.3	-56.6	-72.8	56.9	56.9
202	ULS-STR	-75.0	-75.0	96.4	75.0	-12.5	12.3	-75.1	-96.6	75.5	75.5
203	ULS-STR	-62.9	-62.9	89.7	68.2	-19.3	1.6	-57.8	-72.3	63.4	63.4
204	ULS-STR	-62.9	-62.9	72.2	57.6	-1.7	19.1	-68.4	-89.9	63.4	63.4
205	ULS-STR	26.0	-2.3	-10.0	-8.6	-2.9	-2.3	6.9	9.2	-10.5	1.6
206	ULS-STR	-2.0	-30.4	32.6	23.2	-15.1	-6.2	-11.1	-12.3	11.4	23.6
210	ULS-STR	33.0	4.6	-18.9	-15.5	-1.8	-3.4	13.8	18.1	-17.5	-5.3
211	ULS-STR	-43.4	-60.4	69.8	53.7	-11.6	8.3	-54.9	-70.5	53.0	60.3
212	ULS-STR	-60.1	-77.1	95.3	72.8	-18.9	5.9	-65.8	-83.4	66.2	73.5
213	ULS-STR	-31.3	-48.3	63.0	47.0	-18.3	-2.4	-37.5	-46.2	40.9	48.2
214	ULS-STR	-48.0	-65.0	88.6	66.0	-25.7	-4.8	-48.4	-59.1	54.1	61.4
215	ULS-STR	-31.3	-48.3	45.5	36.4	-0.8	15.1	-48.1	-63.7	40.9	48.2
216	ULS-STR	-48.1	-65.1	71.1	55.4	-8.1	12.7	-59.0	-76.6	54.1	61.4
217	ULS-STR	1.8	-26.6	21.1	15.5	-6.9	1.7	-17.2	-21.9	13.7	25.8
218	ULS-STR	7.8	-20.5	17.7	12.2	-10.3	-3.7	-8.6	-9.8	7.6	19.8
219	ULS-STR	7.8	-20.5	8.9	6.9	-1.5	5.1	-13.9	-18.5	7.6	19.8
220	ULS-STR	-26.2	-54.6	63.7	47.3	-19.1	-2.2	-35.3	-43.4	35.6	47.8
221	ULS-STR	-20.2	-48.5	60.3	43.9	-22.4	-7.6	-26.6	-31.3	29.6	41.7
222	ULS-STR	-20.2	-48.5	51.5	38.6	-13.7	1.2	-31.9	-40.0	29.6	41.7
231	ULS-STR	-19.4	-36.4	38.8	29.7	-7.5	4.4	-30.7	-39.3	28.6	35.9
232	ULS-STR	-36.0	-53.0	64.3	48.7	-14.9	2.0	-41.6	-52.3	41.9	49.2
233	ULS-STR	-13.3	-30.3	35.5	26.3	-10.9	-1.0	-22.0	-27.2	22.6	29.9
234	ULS-STR	-29.9	-47.0	60.9	45.3	-18.3	-3.4	-32.9	-40.2	35.9	43.2
235	ULS-STR	-13.3	-30.3	26.7	21.0	-2.1	7.8	-27.3	-36.0	22.6	29.9
236	ULS-STR	-30.0	-47.0	52.2	40.0	-9.5	5.4	-38.2	-48.9	35.9	43.2
251	ULS-STR	-39.4	-56.4	64.7	49.8	-10.9	7.7	-50.9	-65.3	49.0	56.3
252	ULS-STR	-56.1	-73.2	90.2	68.8	-18.2	5.3	-61.8	-78.3	62.2	69.5
253	ULS-STR	-27.3	-44.3	57.9	43.0	-17.7	-3.1	-33.6	-41.0	36.9	44.2
254	ULS-STR	-44.1	-61.1	83.5	62.1	-25.0	-5.5	-44.4	-54.0	50.1	57.4
255	ULS-STR	-27.3	-44.3	40.4	32.4	-0.2	14.4	-44.2	-58.6	36.9	44.2
256	ULS-STR	-44.1	-61.1	66.0	51.5	-7.5	12.1	-55.0	-71.5	50.1	57.4
257	ULS-STR	5.8	-22.6	16.0	11.6	-6.3	1.0	-13.3	-16.8	9.7	21.9
258	ULS-STR	11.8	-16.5	12.6	8.2	-9.7	-4.3	-2.9	-4.6	3.7	15.8
259	ULS-STR	11.8	-16.5	3.8	2.9	-0.9	4.4	-9.9	-13.4	3.7	15.8
260	ULS-STR	-22.3	-50.6	58.5	43.4	-18.4	-2.9	-31.3	-38.3	31.6	43.8
261	ULS-STR	-16.2	-44.6	55.2	40.0	-21.8	-8.3	-22.6	-26.2	25.6	37.7
262	ULS-STR	-16.2	-44.6	46.4	34.7	-13.0	0.5	-27.9	-34.9	25.6	37.7

A:left end, C:haunch end, B: right end

10.7. Bending moments Med [kNm]

L.C.		Left column 1			Right column 4	
		MedA,1	MedM,1	MedB,1	MedA,4	MedM,4
201	ULS-STR	0.0	-141.3	-282.5	-284.3	-142.2
202	ULS-STR	0.0	-187.5	-375.0	-377.4	-188.7
203	ULS-STR	0.0	-157.3	-314.6	-316.8	-158.4
204	ULS-STR	0.0	-157.3	-314.6	-316.8	-158.4
205	ULS-STR	0.0	59.6	59.1	22.2	-0.5
206	ULS-STR	0.0	-40.5	-81.1	-87.4	-43.7
210	ULS-STR	0.0	47.0	94.0	57.1	28.5
211	ULS-STR	0.0	-129.6	-259.3	-283.2	-141.6
212	ULS-STR	0.0	-171.5	-343.1	-349.2	-174.6
213	ULS-STR	0.0	-99.4	-198.9	-222.6	-111.3
214	ULS-STR	0.0	-141.3	-282.7	-288.6	-144.3
215	ULS-STR	0.0	-99.4	-198.9	-222.6	-111.3
216	ULS-STR	0.0	-141.4	-282.8	-288.5	-144.3
217	ULS-STR	0.0	0.3	-61.9	-98.8	-49.4
218	ULS-STR	0.0	5.4	-31.7	-68.5	-34.3
219	ULS-STR	0.0	5.4	-31.7	-68.5	-34.3
220	ULS-STR	0.0	-101.1	-202.1	-208.5	-104.2
221	ULS-STR	0.0	-85.9	-171.9	-178.2	-89.1
222	ULS-STR	0.0	-85.9	-171.9	-178.2	-89.1
231	ULS-STR	0.0	-69.6	-139.3	-161.4	-80.7
232	ULS-STR	0.0	-111.2	-222.5	-227.9	-114.0
233	ULS-STR	0.0	-54.5	-109.0	-131.2	-65.6
234	ULS-STR	0.0	-96.1	-192.3	-197.6	-98.8
235	ULS-STR	0.0	-54.5	-109.0	-131.2	-65.6
236	ULS-STR	0.0	-96.2	-192.4	-197.5	-98.8
251	ULS-STR	0.0	-119.7	-239.5	-263.3	-131.6
252	ULS-STR	0.0	-161.6	-323.3	-329.3	-164.6
253	ULS-STR	0.0	-89.5	-179.1	-202.7	-101.3
254	ULS-STR	0.0	-131.4	-262.9	-268.7	-134.3
255	ULS-STR	0.0	-89.5	-179.1	-202.7	-101.3
256	ULS-STR	0.0	-131.5	-263.0	-268.6	-134.3
257	ULS-STR	0.0	2.9	-42.0	-78.9	-39.5
258	ULS-STR	0.0	12.3	-11.8	-48.6	-24.3
259	ULS-STR	0.0	12.3	-11.8	-48.6	-24.3
260	ULS-STR	0.0	-91.1	-182.2	-188.6	-94.3
261	ULS-STR	0.0	-76.0	-152.0	-158.3	-79.2
262	ULS-STR	0.0	-76.0	-152.0	-158.3	-79.2

A:left end, B: right end

L.C.	MedA,2	Left rafter 2			Right rafter 3			MedB,3	
		MedC2	MedM,2	MedB,2	MedA,3	MedM,3	MedC3		
201	ULS-STR	-282.5	-127.6	108.7	102.1	102.1	108.5	-129.0	-284.3
202	ULS-STR	-375.0	-169.3	144.3	135.6	135.6	144.0	-171.2	-377.4
203	ULS-STR	-314.6	-125.1	134.5	113.8	113.8	114.0	-160.6	-316.8
204	ULS-STR	-314.6	-158.9	114.0	113.8	113.8	134.1	-126.9	-316.8
205	ULS-STR	59.1	36.8	19.8	-19.6	-19.6	-22.3	3.0	22.2
206	ULS-STR	-81.1	-14.1	54.5	25.5	25.5	-31.0	-59.2	-87.4
210	ULS-STR	94.0	52.6	30.9	-32.1	-32.1	-35.5	18.7	57.1
211	ULS-STR	-259.3	-111.0	104.9	94.8	94.8	100.1	-132.8	-283.2
212	ULS-STR	-343.1	-141.3	140.8	121.8	121.8	124.2	-170.3	-349.2
213	ULS-STR	-198.9	-66.8	98.2	73.0	73.0	-74.8	-122.2	-222.6
214	ULS-STR	-282.7	-97.2	135.0	100.0	100.0	-94.3	-159.7	-288.6
215	ULS-STR	-198.9	-100.6	73.1	73.0	73.0	90.6	-88.4	-222.6
216	ULS-STR	-282.8	-131.0	105.1	100.0	100.0	111.0	-125.9	-288.5
217	ULS-STR	-61.9	-18.0	34.5	24.1	24.1	24.8	-51.8	-98.8
218	ULS-STR	-31.7	4.1	36.3	13.2	13.2	-27.7	-46.6	-68.5
219	ULS-STR	-31.7	-12.7	14.6	13.2	13.2	19.8	-29.7	-68.5
220	ULS-STR	-202.1	-68.9	95.8	69.1	69.1	-69.7	-114.1	-208.5
221	ULS-STR	-171.9	-46.8	95.3	58.2	58.2	-60.0	-108.8	-178.2
222	ULS-STR	-171.9	-63.7	75.7	58.2	58.2	58.4	-91.9	-178.2
231	ULS-STR	-139.3	-57.0	58.7	51.3	51.3	54.0	-77.3	-161.4
232	ULS-STR	-222.5	-86.9	95.2	78.2	78.2	78.6	-115.2	-227.9
233	ULS-STR	-109.0	-34.9	56.0	40.4	40.4	-45.4	-72.1	-131.2
234	ULS-STR	-192.3	-64.8	92.9	67.3	67.3	-65.2	-109.9	-197.6
235	ULS-STR	-109.0	-51.8	41.3	40.4	40.4	48.8	-55.2	-131.2
236	ULS-STR	-192.4	-81.7	76.2	67.3	67.3	70.5	-93.0	-197.5
251	ULS-STR	-239.5	-102.1	97.3	87.7	87.7	92.5	-123.7	-263.3
252	ULS-STR	-323.3	-132.4	133.3	114.6	114.6	116.7	-161.2	-329.3
253	ULS-STR	-179.1	-57.9	91.0	65.8	65.8	-68.4	-113.1	-202.7
254	ULS-STR	-262.9	-88.2	127.9	92.8	92.8	-87.9	-150.6	-268.7
255	ULS-STR	-179.1	-91.6	65.8	65.8	65.8	83.2	-79.4	-202.7
256	ULS-STR	-263.0	-122.1	97.4	92.8	92.8	103.4	-116.8	-268.6
257	ULS-STR	-42.0	-9.0	27.7	16.9	16.9	17.3	-42.8	-78.9
258	ULS-STR	-11.8	13.2	31.5	6.0	6.0	-21.3	-37.9	-48.6
259	ULS-STR	-11.8	-3.7	7.0	6.0	6.0	12.7	-20.7	-48.6
260	ULS-STR	-182.2	-59.9	88.7	61.9	61.9	-63.3	-105.0	-188.6
261	ULS-STR	-152.0	-37.8	88.6	51.0	51.0	-53.6	-99.8	-158.3
262	ULS-STR	-152.0	-54.7	68.4	51.0	51.0	51.1	-82.9	-158.3

A:left end, C:haunch end, M: span, B: right end

SteelPortalFrameEFC3
Example Report

11. Serviceability Limit State (SLS)

(EN1993-1-1, §7)

11.1. Vertical deflection at the apex

(EN1993-1-1, §7.2.1)

Maximum vertical deflection, L.C. 302: Gk+Qs1 Dy= 44 mm=24000/545=L/545
Vertical deflection due to imposed load only Dy= 17 mm=24000/889=L/1412
Vertical deflection due to snow only Dy= 27 mm=24000/889=L/889
Limit for vertical deflection L/200, Is verified

11.2. Horizontal deflection at the top of column

(EN1993-1-1, §7.2.2)

Maximum horizontal deflection, L.C. 304: Gk+Qs3 Dx= 8 mm= 5000/625=h/625
Horizontal deflection due to wind only Dx= 6 mm= 5000/833=h/833
Limit for horizontal deflection H/150, Is verified

11.3. Dynamic effects

(EN1993-1-1, §7.2.3)

Eigenfrequencies and Eigenperiods of the structure

Mass of building, for loading: L.C. 601: Gk + 0.20Qs1

1	f=	2.616 Hz	T=	0.382 sec
2	f=	3.896 Hz	T=	0.257 sec
3	f=	10.732 Hz	T=	0.093 sec
4	f=	29.103 Hz	T=	0.034 sec
5	f=	42.721 Hz	T=	0.023 sec
6	f=	59.397 Hz	T=	0.017 sec
7	f=	112.457 Hz	T=	0.009 sec
8	f=	149.552 Hz	T=	0.007 sec
9	f=	153.281 Hz	T=	0.007 sec

12. Column verification (Ultimate Limit State)

(EN1993-1-1, §6)

Profile : IPE 600-S 355

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

N_{ed} = 118.7 kNV_{ed} = 75.5 kNM_{yed} = 377.4 kNm, M_{zed} = 0.0 kNmM_{yed} = 320.8 kNm (Column top under the haunch)Buckling length, In-plane buckling L_{cr,y} = 5000mm (System length) (EC3 §5.5.2.(7))Buckling length, Out-of-plane buckling L_{cr,z} = 4250mm (Column height without haunch)Buckling length, Torsional buckling L_{cr,t} = 4250mmBuckling length, Lateral torsional buckling L_{cr,lt} = 4250mm**12.1. Classification of cross-sections, Column**

(EN1993-1-1, §5.5)

Maximum and minimum cross-section stresses $\sigma = N_{ed}/A_e1 \pm M_{yed}/W_{el,y} \pm M_{zed}/W_{el,z}$ $\sigma = [10^{-3}]119/15600 \pm [10^{-6}]377/3069.0 \times 10^3 \pm [10^{-6}]0/307.9 \times 10^3$ $\sigma_1 = 131 \text{ N/mm}^2$, $\sigma_2 = -115 \text{ N/mm}^2$ (compression positive)Web

c = 600.0 - 2x19.0 - 2x24.0 = 514.0 mm, t = 12.0 mm, c/t = 514.0/12.0 = 42.83

S 355, t = 12.0 ≤ 40 mm, f_y = 355 N/mm², ε = (235/355)^{0.5} = 0.81

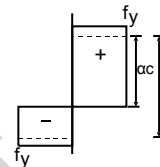
Position of neutral axis for combined Bending and compression

N_{ed} / (2t_w · f_y / γ_{M0}) = 118700 / (2x12.0x355/1.00) = 13.9 mm

α = (514.0/2 + 13.9) / 514.0 = 0.527 > 0.5

c/t = 42.83 ≤ 396x0.81 / (13x0.527 - 1) = 54.81

The web is class 1 (EN1993-1-1, Tab.5.2)

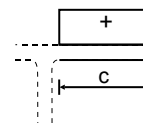
Flange

c = 220.0/2 - 12.0/2 - 24.0 = 80.0 mm, t = 19.0 mm, c/t = 80.0/19.0 = 4.21

S 355, t = 19.0 ≤ 40 mm, f_y = 355 N/mm², ε = (235/355)^{0.5} = 0.81

c/t = 4.21 ≤ 9ε = 9x0.81 = 7.29

The flange is class 1 (EN1993-1-1, Tab.5.2)

Overall classification of cross-section is Class 1, Bending and compression N_{c,ed} + M_{y,ed}**12.2. Resistance of cross-section, Column (Ultimate Limit State)**

(EN1993-1-1, §6.2)

Ultimate Limit State, Verification for compression

(EN1993-1-1, §6.2.4)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

N_{c,ed} = 118.70 kNCompression Resistance N_{pl,rd} = A · f_y / γ_{M0} = [10⁻³]x15600x355/1.00 = 5538.00 kNN_{ed} = 118.70 kN < 5538.00 kN = N_{c,rd} = N_{pl,rd}, Is verifiedUltimate Limit State, Verification for bending moment y-y

(EN1993-1-1, §6.2.5)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

M_{y,ed} = 377.40 kNmBending Resistance M_{pl,y,rd} = W_{pl,y} · f_y / γ_{M0} = [10⁻⁶]x3512.0x10³x355/1.00 = 1246.76 kNmM_{y,ed} = 377.40 kNm < 1246.76 kNm = M_{y,rd} = M_{pl,y,rd}, Is verifiedUltimate Limit State, Verification for shear z

(EN1993-1-1, §6.2.6)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

V_{z,ed} = 77.10 kNA_v = A - 2b · t_f + (t_w + 2r) t_f = 15600 - 2x220.0x19.0 + (12.0 + 2x24.0)x19.0 = 8380 mm² (EC3 §6.2.6.3)A_v = 8380 mm² > η · h_w · t_w = 1.00x(600.0 - 2x19.0)x12.0 = 1.00x581.0x12.0 = 6972 mm²Plastic Shear Resistance V_{pl,z,rd} = A_v (f_y / √3) / γ_{M0} = [10⁻³]x8380x(355/1.73) / 1.00 = 1717.56 kNV_{z,ed} = 77.10 kN < 1717.56 kN = V_{z,rd} = V_{pl,z,rd}, Is verifiedh_w / t_w = (600.0 - 2x19.0) / 12.0 = 581.0 / 12.0 = 48.42 ≤ 72x0.81 / 1.00 = 72ε / η = 58.32 (η = 1.00)S 355, t = 12.0 ≤ 40 mm, f_y = 355 N/mm², ε = (235/355)^{0.5} = 0.81

Shear buckling resistance is not necessary to be verified

(EC3 §6.2.6.6)

Ultimate Limit State, Verification for axial force, shear and bending (EN1993-1-1, §6.2.9)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

N.ed= 118.70kN (Compression), Vz.ed= 75.50kNm, My.ed= 377.40kNm

Nplrd=5538.00kN, Mpl,y,rd=1246.76kNm, Vpl,z,rd=1717.56kN

Ned=118.70kN <= 0.25x5538.00=0.25xNplrd=1384.50kN

Ned=118.70kN <= [10⁻³]x0.5x581.0x12.0x355/1.00=0.5hw·tw·fy/γM0=1237.53 kN

n=Ned/Nplrd=119/5538= 0.021

Effect of axial force is neglected (EC3 §6.2.9.1 Eq.6.33, Eq.6.34, Eq.6.35)

Ved=75.50kN <= 0.50x1717.56=0.50xVpl,rd=858.78kN

Effect of shear force is neglected (EC3 §6.2.8.2)

My,ed= 377.40 kNm < 1246.76 kNm =Mply,rd, Is verified

12.3. Flexural Buckling, Column (Ultimate Limit State) (EN1993-1-1, §6.3.1)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

Buckling lengths: Lcr,y=1.000x5000=5000mm, Lcr,z=0.850x5000=4250mm

Non-dimensional slenderness (Cross-section Class: 1) (EC3 §6.3.1.3)

$\bar{\lambda}_y = \sqrt{(A \cdot f_y / N_{cr,y})} = (L_{cr,y} / i_y) \cdot (1 / \lambda_1) = (5000 / 243.0) \cdot (1 / 76.06) = 0.271$

$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \cdot (1 / \lambda_1) = (4250 / 46.6) \cdot (1 / 76.06) = 1.199$

$\lambda_1 = \pi \sqrt{(E / f_y)} = 93.9 \epsilon = 76.06, \epsilon = \sqrt{(235 / f_y)} = 0.81$

h/b=600/220=2.73>=1.20, tf=19.0mm<=40 mm

y-y buckling curve:a, imperfection factor:αy=0.21, χy=0.984 (T.6.2, T.6.1, Fig.6.4)

Φy=0.5[1+αy(λ̄y-0.2)+λ̄y²]=0.5x[1+0.21x(0.271-0.2)+0.271²]=0.544

χy=1/[Φy+√(Φy²-λ̄y²)]=1/[0.544+√(0.544²-0.271²)]=0.984 <=1 χy=0.984

z-z buckling curve:b, imperfection factor:αz=0.34, χz=0.479

Φz=0.5[1+αz(λ̄z-0.2)+λ̄z²]=0.5x[1+0.34x(1.199-0.2)+1.199²]=1.389

χz=1/[Φz+√(Φz²-λ̄z²)]=1/[1.389+√(1.389²-1.199²)]=0.479 <=1 χz=0.479

Reduction factor χ=1/[Φ+√(Φ²-λ̄²)], χ<=1.0, Φ=0.5[1+α(λ̄-0.2)+λ̄²], χ=0.479 (EC3 Eq.6.49)

Nb,rd=χ·A·fy/γM1= 0.479x[10⁻³]x15600x355/1.00=2652.70kN (EC3 Eq.6.47)

Nc,ed= 118.70 kN < 2652.70 kN =Nb,rd, Is verified

12.4. Lateral torsional buckling, Column (EN1993-1-1, §6.3.2)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

Elastic critical moment for lateral-torsional buckling (EC3 §6.3.2.2.2, EN1993:2002 AnnexC)

Timoshenko, S.P, Gere, J.M, Theory of elastic stability, McGraw-Hill, 1961

$M_{cr} = C_1 \cdot [\pi^2 EI_z / (kL)^2] \cdot \{ \sqrt{[(k_z/k_w)^2 (I_w/I_z) + (kL)^2 GI_t / (\pi^2 EI_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2]} - (C_2 \cdot z_g - C_3 \cdot z_j) \}$

G=E/(2(1+ν))=210000/(2(1+0.30))=80769=8.1x10⁴ N/mm²

k·L=4250mm, zg=h/2=600/2=300mm, zj=0mm (EN1993:2002 T.C.1)

kz=1.0, kw=1.0, ψ=0.000, C1=1.847, C2=0.000, C3=0.000 (EN1993:2002 T.C.1)

$M_{cr} = [10^{-6}] 1.847 \times [\pi^2 \times 2.1 \times 10^5 \times 33.870 \times 10^6 / 4250^2]$

$\times \{ [1.0 \times (2845.5 \times 10^9 / 33.870 \times 10^6)]$

$+ 4250^2 \times 8.1 \times 10^4 \times 1.654 \times 10^6 / (\pi^2 \times 2.1 \times 10^5 \times 33.870 \times 10^6)]^{0.5} \} = 2469.9 \text{ kNm}$

$\bar{\lambda}_{lt} = \sqrt{(W_{pl,y} \cdot f_y / M_{cr})} = \sqrt{([10^{-6}] \times 3512.0 \times 10^3 \times 355 / 2469.9)} = 0.710$ (EC3 Eq.6.56)

h/b=600/220=2.73>2.00 buckling curve:c

imperfection factor:αlt=0.49, β=0.75, χlt=0.819 (T.6.3, T.6.5, Fig.6.4)

Φlt=0.5[1+αlt(λ̄lt-0.4)+βλ̄lt²]=0.5x[1+0.49x(0.710-0.4)+0.75x0.710²]=0.765

χlt=1/[Φlt+√(Φlt²-βλ̄lt²)]=1/[0.765+√(0.765²-0.75x0.765²)]=0.819

Reduction factor χlt=1/[Φlt+√(Φlt²-βλ̄lt²)], χlt<=1.0, 1/λ̄lt², χlt=0.819 (Eq.6.57)

χlt,mod=χlt/f, χlt,mod<=1, χlt,mod<=1/λ̄lt²=1/0.710²=1.98 (EC3 §6.3.2.3(2), Eq.6.58)

Kc=1/(1.33-0.33ψ)=0.752, ψ=0.00 (EC3 Tab.6.6)

f=1-0.5(1-kc)[1-2.0(λ̄lt-0.8)²]=1-0.5x(1-0.752)[1-2.0x(0.710-0.8)²]=0.878, f<=1.0

χlt,mod=χlt/f=0.819/0.878=0.933, χlt,mod<=1.0, χlt,mod<=1.98, χlt,mod=0.933

Mb,rd=χlt·Wpl,y·fy/γM1= 0.933x[10⁻⁶]x3512.0x10³x355/1.00=1163.23kNm (EC3 Eq.6.55)

My,ed= 320.77 kNm < 1163.23 kNm =Mb,rd, Is verified

12.5. Axial force and bending moment, Column

(EN1993-1-1, §6.3.3)

$$\begin{aligned} \text{Ned}/(\chi_y \cdot \text{Nr}k/\gamma_{M1}) + k_{yy} \cdot \text{My,ed}/(\chi_{LT} \cdot \text{My,rk}/\gamma_{M1}) &\leq 1 && \text{(EC3 Eq.6.61)} \\ \text{Ned}/(\chi_z \cdot \text{Nr}k/\gamma_{M1}) + k_{zy} \cdot \text{My,ed}/(\chi_{LT} \cdot \text{My,rk}/\gamma_{M1}) &\leq 1 && \text{(EC3 Eq.6.62)} \\ \text{Nr}k = A \cdot f_y = [10^{-3}] \times 15600 \times 355 = 5538.0 \text{ kN} &&& \text{(Tab.6.7)} \\ \text{My,rk} = W_{pl,y} \cdot f_y = [10^{-6}] \times 3512.0 \times 10^3 \times 355 = 1246.8 \text{ kNm} \\ \chi_y \cdot \text{Nr}k/\gamma_{M1} = \chi_y \cdot A \cdot f_y/\gamma_{M1} = 0.984 \times [10^{-3}] \times 15600 \times 355/1.00 = 5449.4 \text{ kN} \\ \chi_z \cdot \text{Nr}k/\gamma_{M1} = \chi_z \cdot A \cdot f_y/\gamma_{M1} = 0.479 \times [10^{-3}] \times 15600 \times 355/1.00 = 2652.7 \text{ kN} \\ \chi_{LT} \cdot \text{My,rk}/\gamma_{M1} = \chi_{LT} \cdot W_{pl,y} \cdot f_y/\gamma_{M1} = 0.933 \times [10^{-6}] \times 3512.0 \times 10^3 \times 355/1.00 = 1163.2 \text{ kNm} \end{aligned}$$

Interaction factors, Method of computation: Method 1 Annex A

(EC3 AnnexA)

$$\begin{aligned} k_{yy} &= C_{mLT}(\mu_y / (1 - \text{Ned}/\text{Ncr}_y)) / (1 - C_{yy}), \quad \mu_y = (1 - \text{Ned}/\text{Ncr}_y) / (1 - \chi_y \cdot \text{Ned}/\text{Ncr}_y) && \text{(EC3 Tab.A.1)} \\ k_{zy} &= C_{mLT}(\mu_z / (1 - \text{Ned}/\text{Ncr}_y)) / (1 - C_{zy}) \cdot 0.60 \sqrt{w_y/w_z}, \quad \mu_z = (1 - \text{Ned}/\text{Ncr}_z) / (1 - \chi_z \cdot \text{Ned}/\text{Ncr}_z) \end{aligned}$$

$$\begin{aligned} \text{Ncr}_y &= \pi^2 EI_y / l_{cr,y}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 920.80 \times 10^6 / 5000^2 = 76339 \text{ kN} \\ \text{Ncr}_z &= \pi^2 EI_z / l_{cr,z}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 33.870 \times 10^6 / 4250^2 = 3886 \text{ kN} \\ \text{Ncr}_t &= (1 / i_p^2) \times (G \cdot I_t + \pi^2 EI_w / L_{cr,t}^2) && \text{(EC3 NCCI SN003b-EN-EU)} \\ \text{Ncr}_t &= [10^{-3}] \times (1 / 247^2) [80769 \times 1.654 \times 10^6 + \pi^2 \times 210000 \times 2845.5 \times 10^9 / 4250^2] = 7519 \text{ kN} \end{aligned}$$

$$\begin{aligned} \mu_y &= (1 - \text{Ned}/\text{Ncr}_y) / (1 - \chi_y \cdot \text{Ned}/\text{Ncr}_y) = (1 - 118.7 / 76339) / (1 - 0.984 \times 118.7 / 76339) = 1.000 \\ \mu_z &= (1 - \text{Ned}/\text{Ncr}_z) / (1 - \chi_z \cdot \text{Ned}/\text{Ncr}_z) = (1 - 118.7 / 3886) / (1 - 0.479 \times 118.7 / 3886) = 0.984 \\ \text{alt} &= 1 - I_t / I_y \geq 0 = 1 - 1.654 \times 10^6 / 920.80 \times 10^6 = 0.998 && \text{(EC3 Annex A.1)} \end{aligned}$$

$$\begin{aligned} w_y &= W_{pl,y} / W_{el,y} \leq 1.50, \quad w_y = 3.512 \times 10^6 / 3.069 \times 10^6 = 1.144 \leq 1.50 && \text{(EC3 Annex A.1)} \\ w_z &= W_{pl,z} / W_{el,z} \leq 1.50, \quad w_z = 0.486 \times 10^6 / 0.308 \times 10^6 = 1.577 > 1.50, \quad w_z = 1.50 \\ n_{pl} &= \text{Ned} / (\text{Nr}k/\gamma_{M1}) = 118.70 / (5538.00 / 1.00) = 0.021 \end{aligned}$$

$$\bar{\lambda}_{\max} = \max(0.271, 1.199) = 1.200 \quad \text{(EC3 Annex A.1)}$$

$$\begin{aligned} C_{m,0} &= (1.00 / 1.85) \times 2469.90 = 1337.3, \quad C_1 = 1.00 \\ \bar{\lambda}_0 &= \sqrt{([10^{-6}] \times 3512.0 \times 10^3 \times 355 / 1337.3)} = 0.970 \\ \bar{\lambda}_0, \text{lim} &= 0.2 \sqrt{C_1} [(1 - \text{Ned}/\text{Ncr}_z) (1 - \text{Ned}/\text{Ncr}_t)]^{0.25} && \text{(EC3 Annex A.1)} \\ \bar{\lambda}_0, \text{lim} &= 0.2 \sqrt{1.847} [(1 - 118.7 / 3886) (1 - 118.7 / 7519)]^{0.25} = 0.269 \\ \epsilon_y &= (\text{My,ed}/\text{Ned}) (A / W_{el}) = ([10^3] \times 320.77 / 118.70) \times (15600.0 / 3069.0 \times 10^3) = 13.74 \end{aligned}$$

$$\begin{aligned} C_{m,y,0} &= 0.79 + 0.21\psi + 0.36(\psi - 0.33) \times (118.70 / 76339.0) = 0.790, \quad (\psi = 0.00) && \text{(EC3 Annex A, T.A.1)} \\ \bar{\lambda}_0 &= 0.970 > \bar{\lambda}_0, \text{lim} = 0.269 \\ C_{m,y} &= C_{m,y,0} + (1 - C_{m,y,0}) (\sqrt{\epsilon_y \cdot \text{alt}}) / (1 + \sqrt{\epsilon_y \cdot \text{alt}}) = \\ &= 0.790 + (1 - 0.790) \times (\sqrt{13.736 \times 0.998}) / (1 + \sqrt{13.736 \times 0.998}) = 0.955 \\ C_{mLT} &= C_{m,y} \cdot \text{alt} / \sqrt{[(1 - \text{Ned}/\text{Ncr}_z) (1 - \text{Ned}/\text{Ncr}_t)]} \geq 1 \\ C_{mLT} &= 0.955^2 \times 0.998 / \sqrt{[(1 - 118.7 / 3886.0) (1 - 118.7 / 7519.0)]} = 0.932, \quad C_{mLT} = 1.000 \end{aligned}$$

$$\begin{aligned} C_{yy} &= 1 + (w_y - 1) [(2 - 1.6 C_{m,y}^2 \cdot \bar{\lambda}_{\max} / w_y - 1.6 C_{m,y}^2 \cdot \bar{\lambda}_{\max}^2 / w_y) n_{pl} - b_{LT}] \geq W_{el,y} / W_{pl,y} && \text{(Annex A, T.A.1)} \\ b_{LT} &= 0.5 \text{alt} \cdot \bar{\lambda}_0^2 [\text{My,ed} / (\chi_{LT} \cdot M_{pl,y,rd})] (M_{z,ed} / M_{pl,z,rd}) = \\ &= 0.5 \times 0.998 \times 0.970^2 [320.8 / (0.933 \times 1089.5)] (0.0 / 109.3) = 0.000 \\ C_{yy} &= 1 + (1.144 - 1) [(2 - 1.6 \times 0.955^2 \times 1.200 / 1.144 - 1.6 \times 0.955^2 \times 1.200^2 / 1.144) \times 0.021 - 0.000] = 0.996 \\ C_{yy} &\geq 3069.0 \times 10^3 / 3512.0 \times 10^3 = 0.874, \quad C_{yy} = 0.996 \end{aligned}$$

$$\begin{aligned} C_{zy} &= 1 + (w_y - 1) [(2 - 14.0 C_{m,y}^2 \cdot \bar{\lambda}_{\max}^2 / w_y^5) n_{pl} - d_{LT}] \geq 0.6 \sqrt{w_y/w_z} (W_{el,y} / W_{pl,y}) && \text{(Annex A, T.A.1)} \\ d_{LT} &= 2 \text{alt} \cdot [\bar{\lambda}_0 / (0.1 + \bar{\lambda}_z^4)] [\text{My,ed} / (C_{m,y} \cdot \chi_{LT} \cdot M_{pl,y,rd})] [M_{z,ed} / (C_{m,z} \cdot M_{pl,z,rd})] = \\ &= 20.998 \times [0.970 / (0.1 + 1.199^4)] [320.8 / (0.955 \times 0.933 \times 1089.5)] [0.0 / (0.000 \times 109.3)] = 0.000 \\ C_{zy} &= 1 + (1.144 - 1) [(2 - 14.0 \times 0.955^2 \times 1.200^2 / 1.144^5) \times 0.021 - 0.000] = 0.978 \\ C_{zy} &\geq 0.6 \sqrt{(1.144 / 1.500)} (3069.0 \times 10^3 / 3512.0 \times 10^3) = 0.458, \quad C_{zy} = 0.978 \end{aligned}$$

$$\begin{aligned} C_{yy} &= 0.996, \quad C_{zy} = 0.978 && \text{(Annex A, T.A.1)} \\ k_{yy} &= 0.955 \times 1.000 \times 1.000 / (1 - 118.70 / 76339.0) \times (1 / 0.996) = 0.960 \\ k_{zy} &= 0.955 \times 1.000 \times 0.984 / (1 - 118.70 / 76339.0) \times (1 / 0.978) \times 0.6 \times \sqrt{(1.144 / 1.500)} = 0.504 \end{aligned}$$

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

$$N_{ed}/(\chi_y \cdot N_{rk}/\gamma_{M1}) + k_{yy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rk}/\gamma_{M1}) = \quad (\text{EC3 Eq. 6.61})$$

$$118.7/(0.984 \times 5538.0/1.00) + 0.960 \times 320.8/(0.933 \times 1246.8/1.00) = 0.022 + 0.265 = 0.287$$

0.287 < 1.000, Is verified

$$N_{ed}/(\chi_z \cdot N_{rk}/\gamma_{M1}) + k_{zy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rk}/\gamma_{M1}) = \quad (\text{EC3 Eq. 6.62})$$

$$118.7/(0.479 \times 5538.0/1.00) + 0.504 \times 320.8/(0.933 \times 1246.8/1.00) = 0.045 + 0.139 = 0.184$$

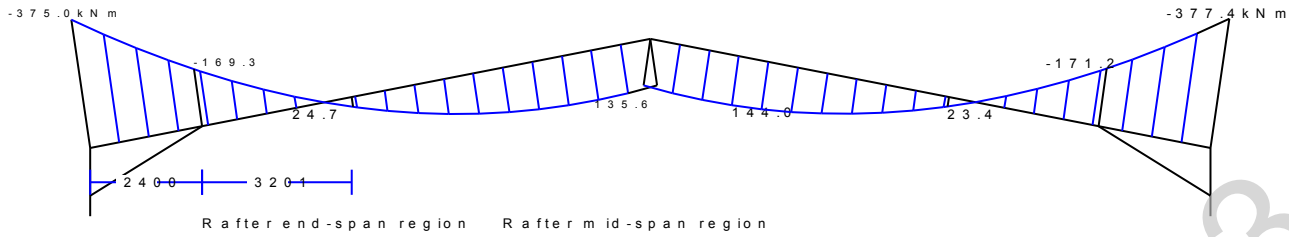
0.184 < 1.000, Is verified

Steel Portal Frame EC3
Example Report

13. Rafter verification (Ultimate Limit State)

(EN1993-1-1, §6)

L.C. 202 Bending moments kNm



Profile : IPE 500-S 355

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

- Ned = 83.5 kN
- Ved = 75.1 kN
- Myed = 171.2 kNm, Mzed = 0.0 kNm
- Myed = 144.3 kNm (at mid-span)
- Myed = -171.2 kNm (at haunch-start)
- Myed = -348.4 kNm (at haunch end)
- Myed = -377.4 kNm (at column axis point)

Maximum design values Rafter-Uplift conditions: L.C. 210: 1.00Gk+1.50Qw1

- Ned = 2.4 kN
- Ved = 13.8 kN
- Myed = -35.5 kNm

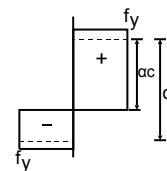
13.1. Classification of cross-sections, Rafter

(EN1993-1-1, §5.5)

Maximum and minimum cross-section stresses $\sigma = N_{ed}/A_{el} \pm M_{y,ed}/W_{el,y} \pm M_{z,ed}/W_{el,z}$
 $\sigma = [10^{-3}]84/11550 \pm [10^{-6}]171/1928.0 \times 10^3 \pm [10^{-6}]0/214.2 \times 10^3$
 $\sigma_1 = 96 \text{ N/mm}^2, \sigma_2 = -82 \text{ N/mm}^2$ (compression positive)

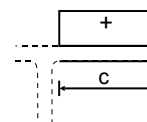
Web

$c = 500.0 - 2 \times 16.0 - 2 \times 21.0 = 426.0 \text{ mm}$, $t = 10.2 \text{ mm}$, $c/t = 426.0/10.2 = 41.76$
 S 355, $t = 10.2 \leq 40 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$, $\epsilon = (235/355)^{0.5} = 0.81$
 Position of neutral axis for combined Bending and compression
 $N_{ed}/(2t \cdot f_y/\gamma_{M0}) = 83500/(2 \times 10.2 \times 355/1.00) = 11.5 \text{ mm}$
 $\alpha = (426.0/2 + 11.5)/426.0 = 0.527 > 0.5$
 $c/t = 41.76 \leq 396 \times 0.81 / (13 \times 0.527 - 1) = 54.81$
 The web is class 1 (EN1993-1-1, Tab.5.2)



Flange

$c = 200.0/2 - 10.2/2 - 21.0 = 73.9 \text{ mm}$, $t = 16.0 \text{ mm}$, $c/t = 73.9/16.0 = 4.62$
 S 355, $t = 16.0 \leq 40 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$, $\epsilon = (235/355)^{0.5} = 0.81$
 $c/t = 4.62 \leq 9 \times 0.81 = 7.29$
 The flange is class 1 (EN1993-1-1, Tab.5.2)



Overall classification of cross-section is Class 1, Bending and compression $N_{c,ed} + M_{y,ed}$

13.2. Resistance of cross-section, Rafter (Ultimate Limit State)

(EN1993-1-1, §6.2)

Ultimate Limit State, Verification for compression

(EN1993-1-1, §6.2.4)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

$N_{c,ed} = 84.60 \text{ kN}$

Compression Resistance $N_{pl,rd} = A \cdot f_y/\gamma_{M0} = [10^{-3}] \times 11550 \times 355/1.00 = 4100.25 \text{ kN}$
 $N_{ed} = 84.60 \text{ kN} < 4100.25 \text{ kN} = N_{c,rd} = N_{pl,rd}$, Is verified

Ultimate Limit State, Verification for bending moment y-y

(EN1993-1-1, §6.2.5)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

My,ed=171.20 kNmBending Resistance $M_{pl,y,rd} = W_{pl,y} \cdot f_y / \gamma_{M0} = [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 778.87 \text{ kNm}$ $M_{y,ed} = 171.20 \text{ kNm} < 778.87 \text{ kNm} = M_{y,rd}$, Is verified**Ultimate Limit State, Verification for shear z**

(EN1993-1-1, §6.2.6)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

Vz,ed= 75.10 kNm $A_v = A - 2b \cdot t_f + (t_w + 2r) t_f = 11550 - 2 \times 200.0 \times 16.0 + (10.2 + 2 \times 21.0) \times 16.0 = 5985 \text{ mm}^2$

(EC3 §6.2.6.3)

 $A_v = 5985 \text{ mm}^2 > \eta \cdot h_w \cdot t_w = 1.00 \times (500.0 - 2 \times 16.0) \times 10.2 = 1.00 \times 484.0 \times 10.2 = 4937 \text{ mm}^2$ Plastic Shear Resistance $V_{pl,z,rd} = A_v (f_y / \sqrt{3}) / \gamma_{M0} = [10^{-3}] \times 5985 \times (355 / 1.73) / 1.00 = 1226.72 \text{ kN}$ $V_{z,ed} = 75.10 \text{ kN} < 1226.72 \text{ kN} = V_{z,rd}$, Is verified $h_w / t_w = (500.0 - 2 \times 16.0) / 10.2 = 484.0 / 10.2 = 47.45 <= 72 \times 0.81 / 1.00 = 72 \epsilon / \eta = 58.32$ ($\eta = 1.00$)S 355, $t = 10.2 <= 40 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$, $\epsilon = (235 / 355)^{0.5} = 0.81$

Shear buckling resistance is not necessary to be verified

(EC3 §6.2.6.6)

Ultimate Limit State, Verification for axial force, shear and bending

(EN1993-1-1, §6.2.9)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

N,ed= 83.50kN (Compression), Vz,ed= 75.10kNm, My,ed= 171.20kN $N_{pl,rd} = 4100.25 \text{ kN}$, $M_{pl,y,rd} = 778.87 \text{ kNm}$, $V_{pl,z,rd} = 1226.72 \text{ kN}$ $N_{ed} = 83.50 \text{ kN} <= 0.25 \times 4100.25 = 0.25 \times N_{pl,rd} = 1025.06 \text{ kN}$ $N_{ed} = 83.50 \text{ kN} <= [10^{-3}] \times 0.5 \times 484.0 \times 10.2 \times 355 / 1.00 = 0.5 h_w \cdot t_w \cdot f_y / \gamma_{M0} = 876.28 \text{ kN}$ $n = N_{ed} / N_{pl,rd} = 84 / 4100 = 0.020$

Effect of axial force is neglected

(EC3 §6.2.9.1 Eq.6.33, Eq.6.34, Eq.6.35)

 $V_{ed} = 75.10 \text{ kN} <= 0.50 \times 1226.72 = 0.50 \times V_{pl,rd} = 613.36 \text{ kN}$

Effect of shear force is neglected

(EC3 §6.2.8.2)

 $M_{y,ed} = 171.20 \text{ kNm} < 778.87 \text{ kNm} = M_{pl,y,rd}$, Is verified**13.3. Buckling resistance, Rafter mid-span region (Ultimate Limit State)**

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

Ned = 83.5 kN

Ved = 96.6 kN

Myed = 144.0 kNm, Mzed = 0.0 kNm

Rafter length $L_r = \sqrt{[(24000/2)^2 + (7000 - 5000)^2]} = 12042 \text{ mm}$

Buckling length, In-plane buckling

 $\alpha_{cr} = 45.47$, $N_{ed} = 83.5 \text{ kN}$, $L_{cr,y} = \pi \sqrt{[EI / \alpha_{cr} \cdot N_{ed}]} >= L_r = 12042 \text{ mm}$ $L_{cr,y} = \pi \sqrt{[210000 \times 482.00 \times 10^6 / (45.47 \times 83.5 \times 10^3)]} = 16217 \text{ mm}$, $L_{cr,y} = 16217 \text{ mm}$ Buckling length, In-plane buckling $L_{cr,y} = 16217 \text{ mm}$ (System length)Buckling length, Out-of-plane buckling $L_{cr,z} = 3000 \text{ mm}$ (Purlin spacing)**13.4. Flexural Buckling, Rafter mid-span region (Ultimate Limit State)**

(EN1993-1-1, §6.3.1)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

Buckling lengths: $L_{cr,y} = 1.347 \times 12042 = 16217 \text{ mm}$, $L_{cr,z} = 0.249 \times 12042 = 3000 \text{ mm}$

Non-dimensional slenderness (Cross-section Class: 1)

(EC3 §6.3.1.3)

 $\bar{\lambda}_y = \sqrt{(A \cdot f_y / N_{cr,y})} = (L_{cr,y} / i_y) \cdot (1 / \lambda_1) = (16217 / 204.3) \times (1 / 76.06) = 1.044$ $\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \cdot (1 / \lambda_1) = (3000 / 43.1) \times (1 / 76.06) = 0.916$ $\lambda_1 = \pi \sqrt{(E / f_y)} = 93.9 \epsilon = 76.06$, $\epsilon = \sqrt{(235 / f_y)} = 0.81$ $h/b = 500 / 200 = 2.50 >= 1.20$, $t_f = 16.0 \text{ mm} <= 40 \text{ mm}$ y-y buckling curve: a, imperfection factor: $\alpha_y = 0.21$, $\chi_y = 0.635$

(T.6.2, T.6.1, Fig.6.4)

 $\Phi_y = 0.5 [1 + \alpha_y (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = 0.5 [1 + 0.21 \times (1.044 - 0.2) + 1.044^2] = 1.134$ $\chi_y = 1 / [\Phi_y + \sqrt{(\Phi_y^2 - \bar{\lambda}_y^2)}] = 1 / [1.134 + \sqrt{(1.134^2 - 1.044^2)}] = 0.635 <= 1$ $\chi_y = 0.635$ z-z buckling curve: b, imperfection factor: $\alpha_z = 0.34$, $\chi_z = 0.651$ $\Phi_z = 0.5 [1 + \alpha_z (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = 0.5 [1 + 0.34 \times (0.916 - 0.2) + 0.916^2] = 1.041$ $\chi_z = 1 / [\Phi_z + \sqrt{(\Phi_z^2 - \bar{\lambda}_z^2)}] = 1 / [1.041 + \sqrt{(1.041^2 - 0.916^2)}] = 0.651 <= 1$ $\chi_z = 0.651$ Reduction factor $\chi = 1 / [\Phi + \sqrt{(\Phi^2 - \bar{\lambda}^2)}]$, $\chi <= 1.0$, $\Phi = 0.5 [1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2]$, $\chi = 0.635$

(EC3 Eq.6.49)

 $N_{b,rd} = \chi \cdot A \cdot f_y / \gamma_{M1} = 0.635 \times [10^{-3}] \times 11550 \times 355 / 1.00 = 2603.66 \text{ kN}$

(EC3 Eq.6.47)

 $N_{c,ed} = 83.54 \text{ kN} < 2603.66 \text{ kN} = N_{b,rd}$, Is verified

13.5. Lateral torsional buckling , Rafter mid-span region (EN1993-1-1, §6.3.2)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1
 Elastic critical moment for lateral-torsional buckling (EC3 §6.3.2.2.2, EN1993:2002 AnnexC)
Timoshenko, S.P, Gere, J.M, Theory of elastic stability, McGraw-Hill, 1961
 $M_{cr} = C_1 \cdot [\pi^2 EI_z / (kL)^2] \{ \sqrt{ [(kz/kw)^2 (I_w/I_z) + (kL)^2 GIt / (\pi^2 EI_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2] } - (C_2 \cdot z_g - C_3 \cdot z_j) \}$
 $G = E / (2(1+\nu)) = 210000 / (2(1+0.30)) = 80769 = 8.1 \times 10^4 \text{ N/mm}^2$
 $k \cdot L = 3000 \text{ mm}, z_g = h/2 = 500/2 = 250 \text{ mm}, z_j = 0 \text{ mm}$ (EN1993:2002 T.C.1)
 $kz = 1.0, kw = 1.0, \psi = 1.000, C_1 = 1.000, C_2 = 0.000, C_3 = 0.000$ (EN1993:2002 T.C.1)
 $M_{cr} = [10^{-6}] 1.000 \times [\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6 / 3000^2]$
 $\times \{ [1.0 \times (1249.4 \times 10^9 / 21.420 \times 10^6)]$
 $+ 3000^2 \times 8.1 \times 10^4 \times 0.893 \times 10^6 / (\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6) \}^{0.5} = 1332.3 \text{ kNm}$

$\bar{\lambda}, lt = \sqrt{(W_{pl,y} \cdot f_y / M_{cr})} = \sqrt{[10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1332.3} = 0.765$ (EC3 Eq.6.56)

$h/b = 500/200 = 2.50 > 2.00$ buckling curve: c
 imperfection factor: $\alpha, lt = 0.49, \beta = 0.75, \chi, lt = 0.786$ (T.6.3, T.6.5, Fig.6.4)
 $\Phi, lt = 0.5 [1 + \alpha, lt (\bar{\lambda}, lt - \bar{\lambda}, lto) + \beta \bar{\lambda}, lt^2] = 0.5 \times [1 + 0.49 \times (0.765 - 0.40) + 0.75 \times 0.765^2] = 0.809$
 $\chi, lt = 1 / [\Phi, lt + \sqrt{(\Phi, lt^2 - \beta \bar{\lambda}, lt^2)}] = 1 / [0.809 + \sqrt{(0.809^2 - 0.75 \times 0.809^2)}] = 0.786$
 Reduction factor $\chi, lt = 1 / [\Phi, lt + \sqrt{(\Phi, lt^2 - \beta \bar{\lambda}, lt^2)}], \chi, lt \leq 1.0, 1 / \bar{\lambda}, lt^2, \chi, lt = 0.786$ (Eq.6.57)

$\chi, lt, mod = \chi, lt / f, \chi, lt, mod \leq 1, \chi, lt, mod \leq 1 / \bar{\lambda}, lt^2 = 1 / 0.765^2 = 1.71$ (EC3 §6.3.2.3(2), Eq.6.58)
 $K_c = 1.00$ (EC3 Tab.6.6)

$f = 1 - 0.5(1 - k_c) [1 - 2.0(\bar{\lambda}, lt - 0.8)^2] = 1 - 0.5 \times (1 - 1.000) [1 - 2.0 \times (0.765 - 0.8)^2] = 1.000, f \leq 1.0$
 $\chi, lt, mod = \chi, lt / f = 0.786 / 1.000 = 0.786, \chi, lt, mod \leq 1.0, \chi, lt, mod \leq 1.71, \chi, lt, mod = 0.786$

$M_{b,rd} = \chi, lt \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 0.786 \times [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 612.19 \text{ kNm}$ (EC3 Eq.6.55)
 $M_{y,ed} = 144.05 \text{ kNm} < 612.19 \text{ kNm} = M_{b,rd}, \text{ Is verified}$

13.6. Axial force and bending moment, Rafter mid-span region (EN1993-1-1, §6.3.3)

$N_{ed} / (\chi_y \cdot N_{rk} / \gamma_{M1}) + k_{yy} \cdot M_{y,ed} / (\chi_{LT} \cdot M_{y,rk} / \gamma_{M1}) \leq 1$ (EC3 Eq.6.61)
 $N_{ed} / (\chi_z \cdot N_{rk} / \gamma_{M1}) + k_{zy} \cdot M_{y,ed} / (\chi_{LT} \cdot M_{y,rk} / \gamma_{M1}) \leq 1$ (EC3 Eq.6.62)
 $N_{rk} = A \cdot f_y = [10^{-3}] \times 11550 \times 355 = 4100.2 \text{ kN}$ (Tab.6.7)
 $M_{y,rk} = W_{pl,y} \cdot f_y = [10^{-6}] \times 2194.0 \times 10^3 \times 355 = 778.9 \text{ kNm}$
 $\chi_y \cdot N_{rk} / \gamma_{M1} = \chi_y \cdot A \cdot f_y / \gamma_{M1} = 0.635 \times [10^{-3}] \times 11550 \times 355 / 1.00 = 2603.7 \text{ kN}$
 $\chi_z \cdot N_{rk} / \gamma_{M1} = \chi_z \cdot A \cdot f_y / \gamma_{M1} = 0.651 \times [10^{-3}] \times 11550 \times 355 / 1.00 = 2669.3 \text{ kN}$
 $\chi_{LT} \cdot M_{y,rk} / \gamma_{M1} = \chi_{LT} \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 0.786 \times [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 612.2 \text{ kNm}$

Interaction factors, Method of computation: Method 1 Annex A (EC3 AnnexA)

$k_{yy} = C_{my} \cdot C_{mLT} (\mu_y / (1 - N_{ed} / N_{cr,y}) (1 / C_{yy}), \mu_y = (1 - N_{ed} / N_{cr,y}) / (1 - \chi_y \cdot N_{ed} / N_{cr,y})$ (EC3 Tab.A.1)
 $k_{zy} = C_{my} \cdot C_{mLT} (\mu_z / (1 - N_{ed} / N_{cr,y}) (1 / C_{zy}) 0.60 \sqrt{(w_y / w_z)}, \mu_z = (1 - N_{ed} / N_{cr,z}) / (1 - \chi_z \cdot N_{ed} / N_{cr,z})$

$N_{cr,y} = \pi^2 EI_y / l_{cr,y}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 482.00 \times 10^6 / 16217^2 = 3799 \text{ kN}$
 $N_{cr,z} = \pi^2 EI_z / l_{cr,z}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 21.420 \times 10^6 / 3000^2 = 4933 \text{ kN}$
 $N_{cr,t} = (1 / i_p^2) \times (G \cdot I_t + \pi^2 EI_w / L_{cr,t}^2)$ (EC3 NCCI SN003b-EN-EU)
 $N_{cr,t} = [10^{-3}] \times (1 / 209^2) [80769 \times 0.893 \times 10^6 + \pi^2 \times 210000 \times 1249.4 \times 10^9 / 4040^2] = 5294 \text{ kN}$

$\mu_y = (1 - N_{ed} / N_{cr,y}) / (1 - \chi_y \cdot N_{ed} / N_{cr,y}) = (1 - 83.5 / 3799) / (1 - 0.635 \times 83.5 / 3799) = 0.992$
 $\mu_z = (1 - N_{ed} / N_{cr,z}) / (1 - \chi_z \cdot N_{ed} / N_{cr,z}) = (1 - 83.5 / 4933) / (1 - 0.651 \times 83.5 / 4933) = 0.994$
 $\alpha_{lt} = 1 - I_t / I_y > 0 = 1 - 0.893 \times 10^6 / 482.00 \times 10^6 = 0.998$ (EC3 Annex A.1)

$w_y = W_{pl,y} / W_{el,y} \leq 1.50, w_y = 2.194 \times 10^6 / 1.928 \times 10^6 = 1.138 \leq 1.50$ (EC3 Annex A.1)
 $w_z = W_{pl,z} / W_{el,z} \leq 1.50, w_z = 0.336 \times 10^6 / 0.214 \times 10^6 = 1.568 > 1.50, w_z = 1.50$
 $n_{pl} = N_{ed} / (N_{rk} / \gamma_{M1}) = 83.54 / (4100.20 / 1.00) = 0.020$

$\bar{\lambda}_{max} = \max(1.044, 0.916) = 1.040$ (EC3 Annex A.1)

$M_{cr,o} = (1.00 / 1.00) \times 1332.30 = 1332.3, C_1 = 1.00$
 $\bar{\lambda}_o = \sqrt{[10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1332.3} = 0.760$
 $\bar{\lambda}_o, lim = 0.2 \sqrt{C_1 [(1 - N_{ed} / N_{cr,z}) (1 - N_{ed} / N_{cr,t})]^{0.25}}$ (EC3 Annex A.1)
 $\bar{\lambda}_o, lim = 0.2 \sqrt{1.000 [(1 - 83.5 / 4933) (1 - 83.5 / 5294)]^{0.25}} = 0.198$

$\epsilon_y = (M_{y,ed} / N_{ed}) (A / W_{el}) = ([10^3] \times 144.05 / 83.54) \times (11550.0 / 1928.0 \times 10^3) = 10.33$

$$C_{my,o} = 0.79 + 0.21\psi + 0.36(\psi - 0.33) \times (83.54/3799.0) = 1.005, \quad (\psi = 1.00) \quad (\text{EC3 Annex A, T.A.1})$$

$$\bar{\lambda}_o = 0.760 > \bar{\lambda}_{o,lim} = 0.198$$

$$C_{my} = C_{my,o} + (1 - C_{my,o}) \cdot (\sqrt{\varepsilon_y \cdot \text{alt}}) / (1 + \sqrt{\varepsilon_y \cdot \text{alt}}) =$$

$$= 1.005 + (1 - 1.005) \times (\sqrt{10.329 \times 0.998}) / (1 + \sqrt{10.329 \times 0.998}) = 1.001$$

$$C_{mlt} = C_{my}^2 \cdot \text{alt} / \sqrt{[(1 - N_{ed}/N_{cr,z})(1 - N_{ed}/N_{cr,t})]} >= 1$$

$$C_{mlt} = 1.001^2 \times 0.998 / \sqrt{[(1 - 83.5/4933.0)(1 - 83.5/5294.0)]} = 1.017, \quad C_{mlt} = 1.017$$

$$C_{yy} = 1 + (w_y - 1) [(2 - 1.6C_{my}^2 \cdot \bar{\lambda}_{max}/w_y - 1.6C_{my}^2 \cdot \bar{\lambda}_{max}^2/w_y) n_{pl} - b_{lt}] >= W_{el,y}/W_{pl,y} \quad (\text{Annex A, T.A.1})$$

$$b_{lt} = 0.5 \text{alt} \cdot \bar{\lambda}_o^2 [M_{y,ed}/(\chi_{lt} \cdot M_{pl,y,rd})] [M_{z,ed}/M_{pl,z,rd}] =$$

$$= 0.5 \times 0.998 \times 0.760^2 [0.0/(0.786 \times 684.4)] (0.0/76.0) = 0.000$$

$$C_{yy} = 1 + (1.138 - 1) [(2 - 1.6 \times 1.001^2 \times 1.040/1.138 - 1.6 \times 1.001^2 \times 1.040^2/1.138) \times 0.020 - 0.000] = 0.997$$

$$C_{yy} >= 1928.0 \times 10^3 / 2194.0 \times 10^3 = 0.879, \quad C_{yy} = 0.997$$

$$C_{zy} = 1 + (w_y - 1) [(2 - 14.0C_{my}^2 \cdot \bar{\lambda}_{max}^2/w_y^5) n_{pl} - d_{lt}] >= 0.6 \sqrt{(w_y/w_z)} (W_{el,y}/W_{pl,y}) \quad (\text{Annex A, T.A.1})$$

$$d_{lt} = 2 \text{alt} \cdot [\bar{\lambda}_o / (0.1 + \bar{\lambda}_z^4)] [M_{y,ed}/(C_{my} \cdot \chi_{lt} \cdot M_{pl,y,rd})] [M_{z,ed}/(C_{mz} \cdot M_{pl,z,rd})] =$$

$$= 20.998 \times [0.760 / (0.1 + 0.916^4)] [0.0 / (1.001 \times 0.786 \times 684.4)] [0.0 / (0.000 \times 76.0)] = 0.000$$

$$C_{zy} = 1 + (1.138 - 1) [(2 - 14.0 \times 1.001^2 \times 1.040^2/1.138^5) \times 0.020 - 0.000] = 0.984$$

$$C_{zy} >= 0.6 \sqrt{(1.138/1.500)} (1928.0 \times 10^3 / 2194.0 \times 10^3) = 0.459, \quad C_{zy} = 0.984$$

$$C_{yy} = 0.997, \quad C_{zy} = 0.984 \quad (\text{Annex A, T.A.1})$$

$$k_{yy} = 1.001 \times 1.017 \times 0.992 / (1 - 83.54/3799.0) \times (1/0.997) = 1.036$$

$$k_{zy} = 1.001 \times 1.017 \times 0.994 / (1 - 83.54/3799.0) \times (1/0.984) \times 0.6 \sqrt{(1.138/1.500)} = 0.550$$

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

$$N_{ed}/(\chi_y \cdot N_{rk}/\gamma_{M1}) + k_{yy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rd}/\gamma_{M1}) = \quad (\text{EC3 Eq.6.61})$$

$$83.5 / (0.635 \times 4100.2 / 1.00) + 1.036 \times 144.0 / (0.786 \times 778.9 / 1.00) = 0.032 + 0.244 = 0.276$$

$$0.276 < 1.000, \quad \text{Is verified}$$

$$N_{ed}/(\chi_z \cdot N_{rk}/\gamma_{M1}) + k_{zy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rd}/\gamma_{M1}) = \quad (\text{EC3 Eq.6.62})$$

$$83.5 / (0.651 \times 4100.2 / 1.00) + 0.550 \times 144.0 / (0.786 \times 778.9 / 1.00) = 0.031 + 0.129 = 0.161$$

$$0.161 < 1.000, \quad \text{Is verified}$$

13.7. Buckling resistance, Rafter end-span region (Ultimate Limit State)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

N_{ed} = 92.6 kN
 V_{ed} = 96.6 kN
 M_{y,ed} = 171.2 kNm, M_{z,ed} = 0.0 kNm

Rafter length L_r = $\sqrt{[(24000/2)^2 + (7000 - 5000)^2]} = 12042$ mm
 Buckling length, In-plane buckling L_{cr,y} = 16217 mm (System length)
 Buckling length, Out-of-plane buckling L_{cr,z} = 3201 mm (Torsional restrains of rafters)

13.8. Flexural Buckling, Rafter end-span region (Ultimate Limit State) (EN1993-1-1, §6.3.1)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

Buckling lengths: L_{cr,y} = 1.347 × 12042 = 16217 mm, L_{cr,z} = 0.266 × 12042 = 3201 mm
 Non-dimensional slenderness (Cross-section Class: 1) (EC3 §6.3.1.3)

$$\bar{\lambda}_y = \sqrt{(A \cdot f_y / N_{cr,y})} = (L_{cr,y} / i_y) \cdot (1/\lambda_1) = (16217/204.3) \times (1/76.06) = 1.044$$

$$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \cdot (1/\lambda_1) = (3201/43.1) \times (1/76.06) = 0.977$$

$$\lambda_1 = \pi \sqrt{(E/f_y)} = 93.9 \varepsilon = 76.06, \quad \varepsilon = \sqrt{(235/f_y)} = 0.81$$

h/b = 500/200 = 2.50 >= 1.20, t_f = 16.0 mm <= 40 mm

y-y buckling curve: a, imperfection factor: α_y = 0.21, χ_y = 0.635 (T.6.2, T.6.1, Fig.6.4)

$$\Phi_y = 0.5 [1 + \alpha_y (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = 0.5 \times [1 + 0.21 \times (1.044 - 0.2) + 1.044^2] = 1.134$$

$$\chi_y = 1 / [\Phi_y + \sqrt{(\Phi_y^2 - \bar{\lambda}_y^2)}] = 1 / [1.134 + \sqrt{(1.134^2 - 1.044^2)}] = 0.635 <= 1 \quad \chi_y = 0.635$$

z-z buckling curve: b, imperfection factor: α_z = 0.34, χ_z = 0.612

$$\Phi_z = 0.5 [1 + \alpha_z (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = 0.5 \times [1 + 0.34 \times (0.977 - 0.2) + 0.977^2] = 1.109$$

$$\chi_z = 1 / [\Phi_z + \sqrt{(\Phi_z^2 - \bar{\lambda}_z^2)}] = 1 / [1.109 + \sqrt{(1.109^2 - 0.977^2)}] = 0.612 <= 1 \quad \chi_z = 0.612$$

Reduction factor χ = 1 / [Φ + √(Φ² - λ̄²)], χ <= 1.0, Φ = 0.5 [1 + α(λ̄ - 0.2) + λ̄²], χ = 0.612 (EC3 Eq.6.49)

N_{b,rd} = χ · A · f_y / γ_{M1} = 0.612 × [10⁻³] × 11550 × 355 / 1.00 = 2509.35 kN (EC3 Eq.6.47)

N_{c,ed} = 92.62 kN < 2509.35 kN = N_{b,rd}, Is verified

13.9. Lateral torsional buckling , Rafter end-span region (EN1993-1-1, §6.3.2)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1
 Elastic critical moment for lateral-torsional buckling (EC3 §6.3.2.2.2, EN1993:2002 AnnexC)
 Timoshenko, S.P, Gere, J.M, Theory of elastic stability, McGraw-Hill, 1961
 $M_{cr} = C_1 \cdot [\pi^2 EI_z / (kL)^2] \{ \sqrt{[(kz/kw)^2 (I_w/I_z) + (kL)^2 GIt / (\pi^2 EI_z) + (C_2 \cdot z_g - C_3 \cdot z_j)^2]} - (C_2 \cdot z_g - C_3 \cdot z_j) \}$
 $G = E / (2(1+\nu)) = 210000 / (2(1+0.30)) = 80769 = 8.1 \times 10^4 \text{ N/mm}^2$
 $k \cdot L = 3201 \text{ mm}, z_g = h/2 = 500/2 = 250 \text{ mm}, z_j = 0 \text{ mm}$ (EN1993:2002 T.C.1)
 $kz = 1.0, kw = 1.0, \psi = -0.137, C_1 = 2.044, C_2 = 0.000, C_3 = 0.000$ (EN1993:2002 T.C.1)
 $M_{cr} = [10^{-6}] 2.044 \times [\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6 / 3201^2]$
 $\times \{ [1.0 \times (1249.4 \times 10^9 / 21.420 \times 10^6) + 3201^2 \times 8.1 \times 10^4 \times 0.893 \times 10^6 / (\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6)]^{0.5} \} = 2425.0 \text{ kNm}$

$\bar{\lambda}, lt = \sqrt{(W_{pl,y} \cdot f_y / M_{cr})} = \sqrt{([10^{-6}] \times 2194.0 \times 10^3 \times 355 / 2425.0)} = 0.567$ (EC3 Eq.6.56)

$h/b = 500/200 = 2.50 > 2.00$ buckling curve: c
 imperfection factor: $\alpha, lt = 0.49, \beta = 0.75, \chi, lt = 0.905$ (T.6.3, T.6.5, Fig.6.4)

$\Phi, lt = 0.5 [1 + \alpha, lt (\bar{\lambda}, lt - \bar{\lambda}, lto) + \beta \bar{\lambda}, lt^2] = 0.5 \times [1 + 0.49 \times (0.567 - 0.40) + 0.75 \times 0.567^2] = 0.661$

$\chi, lt = 1 / [\Phi, lt + \sqrt{(\Phi, lt^2 - \beta \bar{\lambda}, lt^2)}] = 1 / [0.661 + \sqrt{(0.661^2 - 0.75 \times 0.567^2)}] = 0.905$

Reduction factor $\chi, lt = 1 / [\Phi, lt + \sqrt{(\Phi, lt^2 - \beta \bar{\lambda}, lt^2)}], \chi, lt \leq 1.0, 1 / \bar{\lambda}, lt^2, \chi, lt = 0.905$ (Eq.6.57)

$\chi, lt, mod = \chi, lt / f, \chi, lt, mod \leq 1, \chi, lt, mod \leq 1 / \bar{\lambda}, lt^2 = 1 / 0.567^2 = 3.11$ (EC3 §6.3.2.3(2), Eq.6.58)

$K_c = 1 / (1.33 - 0.33\psi) = 0.727, \psi = -0.14$ (EC3 Tab.6.6)

$f = 1 - 0.5(1 - k_c) [1 - 2.0(\bar{\lambda}, lt - 0.8)^2] = 1 - 0.5 \times (1 - 0.727) [1 - 2.0 \times (0.567 - 0.8)^2] = 0.878, f \leq 1.0$

$\chi, lt, mod = \chi, lt / f = 0.905 / 0.878 = 1.030, \chi, lt, mod \leq 1.0, \chi, lt, mod \leq 3.11, \chi, lt, mod = 1.000$

$M_{b,rd} = \chi, lt \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 1.000 \times [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 778.87 \text{ kNm}$ (EC3 Eq.6.55)

$M_{y,ed} = 171.23 \text{ kNm} < 778.87 \text{ kNm} = M_{b,rd}$, Is verified

13.10. Axial force and bending moment, Rafter end-span region (EN1993-1-1, §6.3.3)

$N_{ed} / (\chi_y \cdot N_{rk} / \gamma_{M1}) + k_{yy} \cdot M_{y,ed} / (\chi_{LT} \cdot M_{y,rk} / \gamma_{M1}) \leq 1$ (EC3 Eq.6.61)

$N_{ed} / (\chi_z \cdot N_{rk} / \gamma_{M1}) + k_{zy} \cdot M_{y,ed} / (\chi_{LT} \cdot M_{y,rk} / \gamma_{M1}) \leq 1$ (EC3 Eq.6.62)

$N_{rk} = A \cdot f_y = [10^{-3}] \times 11550 \times 355 = 4100.2 \text{ kN}$ (Tab.6.7)

$M_{y,rk} = W_{pl,y} \cdot f_y = [10^{-6}] \times 2194.0 \times 10^3 \times 355 = 778.9 \text{ kNm}$

$\chi_y \cdot N_{rk} / \gamma_{M1} = \chi_y \cdot A \cdot f_y / \gamma_{M1} = 0.635 \times [10^{-3}] \times 11550 \times 355 / 1.00 = 2603.7 \text{ kN}$

$\chi_z \cdot N_{rk} / \gamma_{M1} = \chi_z \cdot A \cdot f_y / \gamma_{M1} = 0.612 \times [10^{-3}] \times 11550 \times 355 / 1.00 = 2509.4 \text{ kN}$

$\chi_{LT} \cdot M_{y,rk} / \gamma_{M1} = \chi_{LT} \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 1.000 \times [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 778.9 \text{ kNm}$

Interaction factors, Method of computation: Method 1 Annex A (EC3 AnnexA)

$k_{yy} = C_{mLT} (\mu_y / (1 - N_{ed} / N_{cr,y}) (1 / C_{yy}), \mu_y = (1 - N_{ed} / N_{cr,y}) / (1 - \chi_y \cdot N_{ed} / N_{cr,y})$ (EC3 Tab.A.1)

$k_{zy} = C_{mLT} (\mu_z / (1 - N_{ed} / N_{cr,y}) (1 / C_{zy}) 0.60 \sqrt{(w_y / w_z)}, \mu_z = (1 - N_{ed} / N_{cr,z}) / (1 - \chi_z \cdot N_{ed} / N_{cr,z})$

$N_{cr,y} = \pi^2 EI_y / l_{cr,y}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 482.00 \times 10^6 / 16217^2 = 3799 \text{ kN}$

$N_{cr,z} = \pi^2 EI_z / l_{cr,z}^2 = 3.14^2 \times [10^{-3}] \times 210000 \times 21.420 \times 10^6 / 3201^2 = 4333 \text{ kN}$

$N_{cr,t} = (1 / i_p^2) \times (G \cdot It + \pi^2 EI_w / L_{cr,t}^2)$ (EC3 NCCI SN003b-EN-EU)

$N_{cr,t} = [10^{-3}] \times (1 / 209^2) [80769 \times 0.893 \times 10^6 + \pi^2 \times 210000 \times 1249.4 \times 10^9 / 4311^2] = 4851 \text{ kN}$

$\mu_y = (1 - N_{ed} / N_{cr,y}) / (1 - \chi_y \cdot N_{ed} / N_{cr,y}) = (1 - 92.6 / 3799) / (1 - 0.635 \times 92.6 / 3799) = 0.991$

$\mu_z = (1 - N_{ed} / N_{cr,z}) / (1 - \chi_z \cdot N_{ed} / N_{cr,z}) = (1 - 92.6 / 4333) / (1 - 0.612 \times 92.6 / 4333) = 0.992$

$\alpha_{lt} = 1 - It / I_y > 0 = 1 - 0.893 \times 10^6 / 482.00 \times 10^6 = 0.998$ (EC3 Annex A.1)

$w_y = W_{pl,y} / W_{el,y} \leq 1.50, w_y = 2.194 \times 10^6 / 1.928 \times 10^6 = 1.138 \leq 1.50$ (EC3 Annex A.1)

$w_z = W_{pl,z} / W_{el,z} \leq 1.50, w_z = 0.336 \times 10^6 / 0.214 \times 10^6 = 1.568 > 1.50, w_z = 1.50$

$n_{pl} = N_{ed} / (N_{rk} / \gamma_{M1}) = 92.62 / (4100.20 / 1.00) = 0.023$

$\bar{\lambda}_{max} = \max(1.044, 0.977) = 1.040$ (EC3 Annex A.1)

$M_{cr,o} = (1.00 / 2.04) \times 2425.00 = 1186.4, C_1 = 1.00$

$\bar{\lambda}_o = \sqrt{([10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1186.4)} = 0.810$

$\bar{\lambda}_o, lim = 0.2 \sqrt{C_1 [(1 - N_{ed} / N_{cr,z}) (1 - N_{ed} / N_{cr,t})]^{0.25}}$ (EC3 Annex A.1)

$\bar{\lambda}_o, lim = 0.2 \sqrt{2.044 [(1 - 92.6 / 4333) (1 - 92.6 / 4851)]^{0.25}} = 0.283$

$\epsilon_y = (M_{y,ed} / N_{ed}) (A / W_{el}) = ([10^3] \times 171.23 / 92.62) \times (11550.0 / 1928.0 \times 10^3) = 11.07$

$$C_{my,o} = 0.79 + 0.21\psi + 0.36(\psi - 0.33) \times (92.62/3799.0) = 0.757, \quad (\psi = -0.14) \quad (\text{EC3 Annex A, T.A.1})$$

$$\bar{\lambda}_o = 0.810 > \bar{\lambda}_{o,lim} = 0.283$$

$$C_{my} = C_{my,o} + (1 - C_{my,o}) \cdot (\sqrt{\varepsilon_y \cdot \text{alt}}) / (1 + \sqrt{\varepsilon_y \cdot \text{alt}}) =$$

$$= 0.757 + (1 - 0.757) \times (\sqrt{11.075 \times 0.998}) / (1 + \sqrt{11.075 \times 0.998}) = 0.944$$

$$C_{m1t} = C_{my}^2 \cdot \text{alt} / \sqrt{[(1 - N_{ed}/N_{cr,z})(1 - N_{ed}/N_{cr,t})]} >= 1$$

$$C_{m1t} = 0.944^2 \times 0.998 / \sqrt{[(1 - 92.6/4333.0)(1 - 92.6/4851.0)]} = 0.908, \quad C_{m1t} = 1.000$$

$$C_{yy} = 1 + (w_y - 1) [(2 - 1.6C_{my}^2 \cdot \bar{\lambda}_{max}/w_y - 1.6C_{my}^2 \cdot \bar{\lambda}_{max}^2/w_y) n_{pl} - b_{lt}] >= W_{el,y}/W_{pl,y} \quad (\text{Annex A, T.A.1})$$

$$b_{lt} = 0.5 \text{alt} \cdot \bar{\lambda}_o^2 [M_{y,ed}/(\chi_{lt} \cdot M_{pl,y,rd})] [M_{z,ed}/M_{pl,z,rd}] =$$

$$= 0.5 \times 0.998 \times 0.810^2 [0.0/(1.000 \times 684.4)] (0.0/76.0) = 0.000$$

$$C_{yy} = 1 + (1.138 - 1) [(2 - 1.6 \times 0.944^2 \times 1.040/1.138 - 1.6 \times 0.944^2 \times 1.040^2/1.138) \times 0.023 - 0.000] = 0.998$$

$$C_{yy} >= 1928.0 \times 10^3 / 2194.0 \times 10^3 = 0.879, \quad C_{yy} = 0.998$$

$$C_{zy} = 1 + (w_y - 1) [(2 - 14.0C_{my}^2 \cdot \bar{\lambda}_{max}^2/w_y^5) n_{pl} - d_{lt}] >= 0.6 \sqrt{(w_y/w_z)} (W_{el,y}/W_{pl,y}) \quad (\text{Annex A, T.A.1})$$

$$d_{lt} = 2 \text{alt} \cdot [\bar{\lambda}_o / (0.1 + \bar{\lambda}_z^4)] [M_{y,ed}/(C_{my} \cdot \chi_{lt} \cdot M_{pl,y,rd})] [M_{z,ed}/(C_{mz} \cdot M_{pl,z,rd})] =$$

$$= 20.998 \times [0.810 / (0.1 + 0.977^4)] [0.0 / (0.944 \times 1.000 \times 684.4)] [0.0 / (0.000 \times 76.0)] = 0.000$$

$$C_{zy} = 1 + (1.138 - 1) [(2 - 14.0 \times 0.944^2 \times 1.040^2/1.138^5) \times 0.023 - 0.000] = 0.984$$

$$C_{zy} >= 0.6 \sqrt{(1.138/1.500)} (1928.0 \times 10^3 / 2194.0 \times 10^3) = 0.459, \quad C_{zy} = 0.984$$

$$C_{yy} = 0.998, \quad C_{zy} = 0.984 \quad (\text{Annex A, T.A.1})$$

$$k_{yy} = 0.944 \times 1.000 \times 0.991 / (1 - 92.62/3799.0) \times (1/0.998) = 0.961$$

$$k_{zy} = 0.944 \times 1.000 \times 0.992 / (1 - 92.62/3799.0) \times (1/0.984) \times 0.6 \sqrt{(1.138/1.500)} = 0.510$$

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

$$N_{ed}/(\chi_y \cdot N_{rk}/\gamma_{M1}) + k_{yy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rd}/\gamma_{M1}) = \quad (\text{EC3 Eq.6.61})$$

$$92.6 / (0.635 \times 4100.2/1.00) + 0.961 \times 171.2 / (1.000 \times 778.9/1.00) = 0.036 + 0.211 = 0.247$$

$$0.247 < 1.000, \quad \text{Is verified}$$

$$N_{ed}/(\chi_z \cdot N_{rk}/\gamma_{M1}) + k_{zy} \cdot M_{y,ed}/(\chi_{LT} \cdot M_{y,rd}/\gamma_{M1}) = \quad (\text{EC3 Eq.6.62})$$

$$92.6 / (0.612 \times 4100.2/1.00) + 0.510 \times 171.2 / (1.000 \times 778.9/1.00) = 0.037 + 0.112 = 0.149$$

$$0.149 < 1.000, \quad \text{Is verified}$$

13.11. Buckling resistance, Rafter-Uplift conditions (Ultimate Limit State)

Maximum design values. Verification for load case: L.C. 210: 1.00Gk+1.50Qw1

N_{ed} = 2.4 kN
 V_{ed} = 13.8 kN
 M_{y,ed} = 35.5 kNm, M_{z,ed} = 0.0 kNm

Rafter length L_r = $\sqrt{[(24000/2)^2 + (7000 - 5000)^2]} = 12042$ mm
 Buckling length, In-plane buckling L_{cr,y} = 16217 mm (System length)
 Buckling length, Out-of-plane buckling L_{cr,z} = 3201 mm (Torsional restrains of rafters)

13.12. Flexural Buckling, Rafter-Uplift conditions (Ultimate Limit State) (EN1993-1-1, §6.3.1)

Maximum design values. Verification for load case: L.C. 210: 1.00Gk+1.50Qw1

Buckling lengths: L_{cr,y} = 1.347 × 12042 = 16217 mm, L_{cr,z} = 0.266 × 12042 = 3201 mm
 Non-dimensional slenderness (Cross-section Class: 1) (EC3 §6.3.1.3)

$$\bar{\lambda}_y = \sqrt{(A \cdot f_y / N_{cr,y})} = (L_{cr,y} / i_y) \cdot (1/\lambda_1) = (16217/204.3) \times (1/76.06) = 1.044$$

$$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \cdot (1/\lambda_1) = (3201/43.1) \times (1/76.06) = 0.977$$

$$\lambda_1 = \pi \sqrt{(E/f_y)} = 93.9 \varepsilon = 76.06, \quad \varepsilon = \sqrt{(235/f_y)} = 0.81$$

h/b = 500/200 = 2.50 >= 1.20, t_f = 16.0 mm <= 40 mm

y-y buckling curve: a, imperfection factor: α_y = 0.21, χ_y = 0.635 (T.6.2, T.6.1, Fig.6.4)

$$\Phi_y = 0.5 [1 + \alpha_y (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = 0.5 \times [1 + 0.21 \times (1.044 - 0.2) + 1.044^2] = 1.134$$

$$\chi_y = 1 / [\Phi_y + \sqrt{(\Phi_y^2 - \bar{\lambda}_y^2)}] = 1 / [1.134 + \sqrt{(1.134^2 - 1.044^2)}] = 0.635 <= 1 \quad \chi_y = 0.635$$

z-z buckling curve: b, imperfection factor: α_z = 0.34, χ_z = 0.612

$$\Phi_z = 0.5 [1 + \alpha_z (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = 0.5 \times [1 + 0.34 \times (0.977 - 0.2) + 0.977^2] = 1.109$$

$$\chi_z = 1 / [\Phi_z + \sqrt{(\Phi_z^2 - \bar{\lambda}_z^2)}] = 1 / [1.109 + \sqrt{(1.109^2 - 0.977^2)}] = 0.612 <= 1 \quad \chi_z = 0.612$$

Reduction factor χ = 1 / [Φ + √(Φ² - λ̄²)], χ <= 1.0, Φ = 0.5 [1 + α(λ̄ - 0.2) + λ̄²], χ = 0.612 (EC3 Eq.6.49)

N_{b,rd} = χ · A · f_y / γ_{M1} = 0.612 × [10⁻³] × 11550 × 355 / 1.00 = 2509.35 kN (EC3 Eq.6.47)

N_{c,ed} = 2.44 kN < 2509.35 kN = N_{b,rd}, Is verified

13.13. Lateral torsional buckling, Rafter-Uplift conditions (EN1993-1-1, §6.3.2)

Maximum design values. Verification for load case: L.C. 210: 1.00Gk+1.50Qw1

Hogging

$k \cdot L = 3201 \text{ mm}$, $z_g = -250 \text{ mm}$, $z_j = 0 \text{ mm}$ (EN1993:2002 T.C.1)
 $k_z = 1.0$, $k_w = 1.0$, $C_1 = 1.000$, $C_2 = 0.000$, $C_3 = 1.000$ (EN1993:2002 T.C.1)
 $M_{cr} = [10^{-6}] 1.000 \times [\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6 / 3201^2]$
 $\times \{ [1.0 \times (1249.4 \times 10^9 / 21.420 \times 10^6)]$
 $+ 3201^2 \times 8.1 \times 10^4 \times 0.893 \times 10^6 / (\pi^2 \times 2.1 \times 10^5 \times 21.420 \times 10^6)]^{0.5} \} = 1186.4 \text{ kNm}$

$\bar{\lambda}, l_t = \sqrt{(W_{pl,y} \cdot f_y / M_{cr})} = \sqrt{([10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1186.4)} = 0.810$ (EC3 Eq.6.56)

$h/b = 500/200 = 2.50 > 2.00$ buckling curve: c

imperfection factor: $\alpha, l_t = 0.49$, $\beta = 0.75$, $\chi, l_t = 0.757$ (T.6.3, T.6.5, Fig.6.4)

$\Phi, l_t = 0.5 [1 + \alpha, l_t (\bar{\lambda}, l_t - \bar{\lambda}, l_{t0}) + \beta \bar{\lambda}, l_t^2] = 0.5 \times [1 + 0.49 \times (0.810 - 0.40) + 0.75 \times 0.810^2] = 0.847$

$\chi, l_t = 1 / [\Phi, l_t + \sqrt{(\Phi, l_t^2 - \beta \bar{\lambda}, l_t^2)}] = 1 / [0.847 + \sqrt{(0.847^2 - 0.75 \times 0.810^2)}] = 0.757$

Reduction factor $\chi, l_t = 1 / [\Phi, l_t + \sqrt{(\Phi, l_t^2 - \beta \bar{\lambda}, l_t^2)}]$, $\chi, l_t \leq 1.0$, $1 / \bar{\lambda}, l_t^2$, $\chi, l_t = 0.757$ (Eq.6.57)

$\chi, l_t, \text{mod} = \chi, l_t / f$, $\chi, l_t, \text{mod} \leq 1$, $\chi, l_t, \text{mod} \leq 1 / \bar{\lambda}, l_t^2 = 1 / 0.810^2 = 1.52$ (EC3 §6.3.2.3(2), Eq.6.58)

$K_c = 1 / (1.33 - 0.33\psi) = 0.752$, $\psi = 0.00$ (EC3 Tab.6.6)

$f = 1 - 0.5(1 - k_c) [1 - 2.0(\bar{\lambda}, l_t - 0.8)^2] = 1 - 0.5 \times (1 - 0.752) [1 - 2.0 \times (0.810 - 0.8)^2] = 0.876$, $f \leq 1.0$

$\chi, l_t, \text{mod} = \chi, l_t / f = 0.757 / 0.876 = 0.864$, $\chi, l_t, \text{mod} \leq 1.0$, $\chi, l_t, \text{mod} \leq 1.52$, $\chi, l_t, \text{mod} = 0.864$

$M_{b,rd} = \chi, l_t \cdot W_{pl,y} \cdot f_y / \gamma_{M1} = 0.864 \times [10^{-6}] \times 2194.0 \times 10^3 \times 355 / 1.00 = 672.94 \text{ kNm}$ (EC3 Eq.6.55)

$M_{y,ed} = 35.46 \text{ kNm} < 672.94 \text{ kNm} = M_{b,rd}$, Is verified

14. Haunch verification (Ultimate Limit State)

(EN1993-1-1, §6)

The haunch is fabricated by cutting and welding of an IPE 500 section - S 355

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

	at haunch end	at haunch-middle	at haunch-start
Ned =	92.6 kN	91.9 kN	89.0 kN
Ved =	96.6 kN	84.1 kN	75.1 kN
Myed =	348.4 kNm	254.5 kNm	171.2 kNm

Buckling length, In-plane buckling $L_{cr,y}=2400\text{mm}$
 Buckling length, Out-of-plane buckling $L_{cr,z}=2400\text{mm}$

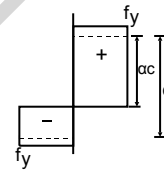
14.1. Classification of cross-sections, at haunch end

(EN1993-1-1, §5.5)

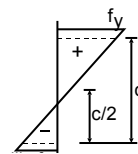
Maximum and minimum cross-section stresses $\sigma=Ned/Ael \pm Myed/Wel.y \pm Mzed/Wel.z$
 $\sigma=[10^{-3}]93/16274 \pm [10^{-6}]348/4640.7 \times 10^3 \pm [10^{-6}]0/214.2 \times 10^3$
 $\sigma_1=81 \text{ N/mm}^2, \sigma_2=-69 \text{ N/mm}^2$ (compression positive)

Web

$c=1000.0-2 \times 16.0-2 \times 21.0=926.0 \text{ mm}$, $t=10.2 \text{ mm}$, $c/t=926.0/10.2=90.78$
 S 355, $t=10.2 \leq 40 \text{ mm}$, $f_y=355 \text{ N/mm}^2$, $\epsilon=(235/355)^{0.5}=0.81$
 Position of neutral axis for combined Bending and compression
 $Ned/(2tw \cdot f_y/\gamma M_0)=92600/(2 \times 10.2 \times 355/1.00)=12.8 \text{ mm}$
 $\alpha=(926.0/2+12.8)/926.0=0.514 > 0.5$
 $c/t=90.78 > 456 \times 0.81/(13 \times 0.514-1)=65.03$
 The web is not class 1 or 2

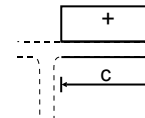


$\sigma=Ned/A \pm Myed \cdot (0.5d)/I_y$, $\sigma_1=75 \text{ N/mm}^2, \sigma_2=-64 \text{ N/mm}^2$
 $\psi=-64/75=-0.850 > -1$
 $c/t=90.78 > 42 \times 0.81/(0.67+0.33 \times -0.850)=87.34$
 The web is not class 3
 The web is class 4 (EN1993-1-1, Tab.5.2)



Flange

$c=200.0/2-10.2/2-21.0=73.9 \text{ mm}$, $t=16.0 \text{ mm}$, $c/t=73.9/16.0=4.62$
 S 355, $t=16.0 \leq 40 \text{ mm}$, $f_y=355 \text{ N/mm}^2$, $\epsilon=(235/355)^{0.5}=0.81$
 $c/t=4.62 \leq 9 \times \epsilon=9 \times 0.81=7.29$
 The flange is class 1 (EN1993-1-1, Tab.5.2)



Overall classification of cross-section is Class 4, Bending and compression $N_{c,ed} + M_{y,ed}$

Effective cross-section properties of Class 4 cross-sections

(EN1993-1-1, §6.2.2.5)

Web

$\bar{\lambda}_p=(b/t)/[28.40 \epsilon \sqrt{K\sigma}]$ (EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3)
 $b=d=926.0\text{mm}$, $t=10.2\text{mm}$, $\epsilon=0.81$, $\psi=1.00$, $K\sigma=4.00$, $\bar{\lambda}_p=1.973$
 $\bar{\lambda}_p=1.973 > 0.673$ $\rho=[1-0.055(3+1.00)/1.973]/1.973=0.450$ ($\rho < 1.0$), $deff=\rho \cdot d=0.450 \times 926=417.0 \text{ mm}$
 Effective area $A_{eff}=16274-1 \times (926.0-417.0) \times 10.20=11081 \text{ mm}^2$

Web

$\bar{\lambda}_p=(b/t)/[28.40 \epsilon \sqrt{K\sigma}]$ (EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3)
 $b=d=926.0\text{mm}$, $t=10.2\text{mm}$, $\epsilon=0.81$, $\psi=-1.00$, $K\sigma=23.90$, $\bar{\lambda}_p=0.807$
 $\bar{\lambda}_p=0.807 > 0.673$ $\rho=[1-0.055(3+-1.00)/0.807]/0.807=1.070$ ($\rho < 1.0$), $heff=\rho \cdot d/2=1.000 \times 463=463.0 \text{ mm}$
 Effective area $A_{eff}=16274-1 \times (463.0-463.0) \times 10.20=16274 \text{ mm}^2$
 $e_{my}277.80 \times (16274/16274-1)=0.00 \text{ mm}$, $I_{y,eff}=2320.3 \times 10^6 \text{ mm}^4$
 Effective section modulus $W_{y,eff}=2320.3 \times 10^6/(1000.0/2+0.00)=4640.7 \times 10^3 \text{ mm}^3$

14.2. Resistance of cross-section, at haunch end (Ultimate Limit State) (EN1993-1-1, §6.2)**Effective cross-section properties of Class 4 cross-sections** (EN1993-1-1, §6.2.2.5)

Web

$$\bar{\lambda}_p = (b/t) / [28.40 \varepsilon \sqrt{K\sigma}] \quad (\text{EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3})$$

$$b=d=926.0\text{mm}, t=10.2\text{mm}, \varepsilon=0.81, \psi=1.00, K\sigma=4.00, \bar{\lambda}_p=1.973$$

$$\bar{\lambda}_p=1.973 > 0.673 \quad \rho = [1 - 0.055(3+1.00)/1.973] / 1.973 = 0.450 \quad (\rho < 1.0), \text{deff} = \rho \cdot d = 0.450 \times 926 = 417.0 \text{ mm}$$

$$\text{Effective area } A_{\text{eff}} = 16274 - 1 \times (926.0 - 417.0) \times 10.20 = 11081 \text{ mm}^2$$

Ultimate Limit State, Verification for compression (EN1993-1-1, §6.2.4)

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2

Nc.ed= 93.70 kN

$$\text{Compression Resistance } N_{\text{crd}} = A_{\text{eff}} \cdot f_y / \gamma_{M0} = [10^{-3}] \times 11081 \times 355 / 1.00 = 3933.90 \text{ kN}$$

$$N_{\text{ed}} = 93.70 \text{ kN} < 3933.90 \text{ kN} = N_{\text{c,rd}}, \text{ Is verified}$$

Effective cross-section properties of Class 4 cross-sections (EN1993-1-1, §6.2.2.5)

Web

$$\bar{\lambda}_p = (b/t) / [28.40 \varepsilon \sqrt{K\sigma}] \quad (\text{EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3})$$

$$b=d=926.0\text{mm}, t=10.2\text{mm}, \varepsilon=0.81, \psi=-1.00, K\sigma=23.90, \bar{\lambda}_p=0.807$$

$$\bar{\lambda}_p=0.807 > 0.673 \quad \rho = [1 - 0.055(3+-1.00)/0.807] / 0.807 = 1.070 \quad (\rho < 1.0), \text{heff} = \rho \cdot d / 2 = 1.000 \times 463 = 463.0 \text{ mm}$$

$$\text{Effective area } A_{\text{eff}} = 16274 - 1 \times (463.0 - 463.0) \times 10.20 = 16274 \text{ mm}^2$$

$$e_{\text{my}} = 277.80 \times (16274 / 16274 - 1) = 0.00 \text{ mm}, I_{y,\text{eff}} = 2320.3 \times 10^6 \text{ mm}^4$$

$$\text{Effective section modulus } W_{y,\text{eff}} = 2320.3 \times 10^6 / (1000.0 / 2 + 0.00) = 4640.7 \times 10^3 \text{ mm}^3$$

Ultimate Limit State, Verification for bending moment y-y (EN1993-1-1, §6.2.5)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

My.ed=348.40 kNm

$$\text{Bending Resistance } M_{\text{c,y,rd}} = W_{\text{eff,y}} \cdot f_y / \gamma_{M0} = [10^{-6}] \times 4640.7 \times 10^3 \times 355 / 1.00 = 1647.43 \text{ kNm}$$

$$M_{y,\text{ed}} = 348.40 \text{ kNm} < 1647.43 \text{ kNm} = M_{y,\text{rd}} = M_{\text{p,y,rd}}, \text{ Is verified}$$

Ultimate Limit State, Verification for shear z (EN1993-1-1, §6.2.6)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

Vz.ed= 96.60 kNm

$$A_v = A - 2b \cdot t_f + (t_w + 2r) t_f = 16274 - 2 \times 200.0 \times 16.0 + (10.2 + 2 \times 21.0) \times 16.0 = 10709 \text{ mm}^2 \quad (\text{EC3 §6.2.6.3})$$

$$A_v = 10709 \text{ mm}^2 > \eta \cdot h_w \cdot t_w = 1.00 \times (1000.0 - 2 \times 16.0) \times 10.2 = 1.00 \times 984.0 \times 10.2 = 10037 \text{ mm}^2$$

$$\text{Plastic Shear Resistance } V_{\text{pl,z,rd}} = A_v \cdot (f_y / \sqrt{3}) / \gamma_{M0} = [10^{-3}] \times 10709 \times (355 / 1.73) / 1.00 = 2194.87 \text{ kN}$$

$$V_{z,\text{ed}} = 96.60 \text{ kN} < 2194.87 \text{ kN} = V_{z,\text{rd}} = V_{\text{pl,z,rd}}, \text{ Is verified}$$

$$h_w / t_w = (1000.0 - 2 \times 16.0) / 10.2 = 984.0 / 10.2 = 96.47 > 72 \times 0.81 / 1.00 = 72 \varepsilon / \eta = 58.32 \quad (\eta = 1.00)$$

$$S_{355}, t = 10.2 \leq 40 \text{ mm}, f_y = 355 \text{ N/mm}^2, \varepsilon = (235 / 355)^{0.5} = 0.81$$

$$\text{Shear buckling resistance must be verified} \quad (\text{EC3 §6.2.6.6})$$

Shear buckling resistance

(EC3 EN1993-1-5:2006, §5)

$$\bar{\lambda}_w = (926.0 / 10.2) / (37.4 \times 0.81 \times \sqrt{5.34}) = 1.297, K_t = 5.34 \quad (\text{EC3-1-5 §5, Eq.5.6, A.3})$$

$$\bar{\lambda}_w = 1.297 \geq 1.08, \chi_w = 0.83 / 1.297 = 0.640 \quad (\text{EC3-1-5 Tab.5.1})$$

$$V_{b,\text{rd}} = \chi_w \cdot f_{yw} \cdot h_w \cdot t / (\sqrt{3} \gamma_{M1}) = 0.001 \times 355 \times 0.640 \times 926.0 \times 10.2 / (1.73 \times 1.00) = 1239.04 \text{ kN} \quad (\text{EC3-1-5 Tab.5.1})$$

$$V_{\text{ed}} = 97 \text{ kN} < 1239 = V_{b,\text{rd}} \text{ kN}, \text{ Is verified}$$

Ultimate Limit State, Verification for axial force, shear and bending (EN1993-1-1, §6.2.9)

Maximum design values. Verification for load case: L.C. 202: 1.35Gk+1.50Qs1

N.ed= 92.60kN (Compression), Vz.ed= 96.60kNm, My.ed= 348.40kN

$$N_{\text{plrd}} = 3933.90 \text{ kN}, M_{\text{c,y,rd}} = 1647.43 \text{ kNm}, V_{\text{pl,z,rd}} = 1239.04 \text{ kN}$$

$$N_{\text{ed}} = 92.60 \text{ kN} \leq 0.25 \times 3933.90 = 0.25 \times N_{\text{plrd}} = 983.47 \text{ kN}$$

$$N_{\text{ed}} = 92.60 \text{ kN} \leq [10^{-3}] \times 0.5 \times 984.0 \times 10.2 \times 355 / 1.00 = 0.5 h_w \cdot t_w \cdot f_y / \gamma_{M0} = 1781.53 \text{ kN}$$

$$n = N_{\text{ed}} / N_{\text{plrd}} = 93 / 3934 = 0.024$$

$$\text{Effect of axial force is neglected} \quad (\text{EC3 §6.2.9.1 Eq.6.33, Eq.6.34, Eq.6.35})$$

$$V_{\text{ed}} = 96.60 \text{ kN} \leq 0.50 \times 1239.04 = 0.50 \times V_{\text{pl,rd}} = 619.52 \text{ kN}$$

$$\text{Effect of shear force is neglected} \quad (\text{EC3 §6.2.8.2})$$

Maximum and minimum cross-section stresses $\sigma = N_{ed}/A_{eff} \pm M_{y,ed}/W_{eff,y} \pm M_{z,ed}/W_{eff,z}$
 $\sigma = [10^{-3}]0/11081 \pm [10^{-6}]348/4640.7 \times 10^3 \pm [10^{-6}]0/214.2 \times 10^3$
 $\sigma_1 = 75 \text{ N/mm}^2, \sigma_2 = -75 \text{ N/mm}^2$ (compression positive)
 $\sigma_{x,ed} = 75 < 355/1.00 = 355 = f_y/\gamma_{M0} \text{ N/mm}^2, \text{ Is verified}$ (EC3 Eq.6.43, Eq.6.44)

14.3. Out-of-plane buckling, at haunch end (Ultimate Limit State) (EN1993-1-1, §6.3.2.4)

We check an equivalent T-section for the compressive part of the haunch section
 The equivalent T-section is made of the bottom flange and 1/3 of the compressed part of the web
Properties of equivalent T-section

Depth of cross section	hf =	167 mm
Width of cross section	bf =	200 mm
Web thickness	tw =	10.20 mm
Flange thickness	tf =	16.00 mm
Area	Af =	4737 mm ²
Second moment of area	If,z =	10.667x10 ⁶ mm ⁴
Radius of gyration	if,z =	$\sqrt{(10.667 \times 10^6 / 4737)} = 47.5 \text{ mm}$

Compression in the T-section

Maximum design values. Verification for load case: L.C. 212: 1.35xGk+1.50Qs1+0.90Qw2
 $N_{ed,f} = N_{ed} \cdot A_f/A + M_{ed} \cdot A_f/W_{el,y} = 92.6 \times 4737 / 16274 + 348.4 \times 4737 \times 10^3 / 4640.7 \times 10^3 = 382.6 \text{ kN}$

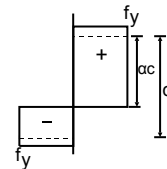
$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \sqrt{(A_{eff}/A) / \lambda_1} = (2400 / 47.5) \times (1.000 / 76.06) = 0.665$
 $f_{z-f,z}$ buckling curve: c, imperfection factor: $\alpha_{f,z} = 0.49, \chi_{f,z} = 0.746$ (T.6.2, T.6.1, Fig.6.4)
 $\Phi_{f,z} = 0.5 [1 + \alpha_{f,z} (\bar{\lambda}_{f,z} - 0.2) + \bar{\lambda}_{f,z}^2] = 0.5 [1 + 0.49 \times (0.665 - 0.2) + 0.665^2] = 0.835$
 $\chi_{f,z} = 1 / [\Phi_{f,z} + \sqrt{(\Phi_{f,z}^2 - \bar{\lambda}_{f,z}^2)}] = 1 / [0.835 + \sqrt{(0.835^2 - 0.665^2)}] = 0.746 < 1, \chi_{f,z} = 0.746$
 $N_{b,rd} = \chi_z \cdot A \cdot f_y / \gamma_{M1} = 0.746 \times 16274 \times 355 / 1.00 = 1254.45 \text{ kN}$ (EC3 Eq.6.47)
 $N_{c,ed} = 382.57 \text{ kN} < 1254.45 \text{ kN} = N_{b,rd}, \text{ Is verified}$

14.4. Classification of cross-sections, at haunch-middle (EN1993-1-1, §5.5)

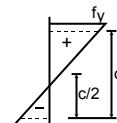
Maximum and minimum cross-section stresses $\sigma = N_{ed}/A_{el} \pm M_{y,ed}/W_{el,y} \pm M_{z,ed}/W_{el,z}$
 $\sigma = [10^{-3}]92/13724 \pm [10^{-6}]255/3138.1 \times 10^3 \pm [10^{-6}]0/214.0 \times 10^3$
 $\sigma_1 = 88 \text{ N/mm}^2, \sigma_2 = -74 \text{ N/mm}^2$ (compression positive)

Web

$c = 750.0 - 2 \times 16.0 - 2 \times 21.0 = 676.0 \text{ mm}, t = 10.2 \text{ mm}, c/t = 676.0 / 10.2 = 66.27$
 S 355, $t = 10.2 \leq 40 \text{ mm}, f_y = 355 \text{ N/mm}^2, \epsilon = (235/355)^{0.5} = 0.81$
 Position of neutral axis for combined Bending and compression
 $N_{ed} / (2t_w \cdot f_y / \gamma_{M0}) = 91900 / (2 \times 10.2 \times 355 / 1.00) = 12.7 \text{ mm}$
 $\alpha = (676.0 / 2 + 12.7) / 676.0 = 0.519 > 0.5$
 $c/t = 66.27 > 456 \times 0.81 / (13 \times 0.519 - 1) = 64.30$
 The web is not class 1 or 2

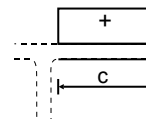


$\sigma = N_{ed}/A + M_{y,ed} \cdot (0.5d) / I_y, \sigma_1 = 80 \text{ N/mm}^2, \sigma_2 = -66 \text{ N/mm}^2$
 $\psi = -66 / 80 = -0.830 > -1$
 $c/t = 66.27 \leq 42 \times 0.81 / (0.67 + 0.33 \times -0.830) = 85.89$
 The web is class 3 (EN1993-1-1, Tab.5.2)



Flange

$c = 200.0 / 2 - 10.2 / 2 - 21.0 = 73.9 \text{ mm}, t = 16.0 \text{ mm}, c/t = 73.9 / 16.0 = 4.62$
 S 355, $t = 16.0 \leq 40 \text{ mm}, f_y = 355 \text{ N/mm}^2, \epsilon = (235/355)^{0.5} = 0.81$
 $c/t = 4.62 \leq 9 \epsilon = 9 \times 0.81 = 7.29$
 The flange is class 1 (EN1993-1-1, Tab.5.2)



Overall classification of cross-section is Class 3, Bending and compression $N_{c,ed} + M_{y,ed}$

14.5. Resistance of cross-section, at haunch-middle (Ultimate Limit State) (EN1993-1-1, §6.2)**Ultimate Limit State, Verification for compression** (EN1993-1-1, §6.2.4)

Maximum design values. Verification for load case: L.C. 212: $1.35xGk+1.50Qs1+0.90Qw2$

Nc.ed= 91.90 kN

Compression Resistance $N_{plrd} = A \cdot f_y / \gamma_{M0} = [10^{-3}] \times 13724 \times 355 / 1.00 = 4871.88 \text{ kN}$

$N_{ed} = 91.90 \text{ kN} < 4871.88 \text{ kN} = N_{c,rd} = N_{plrd}$, Is verified

Ultimate Limit State, Verification for bending moment y-y (EN1993-1-1, §6.2.5)

Maximum design values. Verification for load case: L.C. 202: $1.35Gk+1.50Qs1$

My.ed=267.90 kNm

Bending Resistance $M_{ely,rd} = W_{ely} \cdot f_y / \gamma_{M0} = [10^{-6}] \times 3138.1 \times 10^3 \times 355 / 1.00 = 1114.01 \text{ kNm}$

$M_{y,ed} = 267.90 \text{ kNm} < 1114.01 \text{ kNm} = M_{y,rd} = M_{ply,rd}$, Is verified

Ultimate Limit State, Verification for shear z (EN1993-1-1, §6.2.6)

Maximum design values. Verification for load case: L.C. 202: $1.35Gk+1.50Qs1$

Vz.ed= 85.90 kNm

$A_v = A - 2b \cdot t_f + (t_w + 2r) t_f = 13724 - 2 \times 200.0 \times 16.0 + (10.2 + 2 \times 21.0) \times 16.0 = 8159 \text{ mm}^2$ (EC3 §6.2.6.3)

$A_v = 8159 \text{ mm}^2 > \eta \cdot h_w \cdot t_w = 1.00 \times (750.0 - 2 \times 16.0) \times 10.2 = 1.00 \times 734.0 \times 10.2 = 7487 \text{ mm}^2$

Plastic Shear Resistance $V_{pl,z,rd} = A_v (f_y / \sqrt{3}) / \gamma_{M0} = [10^{-3}] \times 8159 \times (355 / 1.73) / 1.00 = 1672.22 \text{ kN}$

$V_{z,ed} = 85.90 \text{ kN} < 1672.22 \text{ kN} = V_{z,rd} = V_{pl,z,rd}$, Is verified

$h_w / t_w = (750.0 - 2 \times 16.0) / 10.2 = 734.0 / 10.2 = 71.96 > 72 \times 0.81 / 1.00 = 72 \epsilon / \eta = 58.32$ ($\eta = 1.00$)

S 355, $t = 10.2 \leq 40 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$, $\epsilon = (235 / 355)^{0.5} = 0.81$

Shear buckling resistance must be verified (EC3 §6.2.6.6)

Shear buckling resistance (EC3 EN1993-1-5:2006, §5)

$\bar{\lambda}_w = (676.0 / 10.2) / (37.4 \times 0.81 \times \sqrt{5.34}) = 0.947$, $K_t = 5.34$ (EC3-1-5 §5, Eq.5.6, A.3)

$0.83 / \eta \leq \bar{\lambda}_w = 0.947 < 1.08$, $\chi_v = 0.83 / 0.947 = 0.877$ ($\eta = 1.00$) (EC3-1-5 Tab.5.1)

$V_{b,rd} = \chi_v \cdot f_{yw} \cdot h_w \cdot t_w / (\sqrt{3} \gamma_{M1}) = 0.001 \times 355 \times 0.877 \times 676.0 \times 10.2 / (1.73 \times 1.00) = 1239.04 \text{ kN}$ (EC3-1-5 Tab.5.1)

$V_{ed} = 86 \text{ kN} < 1239 = V_{b,rd} \text{ kN}$, Is verified

Ultimate Limit State, Verification for axial force, shear and bending (EN1993-1-1, §6.2.9)

Maximum design values. Verification for load case: L.C. 212: $1.35xGk+1.50Qs1+0.90Qw2$

N.ed= 91.90kN (Compression), Vz.ed= 84.10kNm, My.ed= 254.50kN

$N_{plrd} = 4871.88 \text{ kN}$, $M_{el,y,rd} = 1114.01 \text{ kNm}$, $V_{pl,z,rd} = 1239.04 \text{ kN}$

$N_{ed} = 91.90 \text{ kN} \leq 0.25 \times 4871.88 = 0.25 \times N_{plrd} = 1217.97 \text{ kN}$

$N_{ed} = 91.90 \text{ kN} \leq [10^{-3}] \times 0.5 \times 734.0 \times 10.2 \times 355 / 1.00 = 0.5 h_w \cdot t_w \cdot f_y / \gamma_{M0} = 1328.91 \text{ kN}$

$n = N_{ed} / N_{plrd} = 92 / 4872 = 0.019$

Effect of axial force is neglected (EC3 §6.2.9.1 Eq.6.33, Eq.6.34, Eq.6.35)

$V_{ed} = 84.10 \text{ kN} \leq 0.50 \times 1239.04 = 0.50 \times V_{pl,rd} = 619.52 \text{ kN}$

Effect of shear force is neglected (EC3 §6.2.8.2)

Maximum and minimum cross-section stresses $\sigma = N_{ed} / A_{el} \pm M_{y,ed} / W_{el,y} \pm M_{z,ed} / W_{el,z}$

$\sigma = [10^{-3}] 0 / 13724 \pm [10^{-6}] 255 / 3138.1 \times 10^3 \pm [10^{-6}] 0 / 214.0 \times 10^3$

$\sigma_1 = 81 \text{ N/mm}^2$, $\sigma_2 = -81 \text{ N/mm}^2$ (compression positive)

$\sigma_{x,ed} = 81 < 355 / 1.00 = 355 = f_y / \gamma_{M0} \text{ N/mm}^2$, Is verified (EC3 Eq.6.42)

14.6. Out-of-plane buckling, at haunch-middle (Ultimate Limit State) (EN1993-1-1, §6.3.2.4)

We check an equivalent T-section for the compressive part of the haunch section

The equivalent T-section is made of the bottom flange and 1/3 of the compressed part of the web

Properties of equivalent T-section

Depth of cross section	hf =	125 mm
Width of cross section	bf =	200 mm
Web thickness	tw =	10.20 mm
Flange thickness	tf =	16.00 mm
Area	Af =	4312 mm ²
Second moment of area	If,z =	10.667 × 10 ⁶ mm ⁴
Radius of gyration	if,z =	$\sqrt{(10.667 \times 10^6 / 4312)} = 49.7 \text{ mm}$

Compression in the T-section

Maximum design values. Verification for load case: L.C. 212: $1.35 \times G_k + 1.50 Q_{s1} + 0.90 Q_{w2}$

$N_{ed,f} = N_{ed} \cdot A_f / A + M_{ed} \cdot A_f / W_{el,y} = 91.9 \times 4312 / 13724 + 235.5 \times 4312 \times 10^3 / 3138.1 \times 10^3 = 352.4 \text{ kN}$

$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \cdot (1 / \lambda_1) = (2400 / 49.7) \times (1 / 76.06) = 0.634$

$f_{z-f,z}$ buckling curve: c, imperfection factor: $\alpha_{f,z} = 0.49$, $\chi_{f,z} = 0.765$ (T.6.2, T.6.1, Fig.6.4)

$\Phi_{f,z} = 0.5 [1 + \alpha_{f,z} (\bar{\lambda}_{f,z} - 0.2) + \bar{\lambda}_{f,z}^2] = 0.5 [1 + 0.49 \times (0.634 - 0.2) + 0.634^2] = 0.807$

$\chi_{f,z} = 1 / [\Phi_{f,z} + \sqrt{(\Phi_{f,z}^2 - \bar{\lambda}_{f,z}^2)}] = 1 / [0.807 + \sqrt{(0.807^2 - 0.634^2)}] = 0.765 \leq 1$ $\chi_{f,z} = 0.765$

$N_{b,rd} = \chi_z \cdot A \cdot f_y / \gamma_{M1} = 0.765 \times 13724 \times 355 / 1.00 = 1170.98 \text{ kN}$

(EC3 Eq.6.47)

$N_{c,ed} = 352.40 \text{ kN} < 1170.98 \text{ kN} = N_{b,rd}$, Is verified

Steel Portal Frame EC3
Example Report

Connections15. Connection data

(EN1993-1-8)

15.1. Bolt connection data (eave, apex)

(EN1993-1-8)

Type of connection	End-plate connection, non-preloaded bolts	
Category of connection	Category A: Bearing type	(EC3-1-8 §3.4.1)
	Category D: Non-preloaded	(EC3-1-8 §3.4.2)
End Plate	Thickness $t_p=20$ mm, S 235	
Plate of Apex connection	200x706x20 mm, S 235	
Plate of Eave connection	200x1140x20 mm, S 235	
Bolts	M24, Strength grade 10.9	
Bolt diameter	$d = 24$ mm	
Diameter of holes	$d_o = 26$ mm	
Nominal area	$\pi d^2/4 = \pi \times 24^2/4 = 452.4$ mm ²	
Tensile stress area	$A_s = 353.0$ mm ²	
Bolt strength grade	10.9, $f_{yb}=900$ N/mm ² , $f_{ub}=1000$ N/mm ²	(EC3-1-8 §3.1.1)

15.2. Edge distances and spacing of bolts (eave, apex)

(EN1993-1-8, §3.5, Tab.3.3)

Minimum edge distances	$e_1=1.2d_o=1.2 \times 26=32$ mm $e_2=1.2d_o=1.2 \times 26=32$ mm
Maximum edge distances	$e_1=4t+40=4 \times 19.0+40=117$ mm $e_2=4t+40=4 \times 19.0+40=117$ mm
Minimum spacing of bolts	$p_1=2.2d_o=2.2 \times 26=58$ mm $p_2=2.4d_o=2.4 \times 26=63$ mm
Maximum spacing of bolts	$p_1=\min(14t, 200)=\min(14 \times 19.0, 200)=200$ mm $p_2=\min(14t, 200)=\min(14 \times 19.0, 200)=200$ mm
Distance of plate edge to bolt line	$e_1=e_2=e_x=50$ mm
Distance of section edge to bolt line	$e_c=45$ mm
Distance of flange edge to bolt line	$e_f=45$ mm
Pitch between bolt rows	$p_1=p_3=p=90$ mm
Spacing between cross centers	$p_2=g=w=100$ mm
Flange to end-plate weld	$a_{tf} \geq 0.55t_f=0.55 \times 16.0=9$ mm
Web to end-plate weld	$a_w \geq 0.55t_w=0.55 \times 10.2=6$ mm

15.3. Design resistance of individual bolts (eave, apex)

(EC3-1-8 §3.6.1, Tab.3.4)

Bolt strength grade=10.9,	$f_{ub}=1000$ N/mm ² , $A_s=353.0$ mm ² , $\gamma_{M2}=1.25$
Tension resistance of bolts	$F_{t,rd}=k_2 \cdot f_{ub} \cdot A_s / \gamma_{M2}$, ($k_2=0.90$) $F_{t,rd}=[10^{-3}] \times 0.90 \times 1000 \times 353.0 / 1.25=254$ kN
Shear resistance of bolts	$F_{v,rd}=\alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2}$, ($\alpha_v=0.50$) $F_{v,rd}=[10^{-3}] \times 0.50 \times 1000 \times 353.0 / 1.25=141$ kN

16. Apex connection

16.1. Basic data (Apex connection)

Design forces of connection (Apex connection)

Maximum design values for actions (L.C. 202: 1.35Gk+1.50Qs1)

Ned = -71.4 kN
 Ved = 24.6 kN
 Med = 135.6 kNm

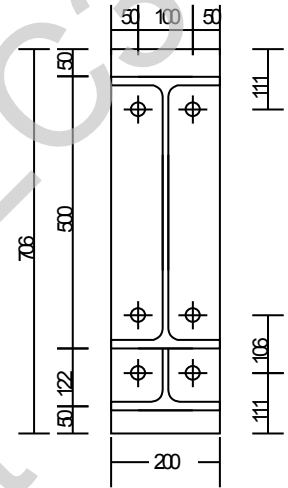
16.2. Connection data (Apex connection)

Bolt connection data

End Plate 200x706x20 mm, S 235
 Bolts M24, Bolt strength grade 10.9
 Number of Bolts top 2x1=2
 bottom 2x2=4
 Total number of bolts =6
 Diameter of holes do = 26 mm
 Shear plane of bolt through the threaded portion

Edge distances and spacing of bolts

Distance of plate edge to bolt line e1=e2=ex= 50 mm
 Distance of section edge to bolt line ec= 45 mm
 Distance of flange enge to bolt line ef= 45 mm
 Pitch between bolt rows p1=p3=p= 90 mm
 Spacing between cross centers p2=g =w= 100 mm
 Flange to end-plate weld atf>= 0.55tf=0.55x16.0= 9 mm
 Web to end-plate weld aw>= 0.55tw=0.55x10.2= 6 mm



16.3. Connection geometry of end-plate (Apex connection)

(EC3-1-8 §6.2.4.1, Fig.6.2)

e=ex=50 mm, emin=50 mm
 $m_x, x = (100 - 10.2 - 2 \times 0.8 \times 6 \times \sqrt{2}) / 2 = 38.1$ mm
 $m_x, y = 45 - 0.8 \times 9 \times \sqrt{2} = 34.8$ mm
 $n_x, x = \text{emin} \leq 1.25m_x, x = \min(50.0, 1.25 \times 38.1) = 47.6$ mm
 $n_x, y = \text{emin} \leq 1.25m_x, y = \min(50.0, 1.25 \times 34.8) = 43.5$ mm
 $\min(m_x, x, m_x, y) = \min(38.1, 34.8) = 34.8$ mm, $\max(m_x, x, m_x, y) = \max(38.1, 34.8) = 38.1$ mm
 $\min(n_x, x, n_x, y) = \min(47.6, 43.5) = 43.5$ mm, $\max(n_x, x, n_x, y) = \max(47.6, 43.5) = 47.6$ mm

16.4. Effective lengths of end-plate (Apex connection)

(EC3-1-8 §6.2.6.5 Tab.6.6)

Bolt-row outside tension flange of beam

$l_{eff} = 2\pi \cdot m_x = 2\pi \times 34.8 = 218.7$ mm
 $= \pi \cdot m_x + w = \pi \times 34.8 + 100.0 = 209.3$ mm
 $= \pi \cdot m_x + 2e = \pi \times 34.8 + 2 \times 50.0 = 209.3$ mm
 $= 4m_x + 1.25e_x = 4 \times 34.8 + 1.25 \times 50.0 = 201.7$ mm
 $= e + 2m_x + 0.625e_x = 50.0 + 2 \times 34.8 + 0.625 \times 50.0 = 150.8$ mm
 $= 0.5b_p = 0.5 \times 200 = 100.0$ mm
 $= 0.5w + 2m_x + 0.625e_x = 0.5 \times 100.0 + 2 \times 34.8 + 0.625 \times 50.0 = 150.8$ mm
 $l_{eff,1b} = \min(218.7, 209.3, 209.3, 201.7, 150.8, 100.0, 150.8) = 100.0$ mm
 $l_{eff,1b} = 100.0$ mm

Bolt next to tension flange alone

$l_{eff} = 2\pi \cdot m_x = 2\pi \times 34.8 = 218.7$ mm
 $= \alpha \cdot m = 6.28 \times 34.8 = 218.7$ mm ($\lambda_1 = \lambda_2 = m / (m + e) = 0.41$, $\alpha = 6.28$)
 $l_{eff,2b} = \min(218.7, 218.7) = 218.7$ mm
 $l_{eff,2b} = 218.7$ mm

(EC3-1-8 Fig.6.11)

Bolt next to tension flange in a group

$$\begin{aligned} l_{eff} &= 2\pi \cdot m_x = 2\pi \times 34.8 = 218.7 \text{ mm} \\ &= \alpha \cdot m = 6.28 \times 34.8 = 218.7 \text{ mm} \quad (\lambda_1 = \lambda_2 = m / (m + e) = 0.41, \alpha = 6.28) \\ &= \pi m + p = \pi \times 34.8 + 90.0 = 199.3 \text{ mm} \\ &= 0.5p + \alpha \cdot m - (2m + 0.625e) = 0.5 \times 90.0 + 6.3 \times 34.8 - (2 \times 34.8 + 0.625 \times 50.0) = 162.8 \text{ mm} \\ l_{eff,3b} &= \min(218.7, 218.7, 199.3, 162.8) = 162.8 \text{ mm} \\ l_{eff,3b} &= 162.8 \text{ mm} \end{aligned}$$

Inner Bolt-row in a group

$$\begin{aligned} l_{eff} &= 2\pi \cdot m_x = 2\pi \times 38.1 = 239.4 \text{ mm} \\ &= 4m + 1.25e = 4 \times 38.1 + 1.25 \times 50.0 = 214.9 \text{ mm} \\ &= 2p = 2 \times 90.0 = 180.0 \text{ mm} \\ &= p = 90.0 \text{ mm} \\ l_{eff,4b} &= \min(239.4, 214.9, 180.0, 90.0) = 90.0 \text{ mm} \\ l_{eff,4b} &= 90.0 \text{ mm} \end{aligned}$$

16.5. End-Plate, Resistance of T-stub flange (Apex connection)

(EC3-1-8 §6.2.4.1, Tab.6.2)

Bolt-row outside tension flange of beam

$$\begin{aligned} M_{pl,1,rd} &= M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 100.0 \times 20.0^2 \times 235 / 1.00 = 2.350 \text{ kNm} \\ \text{Mode 1} \quad F_{t,1,rd} &= 4M_{pl,1,rd} / m = [10^3] \times 4 \times 2.350 / 34.8 = 270 \text{ kN} \\ \text{Mode 2} \quad F_{t,2,rd} &= (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 2.350 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 342 \text{ kN} \\ \text{Mode 3} \quad F_{t,3,rd} &= \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN} \\ F_{t,rd} &= \min(270, 342, 508) = 270 \text{ kN} \end{aligned}$$

Bolt next to tension flange alone

$$\begin{aligned} M_{pl,1,rd} &= M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 218.7 \times 20.0^2 \times 235 / 1.00 = 5.139 \text{ kNm} \\ \text{Mode 1} \quad F_{t,1,rd} &= 4M_{pl,1,rd} / m = [10^3] \times 4 \times 5.139 / 34.8 = 591 \text{ kN} \\ \text{Mode 2} \quad F_{t,2,rd} &= (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 5.139 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 413 \text{ kN} \\ \text{Mode 3} \quad F_{t,3,rd} &= \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN} \\ F_{t,rd} &= \min(591, 413, 508) = 413 \text{ kN} \end{aligned}$$

Bolt next to tension flange in a group

$$\begin{aligned} M_{pl,1,rd} &= M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 162.8 \times 20.0^2 \times 235 / 1.00 = 3.826 \text{ kNm} \\ \text{Mode 1} \quad F_{t,1,rd} &= 4M_{pl,1,rd} / m = [10^3] \times 4 \times 3.826 / 34.8 = 440 \text{ kN} \\ \text{Mode 2} \quad F_{t,2,rd} &= (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 3.826 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 380 \text{ kN} \\ \text{Mode 3} \quad F_{t,3,rd} &= \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN} \\ F_{t,rd} &= \min(440, 380, 508) = 380 \text{ kN} \end{aligned}$$

Inner Bolt-row in a group

$$\begin{aligned} M_{pl,1,rd} &= M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 90.0 \times 20.0^2 \times 235 / 1.00 = 2.115 \text{ kNm} \\ \text{Mode 1} \quad F_{t,1,rd} &= 4M_{pl,1,rd} / m = [10^3] \times 4 \times 2.115 / 38.1 = 222 \text{ kN} \\ \text{Mode 2} \quad F_{t,2,rd} &= (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 2.115 + 47.6 \times 2 \times 254) / (38.1 + 47.6) = 332 \text{ kN} \\ \text{Mode 3} \quad F_{t,3,rd} &= \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN} \\ F_{t,rd} &= \min(222, 332, 508) = 222 \text{ kN} \end{aligned}$$

16.6. Rafter flange and web in compression (Apex connection)

(EC3-1-8 §6.2.6.7)

$$\begin{aligned} F_{c,fb,rd} &= M_{c,rd} / (h - t_f), \quad M_{c,rd} = W_{el,y} \cdot f_y / \gamma_{M0} \\ W_{el,y} &= (200 \times 16.0 \times 590.0^2 + 10.2 \times 574.0^3 / 6) / 606 = 2368.7 \times 10^3 \text{ mm}^3 \\ M_{c,rd} &= [10^{-6}] \times 2368.7 \times 10^3 \times 355 / 1.00 = 841 \text{ kNm}, \quad F_{c,fb,rd} = [10^3] \times 841 / 590.0 = 1425 \text{ kN} \\ F_{c,fb,rd,max} &= (1/0.8) b \cdot t \cdot f_y / \gamma_{M0} = (1/0.8) \times [10^{-3}] \times 200.0 \times 16.0 \times 235 / 1.00 = 940 \text{ kN} \quad (h > 600 \text{ mm}) \\ F_{c,fb,rd} &= \min(1425, 940) = 940 \text{ kN} \end{aligned}$$

16.7. Rafter web in tension (Apex connection)

(EC3-1-8 §6.2.6.8)

$$\begin{aligned} F_{t,wb,rd} &= b_{eff,t,wb} \cdot t_{wb} \cdot f_y / \gamma_{M0} \\ b_{eff,t,wb} &= l_{eff,3b} = \min(l_{eff,3b}, l_{eff,4b}) = \min(162.8, 90.0) = 90.0 \text{ mm} \\ F_{t,wb,rd} &= [10^{-3}] \times 90.0 \times 10.2 \times 355 / 1.00 = 326 \text{ kN} \end{aligned}$$

$$\min F_{t,rd} = \min(270, 413, 380, 222, 326) = 222 \text{ kN}$$

16.8. Moment resistance of connection (Apex connection)

(EN1993-1-8, §6.2.7.2)

$$M_{j,rd} = \Sigma hr \cdot F_{t,rd}$$

(EN1993-1-8, §6.2.7.2Eq.6.25)

hr: row numbering from bottom, distances from center of top (compression) flange

End-plate in bending

(EC3-1-8 §6.2.4.5)

Force distribution in bolt rows

Bolt-row 1, $hr = 537.0$ mm, $F_{t,rd} = 380$ kNBolt-row 2, $hr = 431.0$ mm, $F_{t,rd} = 222$ kNBolt-row 3, $hr = 53.0$ mm, $F_{t,rd} = 413$ kN $F_{c,ed} = \Sigma F_{t,rd} = 380 + 222 + 413 = 1015$ kNRafter web in tension

(EC3-1-8 §6.2.6.8)

 $F_{t,wb,rd} = 326$ kNRafter flange and web in compression

(EC3-1-8 §6.2.4.7)

 $F_{c,fb,rd} = 940$ kN $F_{t,rd} \leq F_{t,wb,rd} = 326$ kN, $F_{c,ed} = \Sigma F_{t,rd} \leq F_{c,fb,rd} = 940$ kNForce distribution in bolt rows

(EC3-1-8 §6.2.7.2.(7))

Bolt-row 1, $hr = 537.0$ mm, $F_{t,rd} = 326$ kNBolt-row 2, $hr = 431.0$ mm, $F_{t,rd} = 222$ kNBolt-row 3, $hr = 53.0$ mm, $F_{t,rd} = 326$ kN $F_{c,ed} = \Sigma F_{t,rd} = 326 + 222 + 326 = 874$ kNMoment resistance of connection

(EN1993-1-8, §6.2.7.2(10))

$$M_{j,rd} = [10^{-3}] \times [326 \times 537.0 + 222 \times 431.0 + 326 \times 53.0]$$

 $M_{j,rd} = 288$ kNm $M_{ed} = 135.6$ kNm < 288.0 kNm = $M_{j,rd}$, Is verified**16.9. Shear resistance (Apex connection)**

(EN1993-1-8, §3.6.1 Tab.3.4)

Shear resistance of bolts

$$F_{v,rd} = \alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2} = [10^{-3}] \times 0.50 \times 1000 \times 353.0 / 1.25 = 141$$
 kN

Shear plane of bolt: through the threaded portion

Bearing resistance of bolts

$$F_{b,rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2}$$

 $t = 20.0$ mm, $d = 24$ mm, $d_o = 26$ mm, $e_1 = 50$ mm, $e_2 = 50$ mm, $p_1 = 90$ mm, $f_{ub} = 1000$ kN/mm², $f_u = 360$ kN/mm², $\alpha_b = \min[f_{ub}/f_u, 1.0, e_1/3d_o, p_1/3d_o - 1/4] =$

$$= \min[1000/360, 1.0, 50/(3 \times 26), 90/(3 \times 26) - 0.25] = 0.64$$

 $k_1 = \min[2.8e_2/d_o - 1.7, 1.4p_2/d_o - 1.7, 2.5] = \min[2.8 \times 50/26 - 1.7, 1.4 \times 100/26 - 1.7, 2.5] = 2.50$ $F_{b,rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2} = [10^{-3}] \times 2.50 \times 0.64 \times 360 \times 24 \times 20.0 / 1.25 = 222$ kNDesign resistance of one bolt in shear = $\min(141, 222) = 141$ kNBending moment and shear

(EN1993-1-8, §3.6.1 Tab.3.4)

Maximum tension force in bolts

$$F_{t,ed} = 326/2 = 163$$
 kN

Reduction of shear resistance due to bending

$$\rho = 1 - F_{t,ed} / 1.40 F_{t,rd} = 1 - 163 / (1.40 \times 254) = 0.54$$

Shear acting together with bending moment for all the bolts

$$V_{rd} = 6 \times 0.54 \times 141 = 457$$
 kN

 $V_{ed} = 25$ kN < 457 kN = V_{rd} , Is verified

17. Eave connection

17.1. Basic data (Eave connection)

Design forces of connection ((Eave connection))

Maximum design values for actions (L.C. 202: 1.35Gk+1.50Qs1)

Ned = -75.5 kN
 Ved = 110.4 kN
 Med = -348.4 kNm

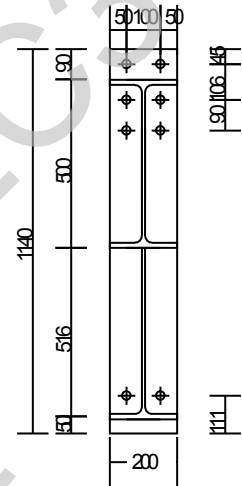
17.2. Connection data (Eave connection)

Bolt connection data

End Plate 200x1140x20 mm, S 235
 Bolts M24, Bolt strength grade 10.9
 Number of Bolts top 2x3=6
 bottom 2x1=2
 Total number of bolts =8
 Diameter of holes do = 26 mm
 Shear plane of bolt through the threaded portion

Edge distances and spacing of bolts

Distance of plate edge to bolt line e1=e2=ex= 50 mm
 Distance of section edge to bolt line ec= 45 mm
 Distance of flange enge to bolt line ef= 45 mm
 Pitch between bolt rows p1=p3=p= 90 mm
 Spacing between cross centers p2=g =w= 100 mm
 Flange to end-plate weld atf>= 0.55tf=0.55x16.0= 9 mm
 Web to end-plate weld aw>= 0.55tw=0.55x10.2= 6 mm



Compression stiffener at the bottom of haunch

Compression stiffener with thickness ts= 20.0 mm

17.3. Connection geometry of end-plate (Eave connection)

(EC3-1-8 §6.2.4.1, Fig.6.2)

e=ex=50 mm, emin=50 mm
 $mx,x=(100-10.2-2 \times 0.8 \times 6 \times \sqrt{2})/2= 38.1$ mm
 $mx,y=45-0.8 \times 9 \times \sqrt{2}= 34.8$ mm
 $nx,x=emin \le 1.25mx,x = \min(50.0, 1.25 \times 38.1=47.6)= 47.6$ mm
 $nx,y=emin \le 1.25mx,y = \min(50.0, 1.25 \times 34.8=43.5)= 43.5$ mm
 $\min(mx,x, mx,y)=\min(38.1, 34.8)=34.8$ mm, $\max(mx,x, mx,y)=\max(38.1, 34.8)=38.1$ mm
 $\min(nx,x, nx,y)=\min(47.6, 43.5)=43.5$ mm, $\max(nx,x, nx,y)=\max(47.6, 43.5)=47.6$ mm

17.4. Effective lengths of end-plate (Eave connection)

(EC3-1-8 §6.2.6.5 Tab.6.6)

Bolt-row outside tension flange of beam

$leff=2n \cdot mx = 2 \times 3 \times 34.8= 218.7$ mm
 $=n \cdot mx+w = 3 \times 34.8+100.0= 209.3$ mm
 $=n \cdot mx+2e=3 \times 34.8+2 \times 50.0= 209.3$ mm
 $=4mx+1.25ex = 4 \times 34.8+1.25 \times 50.0=201.7$ mm
 $=e+2mx+0.625ex = 50.0+2 \times 34.8+0.625 \times 50.0=150.8$ mm
 $=0.5bp = 0.5 \times 200= 100.0$ mm
 $=0.5w+2mx+0.625ex=0.5 \times 100.0+2 \times 34.8+0.625 \times 50.0= 150.8$ mm
 $leff,1b=\min(218.7, 209.3, 209.3, 201.7, 150.8, 100.0, 150.8)= 100.0$ mm
 $leff,1b= 100.0$ mm

Bolt next to tension flange alone

$leff=2n \cdot mx = 2 \times 3 \times 34.8= 218.7$ mm
 $=\alpha \cdot m = 6.28 \times 34.8=218.7$ mm ($\lambda 1=\lambda 2=m/(m+e)=0.41, \alpha=6.28$) (EC3-1-8 Fig.6.11)
 $leff,2b=\min(218.7, 218.7)= 218.7$ mm
 $leff,2b= 218.7$ mm

Bolt next to tension flange in a group

$l_{eff} = 2\pi \cdot m_x = 2\pi \times 34.8 = 218.7 \text{ mm}$
 $= \alpha \cdot m = 6.28 \times 34.8 = 218.7 \text{ mm} \quad (\lambda_1 = \lambda_2 = m / (m + e) = 0.41, \alpha = 6.28)$
 $= \pi m + p = \pi \times 34.8 + 90.0 = 199.3 \text{ mm}$
 $= 0.5p + \alpha \cdot m - (2m + 0.625e) = 0.5 \times 90.0 + 6.3 \times 34.8 - (2 \times 34.8 + 0.625 \times 50.0) = 162.8 \text{ mm}$
 $l_{eff,3b} = \min(218.7, 218.7, 199.3, 162.8) = 162.8 \text{ mm}$
 $l_{eff,3b} = 162.8 \text{ mm}$

Inner Bolt-row in a group

$l_{eff} = 2\pi \cdot m_x = 2\pi \times 38.1 = 239.4 \text{ mm}$
 $= 4m + 1.25e = 4 \times 38.1 + 1.25 \times 50.0 = 214.9 \text{ mm}$
 $= 2p = 2 \times 90.0 = 180.0 \text{ mm}$
 $= p = 90.0 \text{ mm}$
 $l_{eff,4b} = \min(239.4, 214.9, 180.0, 90.0) = 90.0 \text{ mm}$
 $l_{eff,4b} = 90.0 \text{ mm}$

17.5. End-Plate, Resistance of T-stub flange (Eave connection)

(EC3-1-8 §6.2.4.1, Tab.6.2)

Bolt-row outside tension flange of beam

$M_{pl,1,rd} = M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 100.0 \times 20.0^2 \times 235 / 1.00 = 2.350 \text{ kNm}$
Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 2.350 / 34.8 = 270 \text{ kN}$
Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 2.350 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 342 \text{ kN}$
Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN}$
 $F_{t,rd} = \min(270, 342, 508) = 270 \text{ kN}$

Bolt next to tension flange alone

$M_{pl,1,rd} = M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 218.7 \times 20.0^2 \times 235 / 1.00 = 5.139 \text{ kNm}$
Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 5.139 / 34.8 = 591 \text{ kN}$
Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 5.139 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 413 \text{ kN}$
Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN}$
 $F_{t,rd} = \min(591, 413, 508) = 413 \text{ kN}$

Bolt next to tension flange in a group

$M_{pl,1,rd} = M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 162.8 \times 20.0^2 \times 235 / 1.00 = 3.826 \text{ kNm}$
Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 3.826 / 34.8 = 440 \text{ kN}$
Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 3.826 + 43.5 \times 2 \times 254) / (34.8 + 43.5) = 380 \text{ kN}$
Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN}$
 $F_{t,rd} = \min(440, 380, 508) = 380 \text{ kN}$

Inner Bolt-row in a group

$M_{pl,1,rd} = M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 90.0 \times 20.0^2 \times 235 / 1.00 = 2.115 \text{ kNm}$
Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 2.115 / 38.1 = 222 \text{ kN}$
Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 2.115 + 47.6 \times 2 \times 254) / (38.1 + 47.6) = 332 \text{ kN}$
Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508 \text{ kN}$
 $F_{t,rd} = \min(222, 332, 508) = 222 \text{ kN}$

17.6. Rafter flange and web in compression (Eave connection)

(EC3-1-8 §6.2.6.7)

$F_{c,fb,rd} = M_{c,rd} / (h - t_f), \quad M_{c,rd} = W_{el,y} \cdot f_y / \gamma_{M0}$
 $W_{el,y} = (200 \times 16.0 \times 984.0^2 + 10.2 \times 968.0^3 / 6) / 1000 = 4640.4 \times 10^3 \text{ mm}^3$
 $M_{c,rd} = [10^{-6}] \times 4640.4 \times 10^3 \times 355 / 1.00 = 1647 \text{ kNm}, \quad F_{c,fb,rd} = [10^3] \times 1647 / 984.0 = 1674 \text{ kN}$
 $F_{c,fb,rd,max} = (1/0.8) b \cdot t \cdot f_y / \gamma_{M0} = (1/0.8) \times [10^{-3}] \times 200.0 \times 16.0 \times 235 / 1.00 = 940 \text{ kN} \quad (h > 600 \text{ mm})$
 $F_{c,fb,rd} = \min(1674, 940) = 940 \text{ kN}$

17.7. Rafter web in tension (Eave connection)

(EC3-1-8 §6.2.6.8)

$F_{t,wb,rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_y / \gamma_{M0}$
 $b_{eff,t,wb} = l_{eff,3b} = \min(l_{eff,3b}, l_{eff,4b}) = \min(162.8, 90.0) = 90.0 \text{ mm}$
 $F_{t,wb,rd} = [10^{-3}] \times 90.0 \times 10.2 \times 355 / 1.00 = 326 \text{ kN}$

$\min F_{t,rd} = \min(270, 413, 380, 222, 326) = 222 \text{ kN}$

17.8. Connection geometry of column-side (Eave connection)

(EC3-1-8 §6.2.4.1, Fig.6.2)

$e=e_x=50$ mm, $e_{min}=50$ mm
 $m_x,x=(100-12.0-2 \times 0.8 \times 24)/2=24.8$ mm
 $m_x,y=45-0.8 \times 9 \times \sqrt{2}=34.8$ mm
 $n_x,x=e_{min} \leq 1.25m_x,x = \min(50.0, 1.25 \times 24.8=31.0)=31.0$ mm
 $n_x,y=e_{min} \leq 1.25m_x,y = \min(50.0, 1.25 \times 34.8=43.5)=43.5$ mm
 $\min(m_x,x, m_x,y)=\min(24.8, 34.8)=24.8$ mm, $\max(m_x,x, m_x,y)=\max(24.8, 34.8)=34.8$ mm
 $\min(n_x,x, n_x,y)=\min(31.0, 43.5)=31.0$ mm, $\max(n_x,x, n_x,y)=\max(31.0, 43.5)=43.5$ mm

17.9. Effective lengths of column-side (Eave connection)

(EC3-1-8 §6.2.6.4 Tab.6.4)

End Bolt-row in a group

$l_{eff}=2\pi \cdot m = 2\pi \times 24.8 = 155.8$ mm
 $=\pi \cdot m + 2e_1 = \pi \times 24.8 + 2 \times 50.0 = 177.9$ mm
 $=4m + 1.25e = 4 \times 24.8 + 1.25 \times 50.0 = 161.7$ mm
 $=2m + 0.63e + e_1 = 2 \times 24.8 + 0.63 \times 50.0 + 50.0 = 130.8$ mm
 $=\pi \cdot m + p = \pi \times 24.8 + 90.0 = 167.9$ mm
 $=2e_1 + p = 2 \times 50.0 + 90.0 = 190.0$ mm
 $=2m + 0.63e + 0.5p = 2 \times 24.8 + 0.63 \times 50.0 + 0.5 \times 90.0 = 125.8$ mm
 $=e_1 + 0.5p = 50.0 + 0.5 \times 90.0 = 95.0$ mm
 $l_{eff,1c}=\min(155.8, 177.9, 161.7, 130.8, 167.9, 190.0, 125.8, 95.0)=95.0$ mm
 $l_{eff,1c} = 95.0$ mm

Inner Bolt-row in a group

$l_{eff}=2\pi \cdot m = 2\pi \times 24.8 = 155.8$ mm
 $=4m + 1.25e = 4 \times 24.8 + 1.25 \times 50.0 = 161.7$ mm
 $=2p = 2 \times 90.0 = 180.0$ mm
 $=p = 90.0$ mm
 $l_{eff,2c}=\min(155.8, 161.7, 180.0, 90.0)=90.0$ mm
 $l_{eff,2c} = 90.0$ mm

17.10. Column-Side, Resistance of T-stub flange (Eave connection)

(EC3-1-8 §6.2.4.1, Tab.6.2)

End Bolt-row in a group

$M_{pl,1,rd}=M_{pl,2,rd}=0.25l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 95.0 \times 19.0^2 \times 355 / 1.00 = 3.044$ kNm
 Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 3.044 / 24.8 = 491$ kN
 Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 3.044 + 31.0 \times 2 \times 254) / (24.8 + 31.0) = 391$ kN
 Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508$ kN
 $F_{t,rd} = \min(491, 391, 508) = 391$ kN

Inner Bolt-row in a group

$M_{pl,1,rd}=M_{pl,2,rd}=0.25l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 90.0 \times 19.0^2 \times 355 / 1.00 = 2.883$ kNm
 Mode 1 $F_{t,1,rd} = 4M_{pl,1,rd} / m = [10^3] \times 4 \times 2.883 / 24.8 = 465$ kN
 Mode 2 $F_{t,2,rd} = (2M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 2.883 + 31.0 \times 2 \times 254) / (24.8 + 31.0) = 386$ kN
 Mode 3 $F_{t,3,rd} = \Sigma F_{t,rd} = 2 \times 254 = 508$ kN
 $F_{t,rd} = \min(465, 386, 508) = 386$ kN

17.11. Column-web in transverse tension (Eave connection)

(EC3-1-8 §6.2.6.3)

$F_{t,wc,rd} = \omega \cdot b_{eff,t,wc} \cdot t_{wc} \cdot f_y / \gamma_{M0}$
 $\beta=1, \omega=\omega_1=1/\sqrt{[1+1.3(b_{eff,c} \cdot t_{wc} / A_{vc})^2]}, b_{eff,c}=90.0$ mm (EC3-1-8 §6.2.6.2, Tab.6.3)
 $\omega=1/\sqrt{[1+1.3 \times (90.0 \times 12.0 / 8380)^2]}=0.99$
 $F_{t,wc,rd} = [10^{-3}] \times 0.99 \times 90.0 \times 12.0 \times 355 / 1.00 = 380$ kN

17.12. Design resistance of compression stiffener (Eave connection)

(EC3-1-5 §9.1)

Compression stiffener at the bottom of haunch $t_s = 20.0$ mm

$f_y = 235$ N/mm², $b_s = (200 - 12.0 - 2 \times 24.0) / 2 = 70.0$ mm, $t_s = 20.0$ mm, $t_w = 12.0$ mm, $\varepsilon = \sqrt{(235 / f_y)} = 0.81$
 $A_{eff,s} = 2 \times 70.0 \times 20.0 + (2 \times 15 \times 0.81 \times 12.0 + 20.0) \times 12.0 = 6539$ mm² (EC3-1-5 §9.1 (2))
 $l_{eff,s} = \min(70.0, 14 \times 0.81 \times 20.0) = \min(70.0, 226.80) = 70.0$ mm, (EC3 Tab.5.2)
 $I_{eff,s} = (2 \times 70.0 + 12.0)^3 \times 20.0 / 12 = 5853.0 \times 10^3$ mm⁴
 $i_{eff,s} = \sqrt{(5853 \times 10^3 / 6539)} = 29.9$ mm, $\lambda_1 = \pi \sqrt{(E / f_y)} = 93.9 \varepsilon = 76.06$

$L_{cr} = 0.75 \times (600 - 2 \times 19.0) = 421.5 \text{ mm}$ (EC3-1-5 §9.4(2))
 $\bar{\lambda} = L_{cr} / (i_{eff, s} \cdot \lambda_1) = 421.5 / (29.9 \times 76.06) = 0.19$ (EC3 §6.3.1.3(1))
 $\bar{\lambda} < 0.20, \chi = 1.00$ (EC3 §6.3.1.2.4)
 $F_{c, wc, rd} = \chi \cdot A_{eff, s} \cdot f_y / \gamma_{M1} = 1.000 \times 6539 \times 235 / 1.00 = 1537 \text{ kN} > F_{c, fb, rd} = 940 \text{ kN}$
 Compression stiffener, I_s verified

17.13. Moment resistance of connection (Eave connection) (EN1993-1-8, §6.2.7.2)

$M_{j, rd} = \Sigma h_r \cdot F_{tr, rd}$ (EN1993-1-8, §6.2.7.2 Eq. 6.25)

h_r : row numbering from top, distances from center of bottom (compression) flange

End-plate in bending (EC3-1-8 §6.2.4.5)

Force distribution in bolt rows

Bolt-row 1, $h_r = 1037.0 \text{ mm}$, $F_{t, rd} = 270 \text{ kN}$

Bolt-row 2, $h_r = 931.0 \text{ mm}$, $F_{t, rd} = 380 \text{ kN}$

Bolt-row 3, $h_r = 841.0 \text{ mm}$, $F_{t, rd} = 222 \text{ kN}$

$F_{c, ed} = \Sigma F_{t, rd} = 270 + 380 + 222 = 872 \text{ kN}$

End-plate in bending (EC3-1-8 §6.2.4.4)

Force distribution in bolt rows

Bolt-row 1, $h_r = 1037.0 \text{ mm}$, $F_{t, rd} = 391 \text{ kN}$

Bolt-row 2, $h_r = 931.0 \text{ mm}$, $F_{t, rd} = 386 \text{ kN}$

Bolt-row 3, $h_r = 841.0 \text{ mm}$, $F_{t, rd} = 386 \text{ kN}$

$F_{c, ed} = \Sigma F_{t, rd} = 391 + 386 + 386 = 1163 \text{ kN}$

Rafter web in tension (EC3-1-8 §6.2.6.8)

$F_{t, wb, rd} = 326 \text{ kN}$

Rafter flange and web in compression (EC3-1-8 §6.2.4.7)

$F_{c, fb, rd} = 940 \text{ kN}$

$F_{t, rd} \leq F_{t, wb, rd} = 326 \text{ kN}$, $F_{c, ed} = \Sigma F_{t, rd} \leq F_{c, fb, rd} = 940 \text{ kN}$

$F_{c, ed} = \Sigma F_{t, rd} \leq F_{c, wc, rd} = 1537 \text{ kN}$

Force distribution in bolt rows (EC3-1-8 §6.2.7.2.(7))

Bolt-row 1, $h_r = 1037.0 \text{ mm}$, $F_{t, rd} = 270 \text{ kN}$

Bolt-row 2, $h_r = 931.0 \text{ mm}$, $F_{t, rd} = 326 \text{ kN}$

Bolt-row 3, $h_r = 841.0 \text{ mm}$, $F_{t, rd} = 222 \text{ kN}$

$F_{c, ed} = \Sigma F_{t, rd} = 270 + 326 + 222 = 818 \text{ kN}$

Moment resistance of connection (EN1993-1-8, §6.2.7.2(10))

$M_{j, rd} = [10^{-3}] \times [270 \times 1037.0 + 326 \times 931.0 + 222 \times 841.0]$

$M_{j, rd} = 770 \text{ kNm}$

$M_{ed} = 348.4 \text{ kNm} < 770.2 \text{ kNm} = M_{j, rd}$, I_s verified

17.14. Shear resistance (Eave connection) (EN1993-1-8, §3.6.1 Tab.3.4)

Shear resistance of bolts

$F_{v, rd} = \alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2} = [10^{-3}] \times 0.50 \times 1000 \times 353.0 / 1.25 = 141 \text{ kN}$

Shear plane of bolt: through the threaded portion

Bearing resistance of bolts

$F_{b, rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2}$

End-Plate

$t = 20.0 \text{ mm}$, $d = 24 \text{ mm}$, $d_o = 26 \text{ mm}$, $e_1 = 50 \text{ mm}$, $e_2 = 50 \text{ mm}$, $p_1 = 90 \text{ mm}$, $f_{ub} = 1000 \text{ kN/mm}^2$, $f_u = 360 \text{ kN/mm}^2$,

$\alpha_b = \min[f_{ub}/f_u, 1.0, e_1/3d_o, p_1/3d_o - 1/4] =$

$= \min[1000/360, 1.0, 50/(3 \times 26), 90/(3 \times 26) - 0.25] = 0.64$

$k_1 = \min[2.8e_2/d_o - 1.7, 1.4p_2/d_o - 1.7, 2.5] = \min[2.8 \times 50/26 - 1.7, 1.4 \times 100/26 - 1.7, 2.5] = 2.50$

$F_{b, rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2} = [10^{-3}] \times 2.50 \times 0.64 \times 360 \times 24 \times 20.0 / 1.25 = 222 \text{ kN}$

Column-Side

$t=19.0\text{mm}$, $d=24\text{mm}$, $d_o=26\text{mm}$, $e_1=50\text{mm}$, $e_2=50\text{mm}$, $p_1=90\text{mm}$, $f_{ub}=1000\text{kN/mm}^2$, $f_u=510\text{kN/mm}^2$,
 $\alpha_b=\min[f_{ub}/f_u, 1.0, e_1/3d_o, p_1/3d_o-1/4]=$
 $=\min[1000/510, 1.0, 50/(3 \times 26), 90/(3 \times 26)-0.25]=0.64$
 $k_1=\min[2.8e_2/d_o-1.7, 1.4p_2/d_o-1.7, 2.5]=\min[2.8 \times 50/26-1.7, 1.4 \times 100/26-1.7, 2.5]=2.50$
 $F_b, r_d=k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2} = [10^{-3}] \times 2.50 \times 0.64 \times 510 \times 24 \times 19.0 / 1.25 = 298 \text{ kN}$

Design resistance of one bolt in shear $=\min(141, 222, 298)=141 \text{ kN}$

Bending moment and shear

(EN1993-1-8, §3.6.1 Tab.3.4)

Maximum tension force in bolts

$F_{t,ed}=326/2=163 \text{ kN}$

Reduction of shear resistance due to bending

$\rho=1-F_{t,ed}/1.40F_{t,rd}=1-163/(1.40 \times 254)=0.54$

Shear acting together with bending moment for all the bolts

$V_{rd}=8 \times 0.54 \times 141 = 609 \text{ kN}$

$V_{ed}=110 \text{ kN} < 609 \text{ kN} = V_{rd}$, Is verified

Steel Portal Frame EC3
Example Report

18. Column base Connection

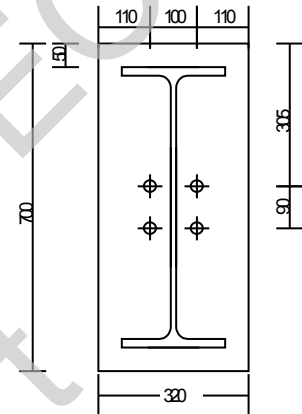
18.1. Basic data (Base connection)

Design forces of connection (Base connection)

Axial force (compression) Ned=-119 kN, L.C. 202: 1.35Gk+1.50Qs1
 Axial force (tension) Ned= 16 kN, L.C. 111: 0.90Gk+1.50Qw1
 Shear force Ved= 75 kN, L.C. 202: 1.35Gk+1.50Qs1
 Moment Med= 0 kNm,

Connection data (Base connection)

Base plate steel grade 700x320x30 mm, S 235
 Anchor bolts M24, Grade 5.6
 Shear plane of bolt through the threaded portion
 middle 2x2=4
 Total number of bolts =4
 Diameter of holes do = 26 mm
 Steel section for column IPE 600, S 355
 Spacing between cross centers 100 mm
 Flange to end-plate weld 11 mm
 Web to end-plate weld 7 mm



Edge distances and spacing of bolts

Distance of plate edge to bolt line e1=e2=ex= 110 mm
 Distance of section edge to bolt line ec= 44 mm
 Distance of flange edge to bolt line ef= 45 mm
 Pitch between bolt rows p1=p3=p= 90 mm
 Spacing between cross centers p2=g=w= 100 mm
 Flange to end-plate weld atf>= 0.55tf=0.55x19.0= 11 mm
 Web to end-plate weld aw>= 0.55tw=0.55x12.0= 7 mm

Concrete of foundation

Concrete-Steel class C25/30-B500C (EC2 §3.1, §3.2)
 Partial factors for materials $\gamma_c=1.50, \gamma_s=1.15$ (EC2 §2.4.2.4)
 Design compressive strength $f_{cd}=\alpha_{cc} \cdot f_{ck} / \gamma_c = 1.00 \times 25 / 1.50 = 16.67 \text{ N/mm}^2$ (EC2 §3.1.6)
 Design tensile strength $f_{ctd}=\alpha_{ct} \cdot f_{ctk05} / \gamma_c = 1.00 \times 2 / 1.50 = 1.20 \text{ N/mm}^2$
 Bearing strength $f_{jd}=\beta \cdot \sqrt{A_c1/A_c0} \cdot f_{cd} = (2/3) \times 1.5 \times 16.67 = 16.67 \text{ N/mm}^2$ (EC2 §6.7)

18.2. Design resistance of individual bolts (Base connection)

(EC3-1-8 §3.6.1, Tab.3.4)

Bolt strength grade=5.6, $f_{ub} = 500 \text{ N/mm}^2, A_s=353.0 \text{ mm}^2, \gamma_{M2}=1.25$
 Tension resistance of bolts $F_{t,rd}=k_2 \cdot f_{ub} \cdot A_s / \gamma_{M2}, (k_2=0.90)$
 $F_{t,rd}=[10^{-3}] \times 0.90 \times 500 \times 353.0 / 1.25 = 127 \text{ kN}$
 Shear resistance of bolts $F_{v,rd}=\alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2}, (\alpha_v=0.60)$
 $F_{v,rd}=[10^{-3}] \times 0.60 \times 500 \times 353.0 / 1.25 = 85 \text{ kN}$

18.3. Connection geometry of end-plate (Base connection)

(EC3-1-8 §6.2.4.1, Fig.6.2)

$e=e_x=110 \text{ mm}, e_{min}=110 \text{ mm}$
 $m_{x,x}=(100-12.0-2 \times 0.8 \times 7 \times \sqrt{2}) / 2 = 36.1 \text{ mm}$
 $m_{x,y}= 36.1 \text{ mm}$
 $n_{x,x}= e_{min} \leq 1.25 m_{x,x} = \min(110.0, 1.25 \times 36.1) = 45.1 \text{ mm}$
 $n_{x,y}= e_{min} \leq 1.25 m_{x,y} = \min(110.0, 1.25 \times 36.1) = 45.1 \text{ mm}$
 $\min(m_{x,x}, m_{x,y}) = \min(36.1, 36.1) = 36.1 \text{ mm}, \max(m_{x,x}, m_{x,y}) = \max(36.1, 36.1) = 36.1 \text{ mm}$
 $\min(n_{x,x}, n_{x,y}) = \min(45.1, 45.1) = 45.1 \text{ mm}, \max(n_{x,x}, n_{x,y}) = \max(45.1, 45.1) = 45.1 \text{ mm}$

18.4. Effective lengths of end-plate (Base connection)

(EC3-1-8 §6.2.6.5 Tab.6.6)

Inner Bolt-row in a group

$$\begin{aligned} l_{eff} &= 2n \cdot m_x = 2 \times 36.1 = 226.8 \text{ mm} \\ &= 4m + 1.25e = 4 \times 36.1 + 1.25 \times 110.0 = 281.9 \text{ mm} \\ &= 2p = 2 \times 90.0 = 180.0 \text{ mm} \\ &= p = 90.0 \text{ mm} \\ l_{eff,4b} &= \min(226.8, 281.9, 180.0, 90.0) = 90.0 \text{ mm} \\ l_{eff,4b} &= 90.0 \text{ mm} \end{aligned}$$

18.5. End-Plate, Resistance of T-stub flange (Base connection)

(EC3-1-8 §6.2.4.1, Tab.6.2)

Inner Bolt-row in a group

$$\begin{aligned} M_{pl,1,rd} &= M_{pl,2,rd} = 0.25 l_{eff} \cdot t_f^2 \cdot f_y / \gamma_{M0} = [10^{-6}] \times 0.25 \times 90.0 \times 30.0^2 \times 235 / 1.00 = 4.759 \text{ kNm} \\ \text{Mode 1} \quad F_{t,1,rd} &= 4 M_{pl,1,rd} / m = [10^3] \times 4 \times 4.759 / 36.1 = 527 \text{ kN} \\ \text{Mode 2} \quad F_{t,2,rd} &= (2 M_{pl,2,rd} + n \Sigma F_{t,rd}) / (m+n) = ([10^3] \times 2 \times 4.759 + 45.1 \times 2 \times 127) / (36.1 + 45.1) = 258 \text{ kN} \\ \text{Mode 3} \quad F_{t,3,rd} &= \Sigma F_{t,rd} = 2 \times 127 = 254 \text{ kN} \\ F_{t,rd} &= \min(527, 258, 254) = 254 \text{ kN} \end{aligned}$$

18.6. Column web in tension (Base connection)

(EC3-1-8 §6.2.6.8)

$$\begin{aligned} F_{t,wb,rd} &= b_{eff,t,wb} \cdot t_{wb} \cdot f_{y,wb} / \gamma_{M0} \\ b_{eff,t,wb} &= l_{eff,4b} = 90.0 \text{ mm} \\ F_{t,wb,rd} &= [10^{-3}] \times 90.0 \times 12.0 \times 355 / 1.00 = 383 \text{ kN} \end{aligned}$$

$$\min F_{t,rd} = \min(254, 383) = 254 \text{ kN}$$

18.7. Tension resistance of connection

(EN1993-1-8, §6.2.4)

$$\begin{aligned} \text{Uplift force of connection} \quad F_{t,ed} &= 16 \text{ kN} \\ \text{Tension resistance of connection} \quad F_{t,rd} &= 2 \times 254 = 508 \text{ kN} \\ N_{ed} &= 16 \text{ kN} < 508 \text{ kN} = N_{rd}, \text{ Is verified} \end{aligned}$$

18.8. Shear resistance (Base connection)

(EN1993-1-8, §3.6.1 Tab.3.4)

Shear resistance of bolts

$$\begin{aligned} F_{v,rd} &= \alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2} = [10^{-3}] \times 0.60 \times 500 \times 353.0 / 1.25 = 85 \text{ kN} \\ \text{Shear plane of bolt: through the threaded portion} \end{aligned}$$

Bearing resistance of bolts

$$F_{b,rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2}$$

$$\begin{aligned} t &= 30.0 \text{ mm}, d = 24 \text{ mm}, d_o = 26 \text{ mm}, e_1 = 110 \text{ mm}, e_2 = 110 \text{ mm}, p_1 = 90 \text{ mm}, f_{ub} = 500 \text{ kN/mm}^2, f_u = 360 \text{ kN/mm}^2, \\ \alpha_b &= \min[f_{ub}/f_u, 1.0, e_1/3d_o, p_1/3d_o - 1/4] = \\ &= \min[500/360, 1.0, 110/(3 \times 26), 90/(3 \times 26) - 0.25] = 0.90 \\ k_1 &= \min[2.8e_2/d_o - 1.7, 1.4p_2/d_o - 1.7, 2.5] = \min[2.8 \times 110/26 - 1.7, 1.4 \times 100/26 - 1.7, 2.5] = 2.50 \\ F_{b,rd} &= k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2} = [10^{-3}] \times 2.50 \times 0.90 \times 360 \times 24 \times 30.0 / 1.25 = 469 \text{ kN} \end{aligned}$$

$$\text{Design resistance of one bolt in shear} = \min(85, 469) = 85 \text{ kN}$$

Tension and shear

(EN1993-1-8, §3.6.1 Tab.3.4)

Maximum tension force in bolts

$$F_{t,ed} = 254 / 2 = 127 \text{ kN}$$

Reduction of shear resistance due to tension

$$\rho = 1 - F_{t,ed} / 1.40 F_{t,rd} = 1 - 127 / (1.40 \times 127) = 0.29$$

Shear acting together with tension for all the bolts

$$V_{rd} = 4 \times 0.29 \times 85 = 99 \text{ kN}$$

$$V_{ed} = 75 \text{ kN} < 99 \text{ kN} = V_{rd}, \text{ Is verified}$$

18.9. Bearing resistance (Base connection)

(EN1993-1-8, §6.2.5)

Compression resistance of T-stub flange $F_{c,rd} = f_{jd} \cdot b_{eff} \cdot l_{eff}$ (§6.2.5(3) Eq. 6.4)
 $f_{jd} = \beta \cdot \sqrt{A_{c1}/A_{co}} \cdot f_{cd} = (2/3) \times 1.5 \times 16.67 = 16.67 \text{ N/mm}^2$ (EC3-1-8 §6.2.5(7))
 $h = 600.0 \text{ mm}$, $b = 220.0 \text{ mm}$, $t_f = 19.0 \text{ mm}$, $t_w = 12.0 \text{ mm}$, $t_p = 30.0 \text{ mm}$
 $c = t_p \cdot (f_y / (3f_{jd} \cdot \gamma_{M0}))^{0.5} = 30 \times (235.00 / (3 \times 16.67 \times 1.00))^{0.5} = 65.0$, < 50.0 , $c = 50.0 \text{ mm}$ (Eq. 6.5)
 $2c + b_f = 2 \times 50.0 + 220 = 320.0 \text{ mm} \leq b_p = 320 \text{ mm}$, $l_{eff} = 320.0 \text{ mm}$
 $A_{co,f} = l_{eff} \cdot (2c + t_f) = 320.0 \times (2 \times 50.0 + 19.0) = 38080 \text{ mm}^2$ (EC3-1-8, Fig. 6.4)
 $A_{co,w} = (h - 2t_f - 2c) \cdot (t_w + 2c) = (600.0 - 2 \times 19.0 - 2 \times 50.0) \times (12.0 + 2 \times 50.0) = 51744 \text{ mm}^2$
 $N_{j,rd} = [10^{-3}] \times 16.7 \times (2 \times 38080 + 51744) = [10^{-3}] \times 16.7 \times 127904 = 2136 \text{ kN}$
 $N_{j,ed} = 119 \text{ kN} < 2136 \text{ kN} = N_{j,rd}$, Is verified

18.10. Anchoring resistance (Base connection)

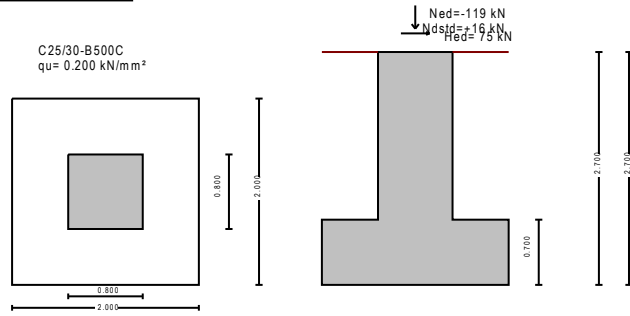
(EN1993-1-8, §6.2.6.12)

Anchoring hook

(EN1992-1-1 §8.4)

Number of fasteners: 4, of diameter 24mm, $A_s = 353 \text{ mm}^2$
 Basic required anchorage length $l_{b,rqd}$, Design anchorage length $l_{bd} = 0.70 l_{b,rqd}$
 $l_{b,rqd} = (\varnothing/4) (\sigma_{sd}/f_{bd}) = (24/4) \times (11.5/1.20) = 57 \text{ mm}$
 $\sigma_{sd} = [10^3] \times 16 / (4 \times 353) = 11.5 \text{ N/mm}^2$, $f_{bd} = f_{ctd} = 1.20 \text{ N/mm}^2$
 Design anchorage length $l_{bd} = 0.70 \times 57 > (10 \times 24, 100)$ $l_{bd} = 250 \text{ mm}$

19. Concrete footing



19.1. Design loads on concrete footing

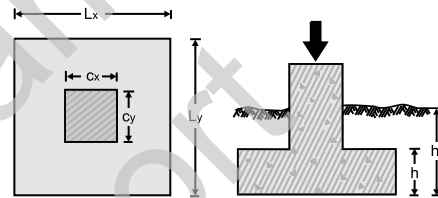
Axial force (downwards)	Ned= 119 kN, L.C. 202: 1.35Gk+1.50Qs1
Axial force (upwards)	Ned= 16 kN, L.C. 111: 0.90Gk+1.50Qw1
Shear force	Hed= 75 kN, L.C. 202: 1.35Gk+1.50Qs1
Moment	Med= 0 kNm,

19.2. Dimensions, materials, loads (Concrete footing)

Dimensions

Footing	Lx= 2.000 m	Ly= 2.000 m
Column	cx= 0.800 m	cy= 0.800 m
Height of footing	h= 0.700 m	
Depth of footing	hf= 2.700 m	

Base area of footing	Af= 4.00 m ²
Volume of footing	Vf= 4.08 m ³



Materials of footing

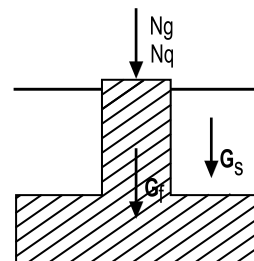
Concrete-Steel class: C25/30-B500C	(EN1992-1-1, §3)
Concrete cover: Cnom=35 mm	(EC2 §4.4.1)
Effective depth of cross section d=h-d1, d1=Cnom+Ø(3/2)=35+3x16/2=59mm, d=700-59=641mm	
Concrete weight: 25.0 kN/m ³	
γc=1.50, γs=1.15	(EC2 Table 2.1N)
fcd=acc·fck/γc=1.00x25/1.50=16.67 MPa	(EC2 §3.1.6)
fyd=fyk/γs=500/1.15=435 MPa	(EC2 §3.2.7)

Soil

Soil bearing pressure	qu= 0.200 N/mm ² (MPa)
Unit weight of soil	γ=18.000 kN/m ³

Loads

Self weight of footing	(1.28+2.80)x25.00	Gf= 102.00 kN
Soil weight on footing	(4.00x2.70-4.08)x18.00	Gs= 120.96 kN
Design Loads		
Vertical load downwards	Ned= 118.65 kN	
Vertical load upwards	Ndst,d= 16.22 kN	
Horizontal load	Hed= 75.48 kN	
Moment	Med= 0.00 kNm	



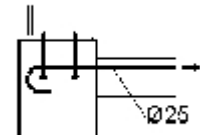
Eurocode parameters

<u>Check of soil bearing capacity</u>				(EC7 EN1997-1-1:2004, §6)		
Partial factors for actions and soil properties				(EC7 Tab. A.1-A.4, EC8-5 §3.1)		
Equilibrium limit state (EQU), Structural limit state (STR), Geotechnical limit state (GEO)				(EQU)	(STR)	(GEO)
Actions	Permanent Unfavourable		γ_{Gdst} : 1.10	1.35	1.00	
	Permanent Favourable		γ_{Gstb} : 0.90	1.00	1.00	
	Variable Unfavourable		γ_{Qdst} : 1.50	1.50	1.30	
	Variable Favourable		γ_{Qstb} : 0.00	0.00	0.00	
Soil parameters	Angle of shearing resistance	γ_{ϕ} :	1.25	1.00	1.25	
	Effective cohesion	γ_c :	1.25	1.00	1.25	
	Undrained shear strength	γ_{cu} :	1.40	1.00	1.40	
	Unconfined strength	γ_{qu} :	1.40	1.00	1.40	
	Weight density	γ_w :	1.00	1.00	1.00	
Partial safety factors for actions : $\gamma_G=1.35, \gamma_Q=1.50$				(EC0 Annex A1)		
Combination of accidental actions : (EC7) $\psi_2 = 0.30$						
Combination of accidental actions : (EC2) $\psi_2 = 0.30$						

Design of reinforced concrete (EC2 EN1992-1-1:2004)

19.3. Tie for horizontal forces (Concrete footing)

The horizontal force acting outwards, is resisted by a steel tie cast into the floor slab connected to the base of the columns
 Maximum horizontal force force acting outwards Hed= 75 kN
 Steel B500C, ($f_{yk}=500N/mm^2$)
 Required steel area $A_s = Hed / (f_y / \gamma_s) = 10^3 \times 75 / (500 / 1.15) = 174 mm^2$
 Provide 2 steel bars $\varnothing 25$ mm, ($A_s = 982 mm^2$)

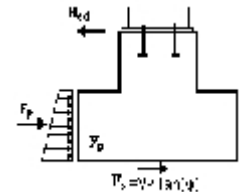


Necessary anchor length (bars with standard hook) (EN1992-1-1 §8.4)
 Basic required anchorage length $l_{b, reqd} = (\varnothing / 4) (\sigma_{sd} / f_{bd}) = (25 / 4) \times (77 / 2.70) = 178$ mm
 $\sigma_{sd} = 10^3 \times 75 / (2 \times 491) = 77$ N/mm², $f_{bd} = 2.25 \times f_{ctd} = 2.25 \times 1.20 = 2.70$ N/mm²
 Design anchorage length $l_{bd} = 0.70 \times 178, > (10 \times 25, 100) = 260$ mm (EC2 §8.4.4)
 Design lap length $l_o = 1.5 \times 178, > (15 \times 25, 200) = 380$ mm (EC2 §8.7.3)

19.4. Passive earth pressure on the side of the foundation

(EC7 EN1997-1-1:2004, §9.5)

Angle of shearing resistance of ground $\phi / \gamma_M = 30.00 / 1.25 = 24.00^\circ$
 Unit weight of soil $\gamma = 18.00$ kN/m³
 Foundation depth $h_f = 2.700$ m
 Foundation height $h = 0.700$ m
 Foundation width $B_y = 2.000$ m
 Coefficient of passive earth pressure $K_p = 2.371$
 Earth pressure at the top $p_1 = 18.00 \times 2.000 \times 2.371 = 85.36$ kN/m²
 Earth pressure at the bottom $p_2 = 18.00 \times 2.700 \times 2.371 = 115.24$ kN/m²
 Earth force $F_{prd} = 0.5 \times (85.36 + 115.24) \times 2.000 \times 0.700 = 140.42$ kN
 Point of application of earth force $y_p = 0.433$ m



19.5. Check stability for forces upwards (Concrete footing)

Loading (EQU), 0.90xPermanent + 1.50xVariable (EC7 §2.4.7.2)
 Vertical forces upwards $N_{dst,d} = 16$ kN
 Vertical forces downwards $G = 102.00 + 120.96 = 222.96$ kN
 Holding down forces $N_{stb,d} = \gamma_G \times G = 0.90 \times 222.96 = 201$ kN

 $N_{dst,d} = 16$ kN < 201 kN = $N_{stb,d}$, Is verified

19.6. Check of soil bearing capacity (Concrete footing)

(EC7 EN1997-1-1:2004, §6)

Loading (STR,GEO), 1.35xPermanent + 1.50xVariable

(EC7 §2.4.7.3)

Design Loads

Vertical load at fundament bottom $N_{ed} = 118.65 + 1.35 \times (102.00 + 120.96) = 419.65 \text{ kN}$

Vertical load at fundament top $N_{ed1} = 118.65 + 1.35 \times 32.00 = 161.85 \text{ kN}$

Soil pressure $q = 10^{-3} \times 419.65 / (2.000 \times 2.000) = 0.105 \text{ N/mm}^2 \text{ (Mpa)}$

Check bearing resistance failure $R_d \geq V_d$

(EC7 EN1997-1-1:2004, §6.5.2)

Design effective foundation area $A' = 2.000 \times 2.000 = 4.00 \text{ m}^2$

(EC7 Annex D)

Design bearing resistance of footing $R_d = A' \cdot q_u / \gamma_{qu}$, $q_u = 0.20 \text{ N/mm}^2$, $\gamma_{qu}(\text{EQU,GEO}) = 1.40$

$R_d = 1000 \times 4.00 \times 0.200 / 1.40 = 571.43 \text{ kN} > V_d = 419.65 \text{ kN}$

$N_{ed} = 419.65 \text{ kN} < 571.43 \text{ kN} = N_{rd}$, Is verified

19.7. Design for bending (Concrete footing)

(EC2 EN1992-1-1:2004, §6.1)

Bending at bottom surface

$M_{ed}(yy) = 0.125 \times 162 \times 2.000 \times (1 - 0.800 / 2.000)^2 = 14.57 \text{ kNm}$

$M_{ed}(xx) = 0.125 \times 162 \times 2.000 \times (1 - 0.800 / 2.000)^2 = 14.57 \text{ kNm}$

$M_{ed} = 14.57 \text{ kNm}$, $b = 2000 \text{ mm}$, $d = 641 \text{ mm}$, $K_d = 23.75$, $x/d = 0.01$

$\epsilon_c / \epsilon_s = 0.2 / 20.0$, $K_s = 2.31$, $A_s = 0.52 \text{ cm}^2$

Minimum reinforcement $s \leq 400 \text{ mm}$ (Ø16/30.0, $A_s = 6.70 \text{ cm}^2/\text{m}$) (EC2 §9.3.1)

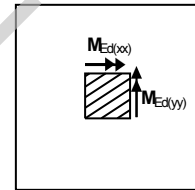
Minimum reinforcement Ø16/30.0 (6.70 cm^2/m)

$M_{ed} = 14.57 \text{ kNm}$, $b = 2000 \text{ mm}$, $d = 641 \text{ mm}$, $K_d = 23.75$, $x/d = 0.01$

$\epsilon_c / \epsilon_s = 0.2 / 20.0$, $K_s = 2.31$, $A_s = 0.52 \text{ cm}^2$

Minimum reinforcement $s \leq 400 \text{ mm}$ (Ø16/30.0, $A_s = 6.70 \text{ cm}^2/\text{m}$)

Minimum reinforcement Ø16/30.0 (6.70 cm^2/m)



Reinforcement of footing at bottom surface

Reinforcement in x-x direction: Ø16/30.0 (6.70 cm^2/m), 8Ø16 (16.08 cm^2)

Reinforcement in y-y direction: Ø16/30.0 (6.70 cm^2/m), 8Ø16 (16.08 cm^2)

Bending at top surface

$M_{ed}(yy) = 0.125 \times 16 \times 2.000 \times (1 - 0.800 / 2.000)^2 = 1.46 \text{ kNm}$

$M_{ed}(xx) = 0.125 \times 16 \times 2.000 \times (1 - 0.800 / 2.000)^2 = 1.46 \text{ kNm}$

$M_{ed} = 1.46 \text{ kNm}$, $b = 2000 \text{ mm}$, $d = 641 \text{ mm}$, $K_d = 75.03$, $x/d = 0.00$

$\epsilon_c / \epsilon_s = 0.1 / 20.0$, $K_s = 2.30$, $A_s = 0.05 \text{ cm}^2$

Minimum reinforcement $s \leq 400 \text{ mm}$ (Ø16/30.0, $A_s = 6.70 \text{ cm}^2/\text{m}$) (EC2 §9.3.1)

Minimum reinforcement Ø16/30.0 (6.70 cm^2/m)

$M_{ed} = 1.46 \text{ kNm}$, $b = 2000 \text{ mm}$, $d = 641 \text{ mm}$, $K_d = 75.03$, $x/d = 0.00$

$\epsilon_c / \epsilon_s = 0.1 / 20.0$, $K_s = 2.30$, $A_s = 0.05 \text{ cm}^2$

Minimum reinforcement $s \leq 400 \text{ mm}$ (Ø16/30.0, $A_s = 6.70 \text{ cm}^2/\text{m}$)

Minimum reinforcement Ø16/30.0 (6.70 cm^2/m)



Reinforcement of footing at top surface

Reinforcement in x-x direction: Ø16/30.0 (6.70 cm^2/m), 8Ø16 (16.08 cm^2)

Reinforcement in y-y direction: Ø16/30.0 (6.70 cm^2/m), 8Ø16 (16.08 cm^2)

19.8. Design for shear (Concrete footing)

(EC2 EN1992-1-1:2004, §6.2)

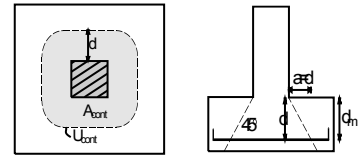
The design for shear is covered by the design in punching shear, because the critical rupture surface is considered at angle 45°

19.9. Design for punching shear (Concrete footing)

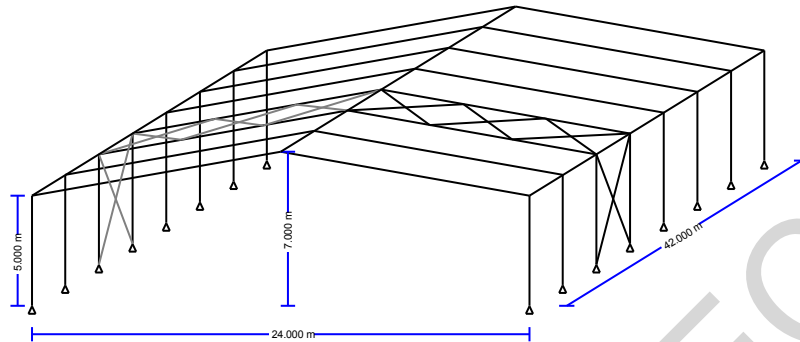
(EC2 EN1992-1-1:2004, §6.4)

Footing cantilevers in x-x, $L_1=0.600<d=0.641\text{m}$, $L_2=0.600<d=0.641\text{m}$ Footing cantilevers in y-y, $L_1=0.600<d=0.641\text{m}$, $L_2=0.600<d=0.641\text{m}$

the width of footing cantilevers is $<$ footing height d .
The critical rupture surface at angle 45° ,
is outside the area of the footing.
The check for punching shear is satisfied



Steel Portal Frame EC3
Example Report



20. Transverse restraint system

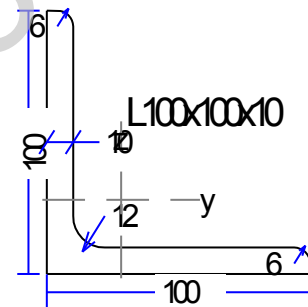
Number of frames in transverse direction 8, at 6.000m apart. Totally 1 bracing systems are provided. Each bracing system carries 1/1=1.00 of the total horizontal load. The roof bracing system consists of wind girders diagonally between 24/6=4.000m points. The vertical bracing system at the columns, consists of 2 diagonal girders from the top to the bottom of the next column, acting as strut/tie.

20.1. Cross-section properties, Bracing member

Cross-section L100x100x10-S 355

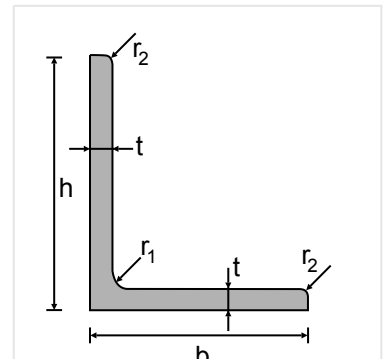
Dimensions of cross section

Depth of cross section	h=	100.00 mm
Width of cross section	b=	100.00 mm
Web depth	hw=	100.00 mm
Depth of straight portion of web	dw=	100.00 mm
Web thickness	tw=	10.00 mm
Flange thickness	tf=	10.00 mm
Radius of root fillet	r=	12.00 mm
Mass	=	15.00 Kg/m



Properties of cross section

Area	A=	1915 mm ²	
Second moment of area	I _y =	1.767x10 ⁶ mm ⁴	I _z = 1.767x10 ⁶ mm ⁴
Second moment of area	I _u =	2.807x10 ⁶ mm ⁴	I _v = 0.726x10 ⁶ mm ⁴
Section modulus	W _y =	24.610x10 ³ mm ³	W _z =24.610x10 ³ mm ³
Plastic section modulus	W _{py} =	106.00x10 ³ mm ³	W _{pz} =52.000x10 ³ mm ³
Radius of gyration	i _y =	30.4 mm	i _z = 30.4 mm
Radius of gyration	i _u =	38.3 mm	i _v = 19.5 mm
Shear area	A _{vz} =	1025 mm ²	A _{vy} = 1000 mm ²
Torsional constant	I _t =	0.089x10 ⁶ mm ⁴	i _p = 43 mm
Warping constant	I _w =	1.688x10 ⁹ mm ⁶	



20.2. Horizontal loadings

Wind load on wall surface	, w _k =0.90kN/m ² , C _{pe} ,D=0.8, C _{pe} ,E=-0.5	(EN1991-1-4, Tab.7.1)
Transverse wind load/m on roof level	q _{ed,w} = 1.50x0.90x(0.8+0.5)x7.000/2= 6.14kN/m	
Load/m on bracing system, roof level	q _{ed} = (1/1)x6.14 =6.14 kN/m	
Load on bracing system, roof level	Q _{ed1} = 6.14x4.000 =24.6 kN	
Load on bracing system, at top of column	Q _{ed2} = 6.14x24.000/2= 73.7 kN	

Horizontal (roof) braced girder

The braced girder at roof is loaded with point horizontal loads $Q_{ed1} = 6.1 \times 4.000 = 24.6 \text{ kN}$ at the nodes of the bracing system (at spacing $L/6 = 4.000 \text{ m}$).

The braced girder is supported horizontally at the columns

Length of braced girder members 7.211 m , inclination $\varphi = 56.31^\circ$, $\tan\varphi = 6.000/4.000 = 1.500$

Forces in members of braced girder

Compression $N_{ced1} = 1.00 \times 24.6 / \sin 56.31 = 29.6 \text{ kN}$

Tension $N_{ted1} = 0.50 \times 24.6 / \sin 56.31 = 14.8 \text{ kN}$

Vertical (wall) braced girder

The vertical brace system is loaded with point horizontal load $Q_{ed2} = 73.7 \text{ kN}$ at the top of the column $h = 5.000 \text{ m}$.

Length of braced girder members 7.810 m , inclination $\varphi = 39.81^\circ$, $\tan\varphi = 5.000/6.000 = 0.833$

Forces in bracing members

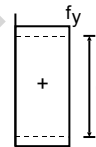
Tension $N_{ted2} = 1.00 \times 73.7 / \cos 39.81 = 95.9 \text{ kN}$

20.3. Classification of cross-sections, Compression N_c (Bracing member) (EN1993-1-1, §5.5)

$h/t = 100.0/10.0 = 10.00$, $(b+h)/2t = (100.0+100.0)/(2 \times 10.0) = 10.00$

S 355, $t = 10.0 \leq 40 \text{ mm}$, $f_y = 355 \text{ N/mm}^2$, $\epsilon = (235/355)^{0.5} = 0.81$

$h/t = 10.00 \leq 15\epsilon = 12.15$, $(b+h)/2t = 10.00 > 11.5\epsilon = 9.32$



Overall classification of cross-section is Class 4, Compression $N_{c,ed}$

Effective cross-section properties of Class 4 cross-sections (EN1993-1-1, §6.2.2.5)Web

$\bar{\lambda}_p = (b/t) / [28.40\epsilon\sqrt{K\sigma}]$ (EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3)

$b = d = 100.0 \text{ mm}$, $t = 10.0 \text{ mm}$, $\epsilon = 0.81$, $\psi = 1.00$, $K\sigma = 4.00$, $\bar{\lambda}_p = 0.217$

$\bar{\lambda}_p = 0.217 \leq 0.673$, $\rho = 1.0$, $d_{eff} = \rho \cdot d = 1.000 \times 100 = 100.0 \text{ mm}$

Flange

$\bar{\lambda}_p = (b/t) / [28.40\epsilon\sqrt{K\sigma}]$ (EN1993-1-3, §5.5.2, Eq.5.5, Tab1.5.3)

$b = c = 100.0 \text{ mm}$, $t = 10.0 \text{ mm}$, $\epsilon = 0.81$, $\psi = 1.00$, $K\sigma = 0.43$, $\bar{\lambda}_p = 0.663$

$\bar{\lambda}_p = 0.663 \leq 0.673$, $\rho = 1.0$, $c_{eff} = \rho \cdot c = 1.000 \times 100 = 100.0 \text{ mm}$

Effective area $A_{eff} = 1915 - 1 \times (100.0 - 100.0) \times 10.00 - 1 \times (100.0 - 100.0) \times 10.00 = 1915 \text{ mm}^2$

Effective area $A_{eff} = 0 \text{ mm}^2$

$e_{y,0.00} \text{ mm}$, $I_{y,eff} = 0.000 \times 10^6 \text{ mm}^4$

Effective section modulus $W_{y,eff} = 0.000 \times 10^6 / (100.0/2 + 0.00) = 0.000 \times 10^3 \text{ mm}^3$

20.4. Resistance of cross-section, Bracing member (EN1993-1-1, §6.2)Ultimate Limit State, Verification for tension (EN1993-1-1, §6.2.3)

$N_{t,ed} = 95.94 \text{ kN}$

Tension Resistance $N_{pl,rd} = A \cdot f_y / \gamma_{M0} = [10^{-3}] \times 1915 \times 355 / 1.00 = 679.82 \text{ kN}$

$N_{t,ed} = 95.94 \text{ kN} < 679.82 \text{ kN} = N_{t,rd} = N_{pl,rd}$, Is verified

Effective cross-section properties of Class 4 cross-sections (EN1993-1-1, §6.2.2.5)

Effective area $A_{eff} = 1915 \text{ mm}^2$

Ultimate Limit State, Verification for compression (EN1993-1-1, §6.2.4)

$N_{c,ed} = 29.60 \text{ kN}$

Compression Resistance $N_{crd} = A_{eff} \cdot f_y / \gamma_{M0} = [10^{-3}] \times 1915 \times 355 / 1.00 = 679.82 \text{ kN}$

$N_{ed} = 29.60 \text{ kN} < 679.82 \text{ kN} = N_{c,rd}$, Is verified

20.5. Flexural Buckling, Bracing member (Ultimate Limit State)

(EN1993-1-1, §6.3.1)

Buckling lengths: $L_{cr,y}=1.000 \times 7211=7211\text{mm}$, $L_{cr,z}=1.000 \times 7211=7211\text{mm}$

Non-dimensional slenderness (Cross-section Class: 4)

(EC3 §6.3.1.3)

$$\bar{\lambda}_y = \sqrt{(A \cdot f_y / N_{cr,y})} = (L_{cr,y} / i_y) \sqrt{(A_{eff}/A) / \lambda_1} = (7211 / 30.4) \times (1.000 / 76.06) = 3.121$$

$$\bar{\lambda}_z = \sqrt{(A \cdot f_y / N_{cr,z})} = (L_{cr,z} / i_z) \sqrt{(A_{eff}/A) / \lambda_1} = (7211 / 30.4) \times (1.000 / 76.06) = 3.121$$

$$\bar{\lambda}_v = \sqrt{(A \cdot f_y / N_{cr,v})} = (L_{cr,v} / i_v) \sqrt{(A_{eff}/A) / \lambda_1} = (7211 / 19.5) \times (1.000 / 76.06) = 4.868$$

$$\lambda_1 = \pi \sqrt{(E / f_y)} = 93.9 \varepsilon = 76.06, \quad \varepsilon = \sqrt{(235 / f_y)} = 0.81, \quad \sqrt{(A_{eff}/A)} = \sqrt{(1915 / 1915)} = 1.000$$

$$\bar{\lambda}_{eff,y} = 0.50 + 0.7 \times 3.121 = 2.685, \quad \bar{\lambda}_{eff,z} = 0.50 + 0.7 \times 3.121 = 2.685$$

(EC3 Annex BB.1.2)

$$\bar{\lambda}_{eff,v} = 0.35 + 0.7 \times 4.868 = 3.758$$

y-y buckling curve:b, imperfection factor: $\alpha_y=0.34$, $\chi_y=0.122$

(T.6.2,T.6.1, Fig.6.4)

$$\Phi_y = 0.5 [1 + \alpha_y (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = 0.5 [1 + 0.34 \times (2.685 - 0.2) + 2.685^2] = 4.526$$

$$\chi_y = 1 / [\Phi_y + \sqrt{(\Phi_y^2 - \bar{\lambda}_y^2)}] = 1 / [4.526 + \sqrt{(4.526^2 - 2.685^2)}] = 0.122 \leq 1 \quad \chi_y = 0.122$$

z-z buckling curve:b, imperfection factor: $\alpha_z=0.34$, $\chi_z=0.122$

$$\Phi_z = 0.5 [1 + \alpha_z (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = 0.5 [1 + 0.34 \times (2.685 - 0.2) + 2.685^2] = 4.526$$

$$\chi_z = 1 / [\Phi_z + \sqrt{(\Phi_z^2 - \bar{\lambda}_z^2)}] = 1 / [4.526 + \sqrt{(4.526^2 - 2.685^2)}] = 0.122 \leq 1 \quad \chi_z = 0.122$$

v-v buckling curve:b, imperfection factor: $\alpha_v=0.34$, $\chi_v=0.065$

$$\Phi_v = 0.5 [1 + \alpha_v (\bar{\lambda}_v - 0.2) + \bar{\lambda}_v^2] = 0.5 [1 + 0.34 \times (3.758 - 0.2) + 3.758^2] = 8.165$$

$$\chi_v = 1 / [\Phi_v + \sqrt{(\Phi_v^2 - \bar{\lambda}_v^2)}] = 1 / [8.165 + \sqrt{(8.165^2 - 3.758^2)}] = 0.065 \leq 1 \quad \chi_v = 0.065$$

$$\text{Reduction factor } \chi = 1 / [\Phi + \sqrt{(\Phi^2 - \bar{\lambda}^2)}], \quad \chi \leq 1.0, \quad \Phi = 0.5 [1 + \alpha (\bar{\lambda} - 0.2) + \bar{\lambda}^2], \quad \chi = 0.065$$

(EC3 Eq.6.49)

$$N_{b,rd} = \chi \cdot A_{eff} \cdot f_y / \gamma_{M1} = 0.065 \times [10^{-3}] \times 1915 \times 355 / 1.00 = 44.19 \text{ kN}$$

(EC3 Eq.6.48)

$$N_{c,ed} = 29.60 \text{ kN} < 44.19 \text{ kN} = N_{b,rd}, \quad \text{Is verified}$$

20.6. Bolts connecting bracesBolt connection data, Bracing member

(EN1993-1-8)

Type of connection End-plate connection, non-preloaded bolts

Category of connection Category A: Bearing type

(EC3-1-8 §3.4.1)

Connected members Thickness $t=10 \text{ mm}$

Bolts M20, Strength grade 10.9

Bolt diameter $d = 20 \text{ mm}$ Diameter of holes $d_o = 22 \text{ mm}$ Nominal area $\pi d^2 / 4 = \pi \times 20^2 / 4 = 314.2 \text{ mm}^2$ Tensile stress area $A_s = 314.2 \text{ mm}^2$ Bolt strength grade 10.9, $f_y = 900 \text{ N/mm}^2$, $f_{ub} = 1000 \text{ N/mm}^2$

(EC3-1-8 §3.1.1)

Shear resistance of bolts

(EN1993-1-8, §3.6.1 Tab.3.4)

$$F_{v,rd} = \alpha_v \cdot f_{ub} \cdot A_s / \gamma_{M2} = [10^{-3}] \times 0.50 \times 1000 \times 314.2 / 1.25 = 125.7 \text{ kN}$$

Bearing resistance of bolts

(EN1993-1-8, §3.6.1 Tab.3.4)

$$F_{b,rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2}$$

 $t=10.0\text{mm}$, $d=20\text{mm}$, $d_o=22\text{mm}$, $e_1=50\text{mm}$, $e_2=50\text{mm}$, $p_1=100\text{mm}$, $f_{ub}=1000\text{kN/mm}^2$, $f_u=360\text{kN/mm}^2$,

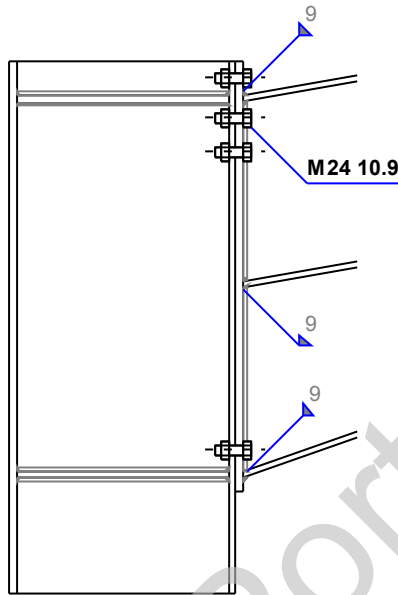
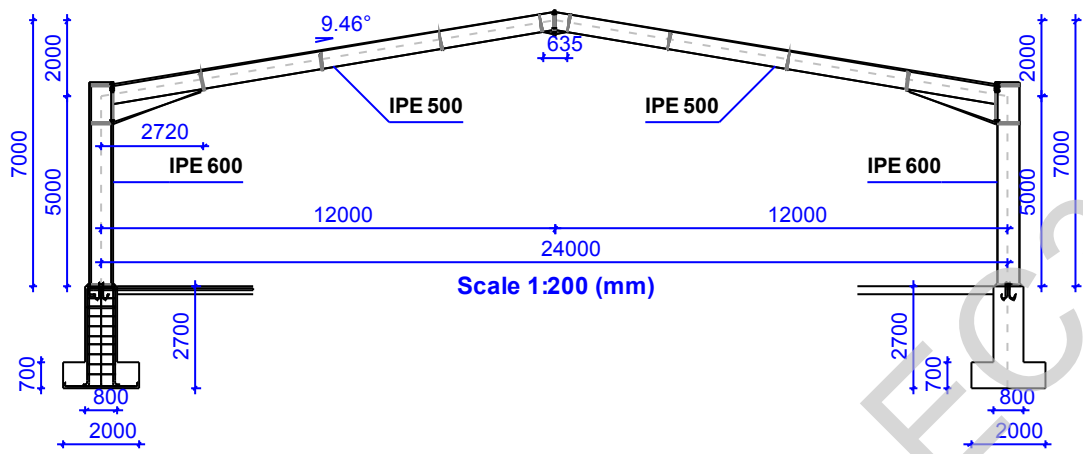
$$\alpha_b = \min[f_{ub}/f_u, 1, e_1/3d_o, p_1/3d_o - 1/4] = \min[1000/360, 1, 50/(3 \times 22), 100/(3 \times 22) - 0.25] = 0.76$$

$$k_1 = \min[2.8e_2/d_o - 1.7, 2.5] = \min[2.8 \times 50/22 - 1.7, 2.5] = 2.50$$

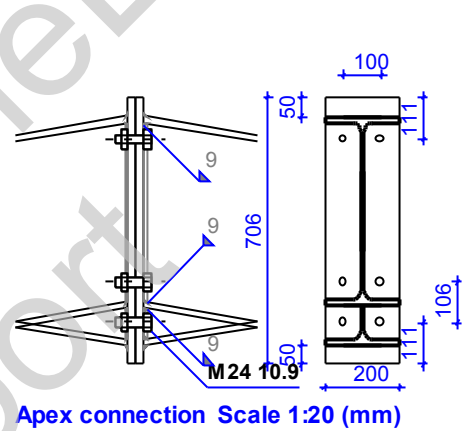
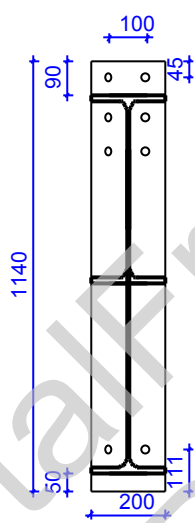
$$F_{b,rd} = k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t / \gamma_{M2} = [10^{-3}] \times 2.50 \times 0.76 \times 360 \times 20 \times 10.0 / 1.25 = 109.1 \text{ kN}$$

Necessary bolts per brace $95.9/109.1 = 1 \text{ M20, Grade 10.9}$

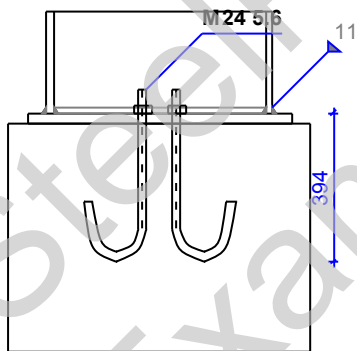
SteelPortalFrameEC3
Example Report



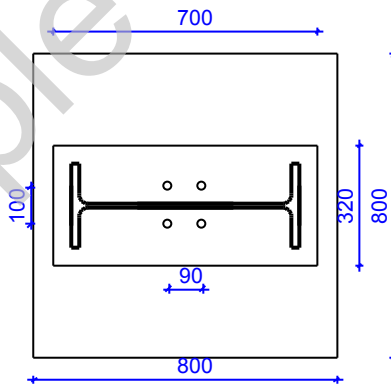
Eave connection Scale 1:20 (mm)

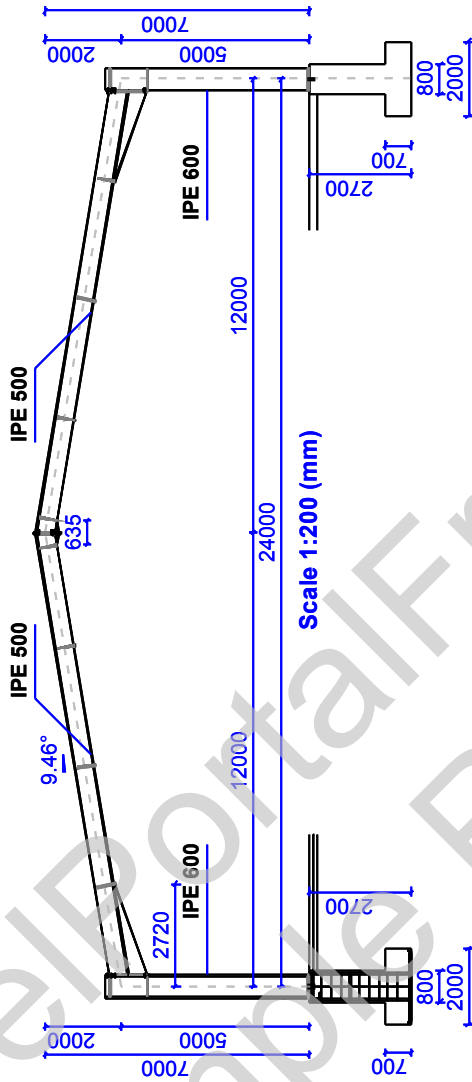


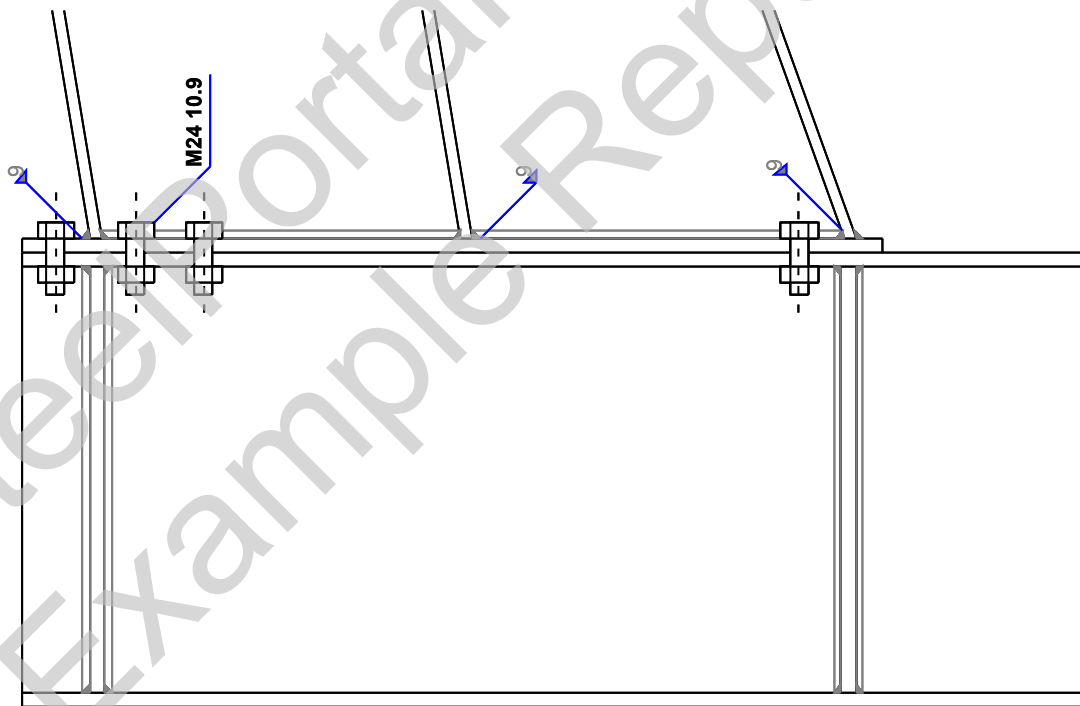
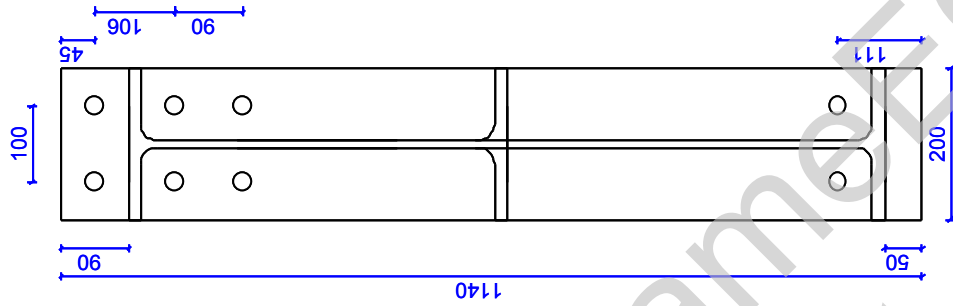
Apex connection Scale 1:20 (mm)



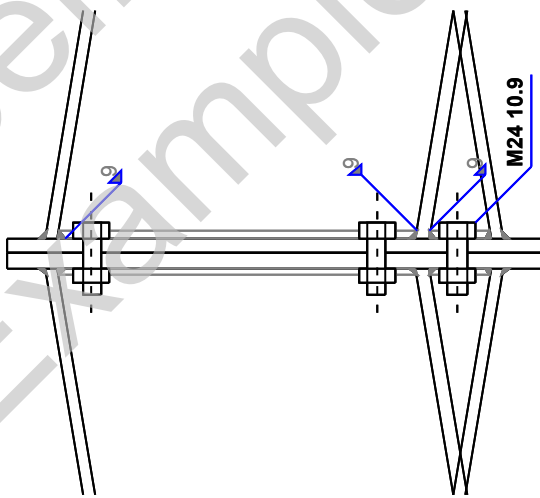
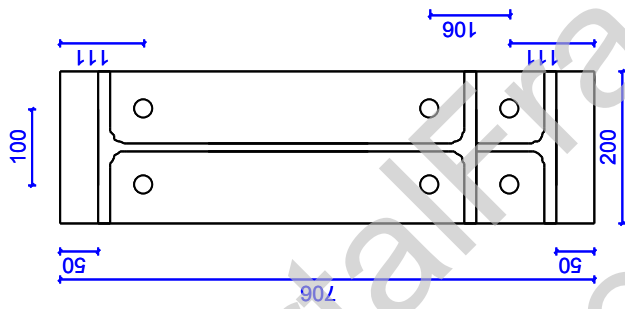
Base connection Scale 1:20 (mm)



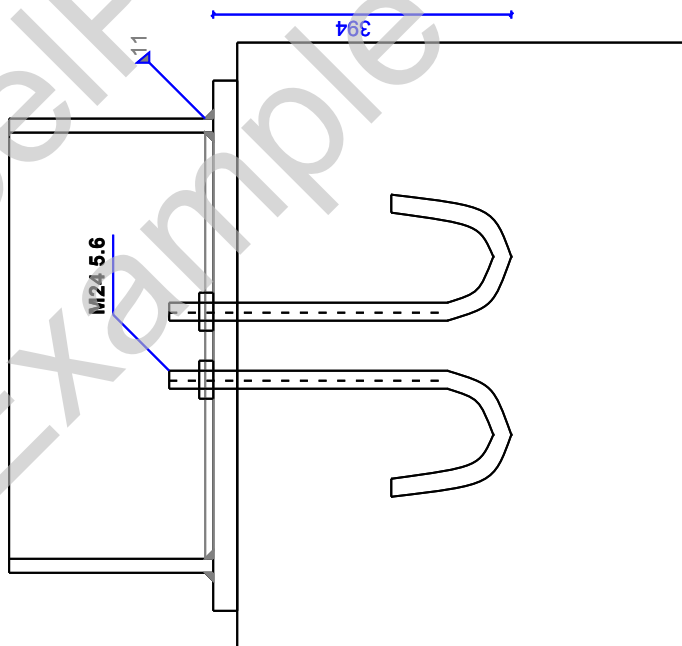
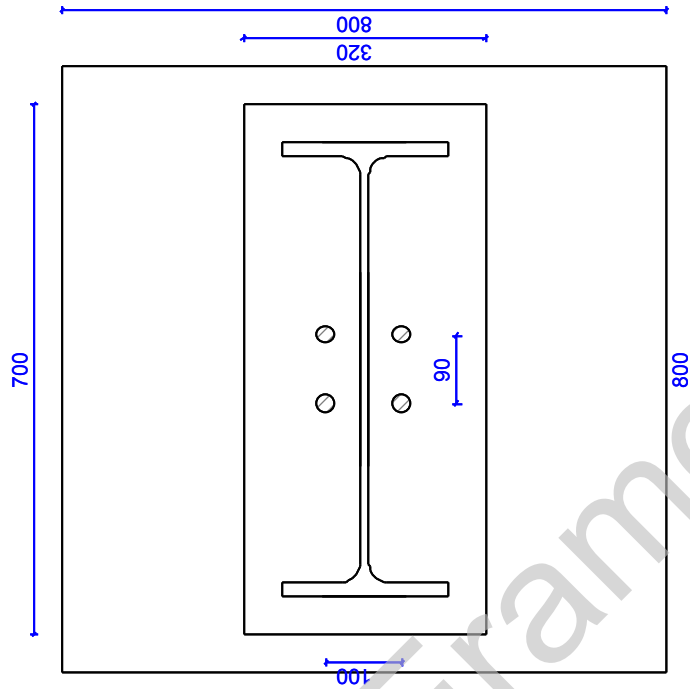




Eave connection Scale 1:10 (mm)



Apex connection Scale 1:10 (mm)



Base connection Scale 1:10 (mm)

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